

# Distinguishing WIMP-nucleon interactions with directional dark matter experiments

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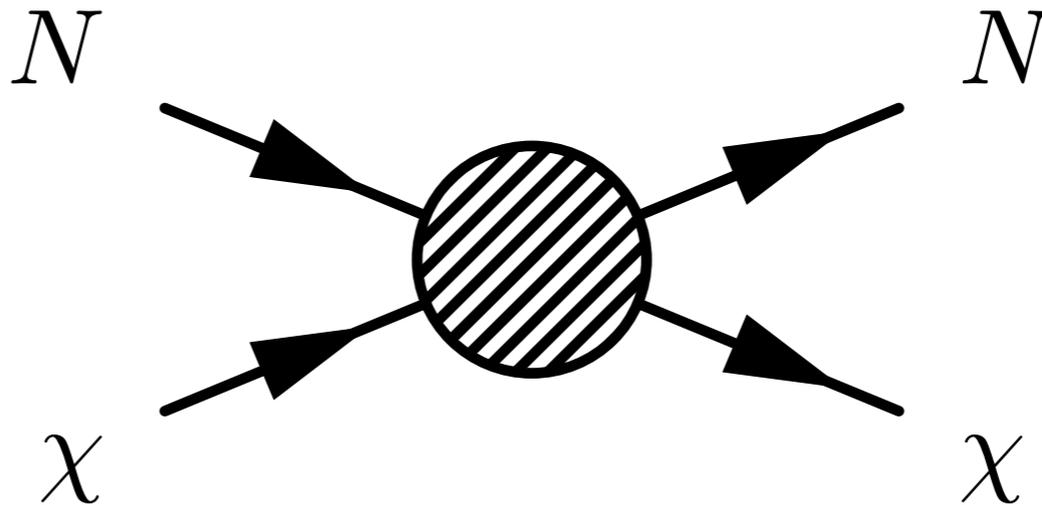
Based on [arXiv:1505.07406](https://arxiv.org/abs/1505.07406)

# Possible WIMP-nucleon operators

Direct detection:

$$m_\chi \gtrsim 1 \text{ GeV}$$

$$v \sim 10^{-3}$$



$$q \lesssim 100 \text{ MeV} \sim (2 \text{ fm})^{-1}$$

Relevant non-relativistic (NR) degrees of freedom:

$$\vec{S}_\chi \quad \vec{S}_N \quad \frac{\vec{q}}{2m_N} \quad \vec{v}_\perp = \vec{v} + \frac{\vec{q}}{2\mu_{\chi N}}$$

# Non-relativistic effective field theory (NREFT)

Require Hermitian, Galilean invariant and time-translation invariant combinations:

SI  $\rightarrow$   $\mathcal{O}_1 = 1$

SD  $\rightarrow$   $\mathcal{O}_4 = \vec{S}_\chi \cdot \vec{S}_N$

[1008.1591, 1203.3542, 1308.6288, 1505.03117]

# Non-relativistic effective field theory (NREFT)

Require Hermitian, Galilean invariant and time-translation invariant combinations:

SI  $\rightarrow$   $\mathcal{O}_1 = 1$

$\mathcal{O}_3 = i\vec{S}_N \cdot (\vec{q} \times \vec{v}^\perp)/m_N$

SD  $\rightarrow$   $\mathcal{O}_4 = \vec{S}_\chi \cdot \vec{S}_N$

$\mathcal{O}_5 = i\vec{S}_\chi \cdot (\vec{q} \times \vec{v}^\perp)/m_N$

$\mathcal{O}_6 = (\vec{S}_\chi \cdot \vec{q})(\vec{S}_N \cdot \vec{q})/m_N^2$

$\mathcal{O}_7 = \vec{S}_N \cdot \vec{v}^\perp$

$\mathcal{O}_8 = \vec{S}_\chi \cdot \vec{v}^\perp$

$\mathcal{O}_9 = i\vec{S}_\chi \cdot (\vec{S}_N \times \vec{q})/m_N$

$\mathcal{O}_{10} = i\vec{S}_N \cdot \vec{q}/m_N$

$\mathcal{O}_{11} = i\vec{S}_\chi \cdot \vec{q}/m_N$

$$\mathcal{O}_{12} = \vec{S}_\chi \cdot (\vec{S}_N \times \vec{v}^\perp)$$

$$\mathcal{O}_{13} = i(\vec{S}_\chi \cdot \vec{v}^\perp)(\vec{S}_N \cdot \vec{q})/m_N$$

