## On $\mu \rightarrow e\gamma$ and $(g - 2)_{\mu}$ in Non-Sterile Electroweak Scale $\nu_{R}$ Models

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# Outline

### Introduction

- Minimal EW Scale  $\nu_R$  Model (PQ Hung, 2007)
- Motivations: Neutrino masses, Seesaw Mechanism, and All That
- Extension with A<sub>4</sub> Symmetry (Trinh Le & PQ Hung, 2015)

### • Calculations

- LFV Decay  $\mu \rightarrow e\gamma$
- Muon Magnetic Moment (g 2) $_{\mu}$
- Numerical Results
- Summary & Outlook

(In Collaborations with PQ Hung, Trinh Le and Van Que Tran, arXiv:1508.07016)

## Introduction

Non-Sterile EW scale  $v_R$  model (Minimal Version)

- Gauge Group Same as Standard Model
- Leptons  $l_{L} = \begin{pmatrix} \nu_{L} \\ e_{L} \end{pmatrix} \longleftrightarrow l_{R}^{M} = \begin{pmatrix} \nu_{R} \\ e_{R}^{M} \end{pmatrix},$   $e_{R} \iff e_{L}^{M}$ • Quarks  $q_{L} = \begin{pmatrix} u_{L} \\ d_{L} \end{pmatrix} \iff q_{R}^{M} = \begin{pmatrix} u_{R}^{M} \\ d_{R}^{M} \end{pmatrix},$   $u_{R}, d_{R} \iff u_{L}^{M}, d_{L}^{M}$
- Higgses (With Custodial Symmetry)

$$\Phi = \begin{pmatrix} \phi^{0*} & \phi^+ \\ \phi^- & \phi^0 \end{pmatrix} \qquad \chi = \begin{pmatrix} \chi^0 & \xi^+ & \chi^{++} \\ \chi^- & \xi^0 & \xi^+ \\ \chi^{--} & \xi^- & \chi^{0*} \end{pmatrix} \qquad \phi_S$$

$$(2, Y = 1/2) \qquad \tilde{\chi} (3, Y = 1/2) \quad \xi (3, Y = 0) \qquad (1, Y = 0)$$

Georgi-Machacek

PQ Hung, PLB 649 (2007)

## Motivations

- Motivation of the original model
   LFV processes to probe for new physics (SM contributions are minuscule!)
  - Parity Restoration (at high energies)
  - Non-perturbative (Lattice) formulation of SM (e.g. to study 1<sup>st</sup> Phase Transition etc)
  - Left mirrors Right (fermions)
  - Electroweak scale non-sterile  $\nu_R$  ('Testable' Seesaw Mechanism)
  - Embed-able into GUT like  $E_6$
- Two Extensions

- Mirror Higgs doublet was introduced to accommodate the 125 GeV scalar resonance observed at LHC

[Hoang, Hung, Kamat, 1412.0343]

- Introduce a A4 triplet of scalar singlets  $\{\varphi_{Si}\}$  to account for lepton mixing effects [Hung and Le, 1501.02538]



## Neutrino Masses in EW scale $v_R$ Model

Majorana Mass from Triplet

$$\mathcal{L}_{M} = g_{M} l_{R}^{M,T} \sigma_{2} \tau_{2} \tilde{\chi} l_{R}^{M}$$

$$= g_{M} \nu_{R}^{T} \sigma_{2} \nu_{R} \chi^{0} + \cdots$$

$$\rightarrow M_{R} \nu_{R}^{T} \sigma_{2} \nu_{R} + \cdots$$
(As opposed to GUT scale!)
with  $M_{R} = g_{M} \langle \chi_{0} \rangle = g_{M} v_{M} \ge M_{Z}/2 \approx 46 \text{ GeV}$ 

• Dirac Mass from Singlet

$$\mathcal{L}_{S} = g_{Sl} \overline{l}_{L} \phi_{S} l_{R}^{M} + \text{H.c.}$$
  
=  $g_{Sl} \overline{\nu}_{L} \phi_{S} \nu_{R} + \dots + \text{H.c.}$   
 $\rightarrow M_{D} \overline{\nu}_{L} \nu_{R} + \dots + \text{H.c.}$   
with  $M_{D} = g_{Sl} \langle \phi_{S} \rangle = g_{Sl} v_{S}$  (Not necessarily related to EW scale!)

• Light Neutrinos (See-Saw)

$$m_{\nu} = \frac{M_D^2}{M_R} < \mathcal{O}(\text{eV})$$

 $\sum m_{\nu} < 0.23 \,\mathrm{eV} \,[\mathrm{Planck}\, 2015]$ 

If  $g_{Sl} \sim \mathcal{O}(1)$ , then  $v_S \sim \mathcal{O}(10^{5-6} \,\mathrm{eV})$ ; If  $g_{Sl} \sim \mathcal{O}(10^{-6})$ , then  $v_S \sim \mathcal{O}(\Lambda_{EW} \sim 246 \,\mathrm{GeV})$ .

### Further Extension: A4 Model of Neutrino Masses

- Recently, the minimal model has been extended to include a A<sub>4</sub> symmetry in the neutrino sector (Hung & Le, arXiv:1501.02538).
- Instead of one, four Higgs singlets were introduced.

Field
$$(\nu, l)_L$$
 $(\nu, l^M)_R$  $e_R$  $e_M^M$  $\phi_{oS}$  $\tilde{\phi}_S$  $\Phi_2$  $A_4$  $\underline{3}$  $\underline{3}$  $\underline{3}$  $\underline{3}$  $\underline{1}$  $\underline{3}$  $\underline{1}$ 

- A<sub>4</sub> multiplication rule
- $\underline{3} \times \underline{3} = \underline{1}(11 + 22 + 33) + \underline{1}'(11 + \omega^2 22 + \omega 33) + \underline{1}''(11 + \omega 22 + \omega^2 33) + \underline{3}(23, 31, 12) + \underline{3}(32, 13, 21)$ 
  - Three Yukawa couplings are now possible for the neutrino Dirac mass  $\mathcal{L}_{S} = -\overline{l_{L}^{0}} \begin{pmatrix} g_{0S}\phi_{0S} + g_{1S}\tilde{\phi}_{S} + g_{2S}\tilde{\phi}_{S} \end{pmatrix} l_{R}^{M,0} + \text{H.c.}$   $\underline{3} \otimes \begin{pmatrix} \underline{1} & \underline{3} & \underline{3} \end{pmatrix} \underline{3}$ where  $g_{1S}$  and  $g_{2S}$  terms are the two possible ways that the triplet singlet

where  $g_{1S}$  and  $g_{2S}$  terms are the two possible ways that the triplet singlet couples to the product of lepton doublet and mirror lepton doublet. However  $(g_{2S})^* = g_{1S}$  from lepton mass reality!

• Similar Yukawa couplings for right-handed SM singlets can be written down with three new Yukawa couplings  $g'_{0S}$ ,  $g'_{1S}$ , and  $g'_{2S}$ .

### More Details of the Extension - I

• From the A<sub>4</sub> multiplication rules, we have

$$\mathcal{L}_S = -\overline{l_L^0} \left( g_{0S} \phi_{0S} + g_{1S} \tilde{\phi}_S + g_{2S} \tilde{\phi}_S \right) l_R^{M,0} + \text{H.c.}$$
$$= -\overline{l_L^0} M_\phi l_R^{M,0} + \text{H.c.}$$

where

$$M_{\phi} = \begin{pmatrix} g_{0S}\phi_{0S} & g_{1S}\phi_{3S} & g_{2S}\phi_{2S} \\ g_{2S}\phi_{3S} & g_{0S}\phi_{0S} & g_{1S}\phi_{1S} \\ g_{1S}\phi_{2S} & g_{2S}\phi_{1S} & g_{0S}\phi_{0S} \end{pmatrix} \longrightarrow M_{\nu}^{D} = \begin{pmatrix} g_{0S}v_{0} & g_{1S}v_{3} & g_{2S}v_{2} \\ g_{2S}v_{3} & g_{0S}v_{0} & g_{1S}v_{1} \\ g_{1S}v_{2} & g_{2S}v_{1} & g_{0S}v_{0} \end{pmatrix}$$