$$\mathcal{O}_{14} = i(\vec{S}_\chi \cdot \vec{q})(\vec{S}_N \cdot \vec{v}^\perp)/m_N$$

$$\mathcal{O}_{15} = -(\vec{S}_\chi \cdot \vec{q})((\vec{S}_N \times \vec{v}^\perp) \cdot \vec{q})/m_N^2$$

$\vdots$

[1008.1591, 1203.3542, 1308.6288, 1505.03117]

# Calculating the cross section

'Dictionaries' are available which allow us to translate from relativistic interactions to NREFT operators:

[e.g. 1211.2818, 1307.5955, 1505.03117]

$$\text{E.g. } \bar{\chi}\gamma^\mu\chi\bar{N}\gamma_\mu\gamma^5N \longrightarrow 8m_N(m_N\mathcal{O}_9 - m_\chi\mathcal{O}_7)$$

Then calculating the scattering cross section is straightforward:

$$\frac{d\sigma_i}{dE_R} = \frac{1}{32\pi} \frac{m_A}{m_\chi^2 m_N^2} \frac{1}{v^2} \sum_{N,N'=p,n} c_i^N c_i^{N'} F_i^{(N,N')}(v_\perp^2, q^2)$$

Nuclear response functions:  $F_i(v_\perp^2, q^2)$

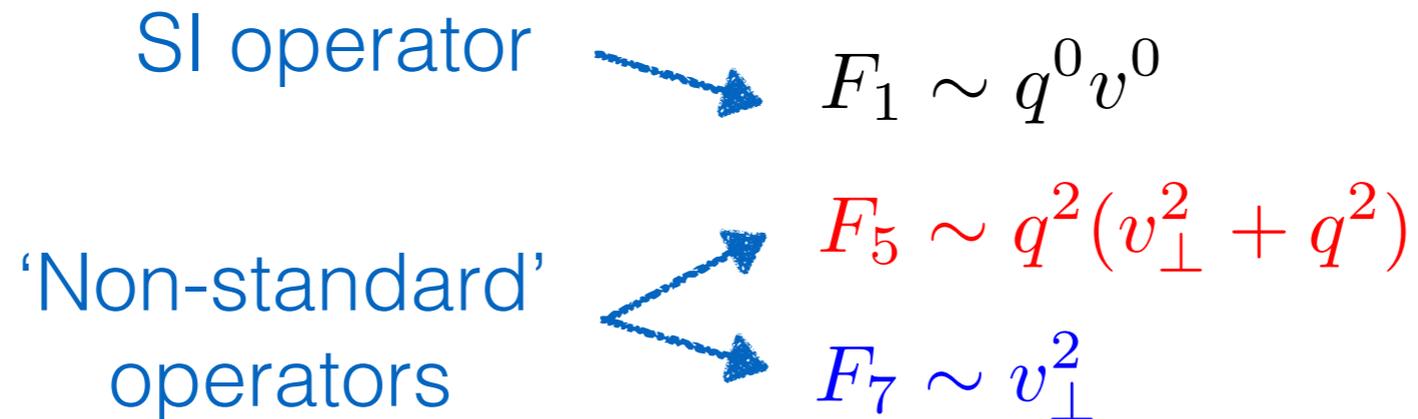
*So how can we distinguish these different cross sections?*

# Distinguishing operators: approaches

- *Materials signal* - compare rates obtained in different experiments [[1405.2637](#), [1406.0524](#), [1504.06554](#), [1506.04454](#)]
  - ↳ May require a large number of experiments
- *Annual modulation* - due to different  $v$ -dependence annual modulation rate and phase can be different [[1504.06772](#)]
  - ↳ Annual modulation is a small effect
- *Energy spectrum* - look for an energy spectrum which differs from the standard SI case in a single experiment [[1503.03379](#)]

# Distinguishing operators: Energy-only

Consider three different operators:  $\mathcal{O}_1$ ,  $\mathcal{O}_5$ ,  $\mathcal{O}_7$



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Generate mock data assuming either  $\mathcal{O}_5$  or  $\mathcal{O}_7$ .

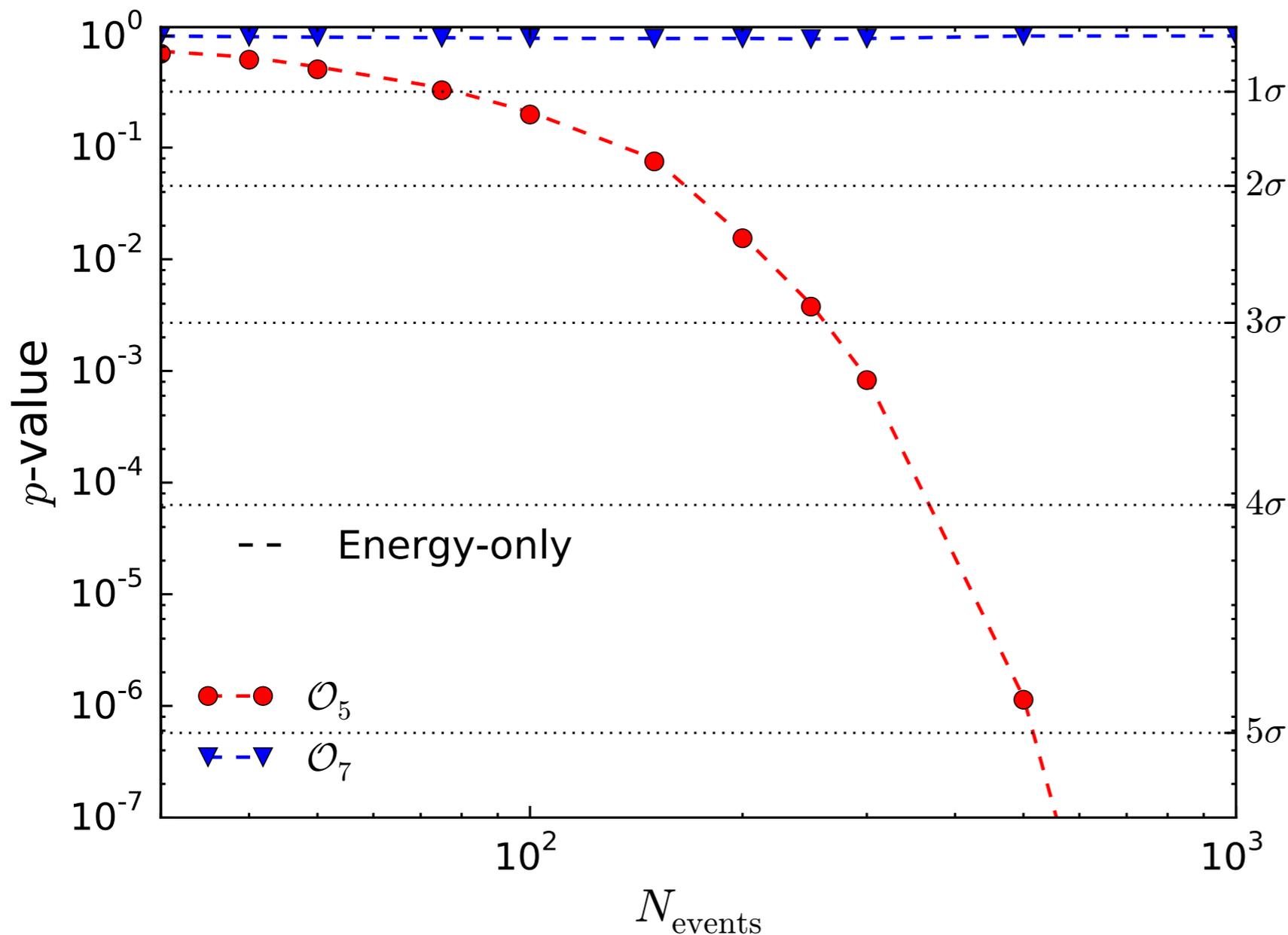
Assume the data is a mixture of events due to  $\mathcal{O}_1$  and the 'non-standard' operator (either  $\mathcal{O}_5$  or  $\mathcal{O}_7$ ).