• Using  $v_0 = \langle \phi_{0S} \rangle$ ,  $v_i = \langle \phi_{iS} \rangle = v$ , we diagonalize  $M_{\nu}^D$ 

$$U_{\nu}^{\dagger}M_{\nu}^{D}U_{\nu} = \begin{pmatrix} m_{1D} & 0 & 0 \\ 0 & m_{2D} & 0 \\ 0 & 0 & m_{3D} \end{pmatrix},$$
Cabibbo (1978),  
Wolfenstein (1978)  

$$U_{\nu} = U_{CW}^{\dagger}$$
For charged lepton mixing!  

$$U_{\nu} = \frac{1}{\sqrt{3}} \begin{pmatrix} 1 & 1 & 1 \\ 1 & \omega^{2} & \omega \\ 1 & \omega & \omega^{2} \end{pmatrix}.$$

$$U_{\nu_{L}} = U_{\nu_{R}} = U_{\nu}$$

$$\omega = e^{2\pi i/3}$$

2015年10月23日星期五

### More Details of the Extension - II

• In the mass eigenstates,

$$l_L^0 = U_L^l l_L \ , \ l_R^{M,0} = U_R^{l^M} l_R^M$$

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the interaction becomes

$$\mathcal{L}_{S} = -\bar{l}_{L} U_{L}^{l\dagger} U_{\nu} U_{\nu}^{\dagger} M_{\phi} U_{\nu} U_{\nu}^{\dagger} U_{R}^{lM} l_{R}^{M} + \text{H.c.}$$
$$= -\bar{l}_{L} U_{\text{PMNS}}^{\dagger} \tilde{M}_{\phi} U_{\text{PMNS}}^{M} l_{R}^{M} + \text{H.c.},$$

where

$$\tilde{M}_{\phi} = U_{\nu}^{\dagger} M_{\phi} U_{\nu}$$
,  $U_{\text{PMNS}} = U_{\nu}^{\dagger} U_L^l$  and  $U_{\text{PMNS}}^M = U_{\nu}^{\dagger} U_R^{l^M}$ 

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• Including the SM right-handed singlets and mirror lefthanded doublets, the interaction is

$$\mathcal{L}_{S} = -\bar{l}_{L} U_{\text{PMNS}}^{\dagger} \tilde{M}_{\phi} U_{\text{PMNS}}^{M} l_{R}^{M} - \bar{l}_{R} U_{\text{PMNS}}^{\prime\dagger} \tilde{M}_{\phi}^{\prime} U_{\text{PMNS}}^{\prime M} l_{L}^{M} + \text{H.c.}$$

$$= -\sum_{i,m,k} (\mathcal{U}_{im}^{L\,k} \bar{l}_{Li} \phi_{kS} l_{Rm}^{M} + \mathcal{U}_{im}^{R\,k} \bar{l}_{Ri} \phi_{kS} l_{Lm}^{M}) + \text{H.c.}$$
where
$$U_{\text{PMNS}}^{\prime} = U_{\nu}^{\dagger} U_{R}^{l}, \quad U_{\text{PMNS}}^{\prime M} = U_{\nu}^{\dagger} U_{L}^{l}, \quad \text{and} \quad l_{R}^{0} = U_{R}^{l} l_{R} \quad , \quad l_{L}^{M,0} = U_{L}^{l^{M}} l_{L}^{M}.$$

$$\tilde{M}_{\phi}^{\prime} = U_{\nu}^{\dagger} M_{\phi}^{\prime} U_{\nu} \qquad M_{\phi}^{\prime} \text{ same as } M_{\phi} \text{ with } g_{0S} \rightarrow g_{0S}^{\prime}, g_{1S} \xrightarrow{\rightarrow} g_{1S}^{\prime}, g_{2S} \rightarrow g_{2S}^{\prime}.$$