Fit values of  $m_{\chi}$  and  $A$ , fraction of events due to 'non-standard' interactions.

*With what significance can we reject the SI-only scenario?*

# Distinguishing operators: Energy-only

*With what significance can we reject 'standard' SI/SD interactions in 95% of experiments?*



'Perfect' CF<sub>4</sub> detector

$$E_R \in [20, 50] \text{ keV}$$

Input WIMP mass:

$$m_\chi = 50 \text{ GeV}$$

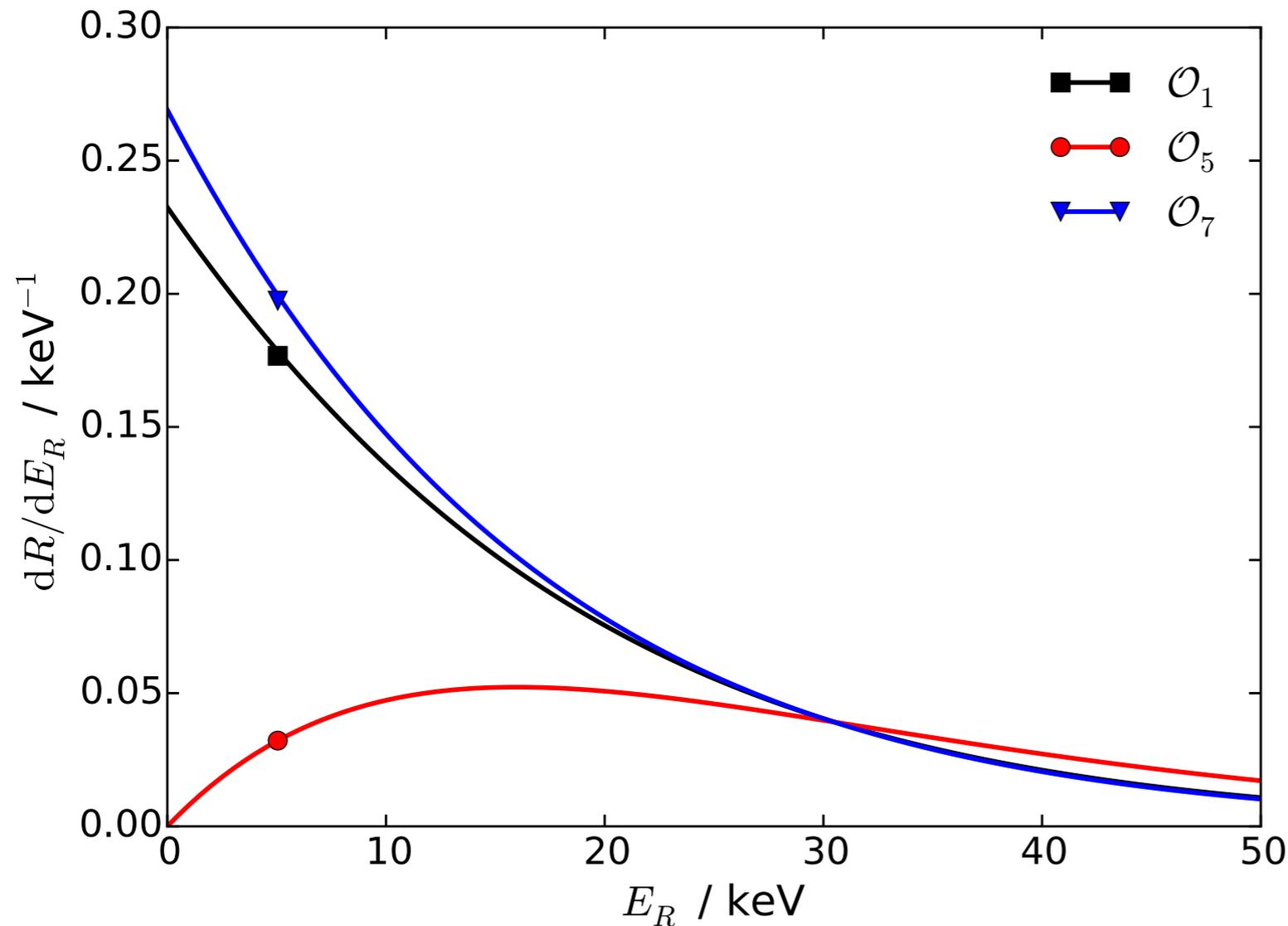
SHM velocity distribution

$$F_1 \sim q^0 v^0$$

$$F_5 \sim q^2 (v_\perp^2 + q^2)$$

$$F_7 \sim v_\perp^2$$

# Comparing energy spectra



$$F_1 \sim q^0 v^0$$