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The Mixing Matrices $\mathcal{U}^L \& \mathcal{U}^R$
$\mathcal{U}_{im}^{Lk} = \sum_{j,n=1}^{3} \left( \left( U_L^l \right)^{\dagger} \cdot U_\nu \right)_{ij} M_{jn}^k \left( U_\nu^{\dagger} \cdot U_R^{l^M} \right)_{nm} ,$
$\equiv \sum_{j,n=1}^{3} \left( U_{\rm PMNS}^{\dagger} \right)_{ij} M_{jn}^{k} \left( U_{\rm PMNS}^{l^{M}} \right)_{nm} ,$
$= \left( U_{\rm PMNS}^{\dagger} \cdot M^k \cdot U_{\rm PMNS}^{l^{\prime\prime\prime}} \right)_{im} ,$
$\mathcal{U}_{im}^{Rk} = \sum_{j,n=1}^{3} \left( \left( U_R^l \right)^{\dagger} \cdot U_{\nu} \right)_{ij} M_{jn}^{\primek} \left( U_{\nu}^{\dagger} \cdot U_L^{l^M} \right)_{nm} ,$
$\equiv \sum_{j,n=1}^{3} \left( U_{\rm PMNS}^{\prime \dagger} \right)_{ij} M_{jn}^{\prime k} \left( U_{\rm PMNS}^{\prime l^M} \right)_{nm} ,$
$= \left( U_{\rm PMNS}^{\prime \prime} \cdot M^{\prime \kappa} \cdot U_{\rm PMNS}^{\prime \prime m} \right)_{im} .$
$U_{\nu} = U_{CW}^{\dagger} = \frac{1}{\sqrt{3}} \begin{pmatrix} 1 & 1 & 1\\ 1 & \omega^2 & \omega\\ 1 & \omega & \omega^2 \end{pmatrix}$
$\omega = e^{2\pi i/3}$

#### • $M^k$ is given by

TABLE I. Matrix elements for  $M^k(k = 0, 1, 2, 3)$ .

$M_{jn}^k$	Value	
$M_{12}^0, M_{13}^0, M_{21}^0, M_{23}^0, M_{31}^0, M_{32}^0$	0	
$M_{11}^0, M_{22}^0, M_{33}^0$	$g_{0S}$	
$M_{11}^1, M_{11}^2, M_{11}^3$	$\frac{2}{3}$ Re $(g_{1S})$	
$M_{22}^1, M_{22}^2, M_{22}^3$	$\frac{2}{3}$ Re $(\omega^* g_{1S})$	Contains information about A4 symmetry
$M^1_{33}, M^2_{33}, M^3_{33}$	$\frac{2}{3}$ Re $(\omega g_{1S})$	
$M_{12}^1, M_{21}^1$	$\frac{2}{3}$ Re $(\omega g_{1S})$	
$M_{12}^2, M_{21}^3$	$\frac{1}{3}\left(g_{1S}+\omega g_{1S}^*\right)$	
$M_{12}^3, M_{21}^2$	$\frac{1}{3}\left(g_{1S}^* + \omega^* g_{1S}\right)$	
$M_{13}^1, M_{31}^1$	$\frac{2}{3}$ Re $(\omega^* g_{1S})$	in the
$M_{13}^2, M_{31}^3$	$\frac{1}{3}\left(g_{1S}+\omega^*g_{1S}^*\right)$	neutrino sector
$M_{13}^3, M_{31}^2$	$\frac{1}{3}\left(g_{1S}^* + \omega g_{1S}\right)$	
$M_{23}^1, M_{32}^1$	$\frac{2}{3}$ Re $(g_{1S})$	
$M_{23}^2, M_{32}^3$	$\frac{2\omega^*}{3}$ Re $(g_{1S})$	
$M_{23}^3, M_{32}^2$	$\frac{2\omega}{3}$ Re $(g_{1S})$	

•  $M'^k$  can be obtained from  $M^k$  with  $g_{0S} \rightarrow g'_{0S}$ and  $g_{1S} \rightarrow g'_{1S}$ 



• Standard Parameterization

$$U_{\rm PMNS} = \begin{pmatrix} c_{12}c_{13} & s_{12}c_{13} & s_{13}e^{-i\delta} \\ -s_{12}c_{23} - c_{12}s_{23}s_{13}e^{i\delta} & c_{12}c_{23} - s_{12}s_{23}s_{13}e^{i\delta} & s_{23}c_{13} \\ s_{12}s_{23} - c_{12}c_{23}s_{13}e^{i\delta} & -c_{12}s_{23} - s_{12}c_{23}s_{13}e^{i\delta} & c_{23}c_{13} \end{pmatrix} \cdot P \qquad P = \begin{pmatrix} 1 & 0 & 0 \\ 0 & e^{i\alpha_{21}/2} & 0 \\ 0 & 0 & e^{i\alpha_{31}/2} \end{pmatrix}$$

Mixing Parameters	Normal Hierarchy	Inverted Hierarchy
$\sin^2 \theta_{12}$	$0.308 \pm 0.017$	$0.308 \pm 0.017$
$\sin^2 heta_{23}$	$0.437^{+0.033}_{-0.023}$	$0.455_{-0.031}^{+0.139}$
$\sin^2  heta_{13}$	$0.0234^{+0.0020}_{-0.0019}$	$0.024_{-0.0022}^{+0.0019}$
$\delta/\pi$	$1.39^{+0.38}_{-0.27}$	$1.31_{-0.33}^{+0.29}$
$\delta m^2 = m_2^2 - m_1^2$	$(7.54^{+0.26}_{-0.22}) \times 10^{-5} \text{eV}^2$	$(7.54^{+0.26}_{-0.22}) \times 10^{-5} \mathrm{eV}^2$
$\left \Delta m^2 =  m_3^2 - (m_1^2 + m_2^2)/2 \right $	$ (2.43 \pm 0.06) \times 10^{-3} \mathrm{eV}^2 $	$(2.38 \pm 0.06) \times 10^{-3} \mathrm{eV}^2$

Capozzi, Fogli, Lisi, Marrone, Montanino, and Palazzo, PRD 89, 093018 (2014) [arXiv:1312.2878]

$$U_{\rm PMNS}^{\rm NH} = \begin{pmatrix} 0.8221 & 0.5484 & -0.0518 + 0.1439i \\ -0.3879 + 0.07915i & 0.6432 + 0.0528i & 0.6533 \\ 0.3992 + 0.08984i & -0.5283 + 0.05993i & 0.7415 \end{pmatrix}$$
$$U_{\rm PMNS}^{\rm IH} = \begin{pmatrix} 0.8218 & 0.5483 & -0.08708 + 0.1281i \\ -0.3608 + 0.0719i & 0.6467 + 0.04796i & 0.6664 \\ 0.4278 + 0.07869i & -0.5254 + 0.0525i & 0.7293 \end{pmatrix}$$

## Calculations

- Early calculation of  $\mu \rightarrow e\gamma$  and  $\tau \rightarrow \mu\gamma$  in the minimal model was done back in 2008 [PQ Hung, PLB 659 (2008)].
- Here we perform an updated analysis in the extended model with A<sub>4</sub> symmetry.
- Current Limit (April, 2013)  $B(\mu^+ \rightarrow e^+ \gamma) \leq 5.7 \times 10^{-13} (90\% \text{CL})$
- MEG-II Short Term Upgrade Engineering Run - End of 2015 Physics Run - 2016
- Expected upper limit 4×10<sup>-14</sup>
   an order of magnitude improvement!



Figure 1: The MEG detector.