$$F_5 \sim q^2 (v_{\perp}^2 + q^2)$$

$$F_7 \sim v_{\perp}^2$$

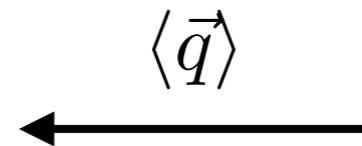
Energy spectrum differences between  $\mathcal{O}_1$  and  $\mathcal{O}_7$  are smoothed out once we integrate over (smooth) DM velocity distribution.

*True of any operators whose cross-sections differ only by  $v_{\perp}^2$ .*

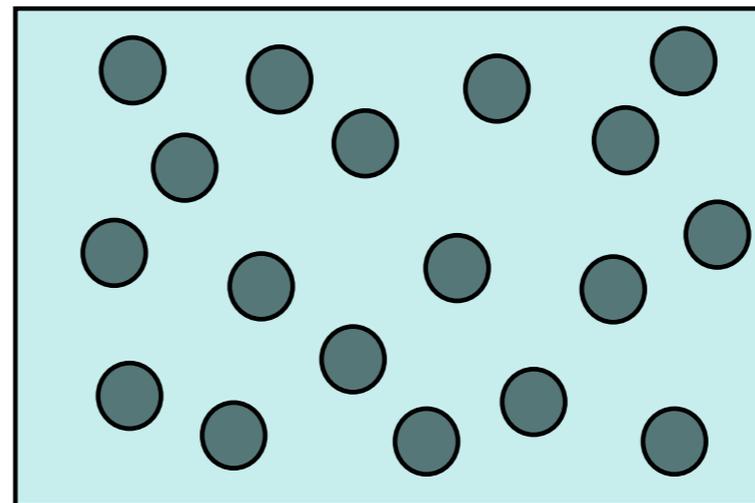
# Directional detection

Different  $v$ -dependence could impact *directional* signal.

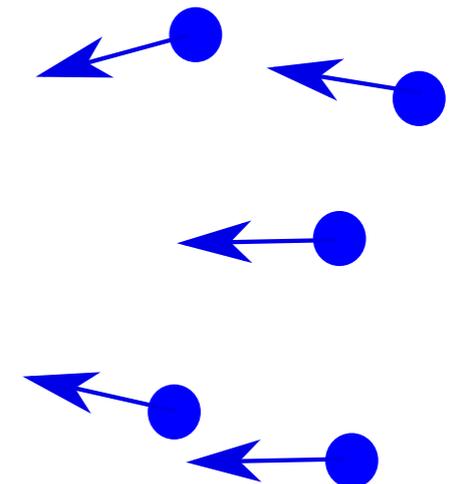
Mean recoil direction is parallel to incoming WIMP direction (due to Earth's motion).