## The Invariant Amplitude

$$\begin{split} M(l_{i}^{-}(p) \rightarrow l_{j}^{-}(p')\gamma(q)) &= \bar{u}_{j}(p')i\sigma^{\mu\nu}q_{\nu}[C_{L}^{ij}L + C_{R}^{ij}R]u_{i}(p)\epsilon_{\mu}^{*}(q) \\ C_{L}^{ij} &= +\frac{e}{16\pi^{2}}\sum_{k=0}^{3}\sum_{m=1}^{3} \left\{ \frac{1}{m_{l_{m}^{k}}^{2}} \left[ m_{i}\mathcal{U}_{jm}^{Rk} \left(\mathcal{U}_{im}^{Rk}\right)^{*} + m_{j}\mathcal{U}_{jm}^{Lk} \left(\mathcal{U}_{im}^{Lk}\right)^{*} \right] \mathcal{I}\left(\frac{m_{\phi_{Sk}}^{2}}{m_{l_{m}^{M}}^{2}}\right) \\ &+ \frac{1}{m_{l_{m}^{k}}}\mathcal{U}_{jm}^{Rk} \left(\mathcal{U}_{im}^{Lk}\right)^{*} \mathcal{J}\left(\frac{m_{\phi_{Sk}}^{2}}{m_{l_{m}^{M}}^{2}}\right) \right\} , \\ C_{R}^{ij} &= +\frac{e}{16\pi^{2}}\sum_{k=0}^{3}\sum_{m=1}^{3} \left\{ \frac{1}{m_{l_{m}^{k}}^{2}} \left[ m_{i}\mathcal{U}_{jm}^{Lk} \left(\mathcal{U}_{im}^{Lk}\right)^{*} + m_{j}\mathcal{U}_{jm}^{Rk} \left(\mathcal{U}_{im}^{Rk}\right)^{*} \right] \mathcal{I}\left(\frac{m_{\phi_{Sk}}^{2}}{m_{l_{m}^{M}}^{2}}\right) \\ &+ \frac{1}{m_{l_{m}^{M}}}\mathcal{U}_{jm}^{Lk} \left(\mathcal{U}_{im}^{Rk}\right)^{*} \mathcal{J}\left(\frac{m_{\phi_{Sk}}^{2}}{m_{l_{m}^{M}}^{2}}\right) \right\} \\ \bullet \quad T \text{ and } \mathcal{J} (\text{Ignoring m, and m}) \\ \mathcal{I}(r) &= \frac{1}{12(1-r)^{4}} \left[ -6r^{2}\log r + r(2r^{2} + 3r - 6) + 1 \right] , \\ \bullet \quad \mathcal{U}^{L} \text{ and } \mathcal{U}^{R} \text{ mix different families of charged lepons with hose of the mirror leptons (sce below)} \\ \end{array}$$

 $l_j$ 

## 3 Observables (1 Stone 3 Birds)

• LFV Radiative Decay Rate

$$\Gamma\left(l_i \to l_j \gamma\right) = \frac{1}{16\pi} m_{l_i}^3 \left(1 - \frac{m_{l_j}^2}{m_{l_i}^2}\right)^3 \left(|C_L^{ij}|^2 + |C_R^{ij}|^2\right)$$

• Anomalous Magnetic Moment

$$\begin{split} \Delta a_{l_{i}} &= \frac{2m_{l_{i}}}{e} \left( \frac{C_{L}^{ii} + C_{R}^{ii}}{2} \right) \\ &= +\frac{1}{16\pi^{2}} \left\{ \sum_{k=0}^{3} \sum_{m=1}^{3} 2 \left( |\mathcal{U}_{im}^{L\,k}|^{2} + |\mathcal{U}_{im}^{R\,k}|^{2} \right) \frac{m_{l_{i}}^{2}}{m_{l_{m}}^{2}} \mathcal{I} \left( \frac{m_{\phi_{Sk}}^{2}}{m_{l_{m}}^{2}} \right) \right. \\ &+ \left. \sum_{k=0}^{3} \sum_{m=1}^{3} \operatorname{Re} \left( \mathcal{U}_{im}^{L\,k} \left( \mathcal{U}_{im}^{R\,k} \right)^{*} \right) \frac{m_{l_{i}}}{m_{l_{m}}^{M}} \mathcal{J} \left( \frac{m_{\phi_{Sk}}^{2}}{m_{l_{m}}^{2}} \right) \right\} \end{split}$$

• Electric Dipole Moment

$$d_{l_{i}} = \frac{i}{2} \left( C_{L}^{ii} - C_{R}^{ii} \right) ,$$
  
=  $+ \frac{e}{16\pi^{2}} \sum_{k=0}^{3} \sum_{m=1}^{3} \frac{1}{m_{l_{m}^{M}}} \operatorname{Im} \left( \mathcal{U}_{im}^{L\,k} \left( \mathcal{U}_{im}^{R\,k} \right)^{*} \right) \mathcal{J} \left( \frac{m_{\phi_{Sk}}^{2}}{m_{l_{m}^{M}}^{2}} \right)$ 

## Numerical Results

9 Assumption

Higgs Singlet Masses 
$$m_{\phi_{Sk}} \sim 10 \,\text{MeV}$$
Mirror Charged Lepton Masses
 $m_{l_m^M} = M_{mirror} + \delta_m$   $M_{mirror} \sim 100 \text{ to } 800 \,\text{GeV}$ 
Yukawa Couplings
 $g_{0S}, g_{1S}, g'_{0S}, g'_{1S}$  are all real!
Mixing Matrices

Scenario 1 :  $U_{PMNS}^{l_M} = U'_{PMNS} = U_{PMNS}^{l_M} = U_{CW}^{l_M}$ 
Scenario 2 :  $U_{PMNS}^{l_M} = U'_{PMNS} = U'_{PMNS}^{l_M} = U_{PMNS}^{l_M}$ 

### Scenario 1/2

#### Branching Ratio Contour on Coupling and Mirror Lepton Mass Space (gos, M<sub>mirror</sub>)



 $g_{1S} = 10^{-2} \cdot g_{0S}$  $g'_{0S} = g_{0S}$  $g'_{1S} = g_{1S}$ 



#### Branching Ratio Contour on Coupling and Mirror Lepton Mass Space (gos, M<sub>mirror</sub>)



 $g_{1S} = 0.5 \cdot g_{0S}$  $g'_{0S} = g_{0S}$  $g'_{1S} = g_{1S}$ 

### Discussions

- In the same mass range of the mirror leptons the LFV process  $\mu \rightarrow e \gamma$  is more sensitive to the couplings by almost 2 orders of magnitudes as compared to  $\Delta a_{\mu}$ .
- As one turns on the A<sub>4</sub> triplet couplings, the contours of  $\text{Log}_{10}(\mu \rightarrow e \gamma)$  are shifting toward to the left, indicating the role of the triplet singlets becomes more relevant and thus the constraints on the parameter space becomes more stringent from the current MEG limit.
- The sensitivity of the couplings in the  $B(\mu \rightarrow e \gamma)$  has been weakened by one to two orders of magnitudes for scenario 2 as compared to scenario 1. However, this sensitivity is not present for  $\Delta a_{\mu}$ .
- As one slowly turns on the A<sub>4</sub> triplet couplings  $g_{1S} = 0$  to  $10^{-1}g_{0S}$ , the red contours of  $Log_{10}(\mu \rightarrow e \gamma)$  of scenario 1 remains the same when comparing NH versus IH, while the blue contours of scenario 2 move toward to the left. This indicates noticeable differences between NH and IH of neutrino masses for scenario 2. However, for  $g_{1S} > 0.5g_{0S}$ , these differences disappear! There features are not there for  $\Delta a_{\mu}$ !
- Due to the smallness of the couplings, decay length of the mirror leptons which depends on the product of the couplings and the mixing parameters will probably decay outside the beam pipe, which may lead to displaced vertex at the collider.

## Summary

- Updated analysis on  $\mu \rightarrow e\gamma$  and  $\Delta a_{\mu}$  in non-sterile EW-scale  $\nu_R$ model with A<sub>4</sub> symmetry (necessarily broken in charged lepton sector) were presented. It links LFV processes with  $U_{PMNS}$  in the neutrino sector which is quite distinct from many other models.
- Current MEG limit on  $B(\mu \rightarrow e\gamma)$  imposes constraints on the mirror lepton masses and Yukawa couplings. Projected limit will put even more interesting constraints on the model.
- Predictions of  $B(\mu \rightarrow e\gamma)$  in the extended model with  $A_4$ symmetry are slightly sensitive to the neutrino mass hierarchy in scenarios 2 but not scenario 1. However,  $\Delta a_{\mu}$  is not sensitive to the mass hierarchies.
- Regions allowed by  $\Delta a_{\mu}$  excluded by current limit of  $B(\mu \rightarrow e\gamma)!$
- Work in progress.
   μe conversion, μ→eee
   h→τμ, τe versus τ→μγ, eγ

# Thank You