Detector



$$\langle \vec{v} \rangle \sim -\vec{v}_e$$

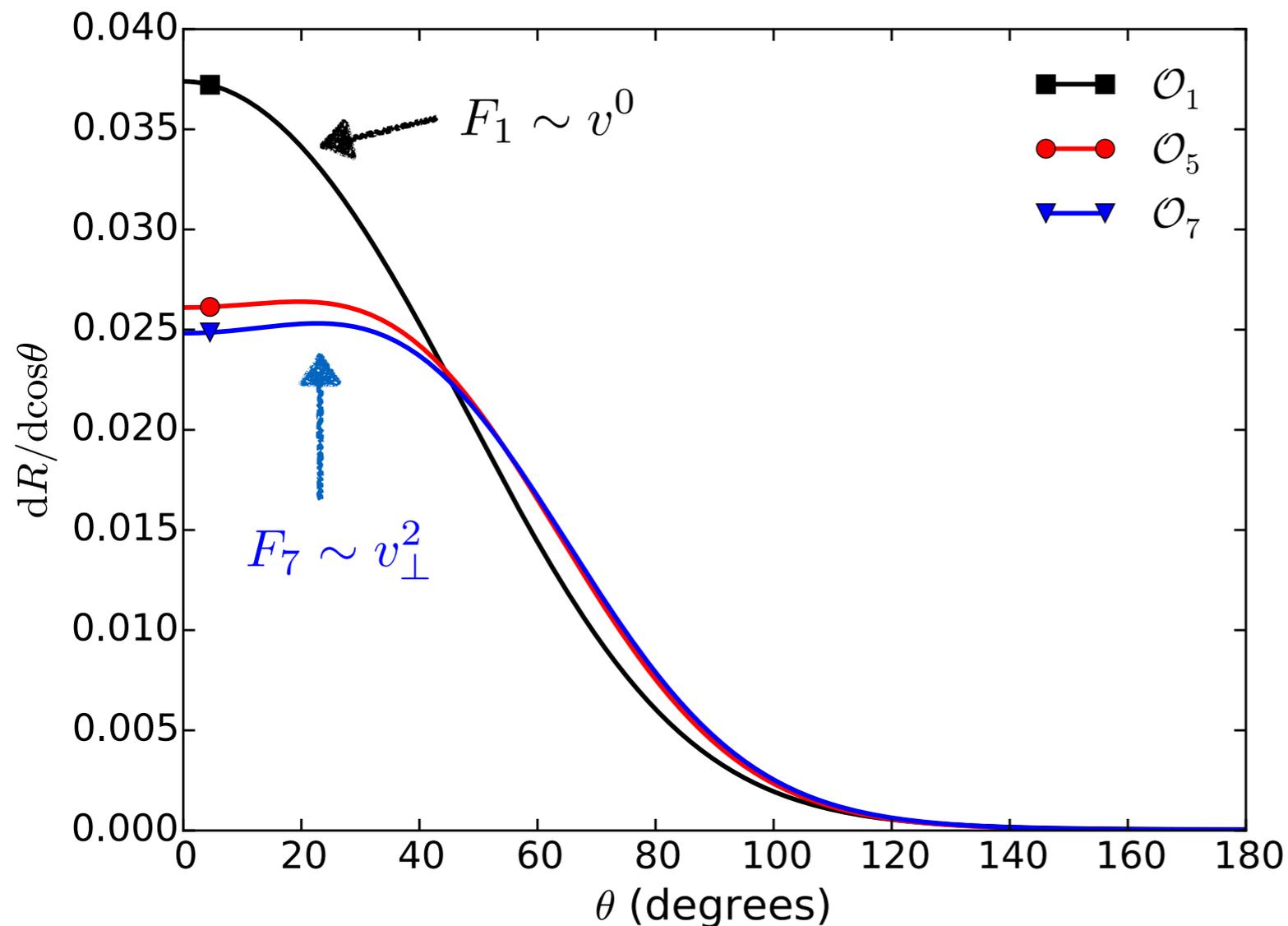


Convolve cross section with velocity distribution to obtain directional spectrum, as a function of  $\theta$ , the angle between the recoil and the peak direction.

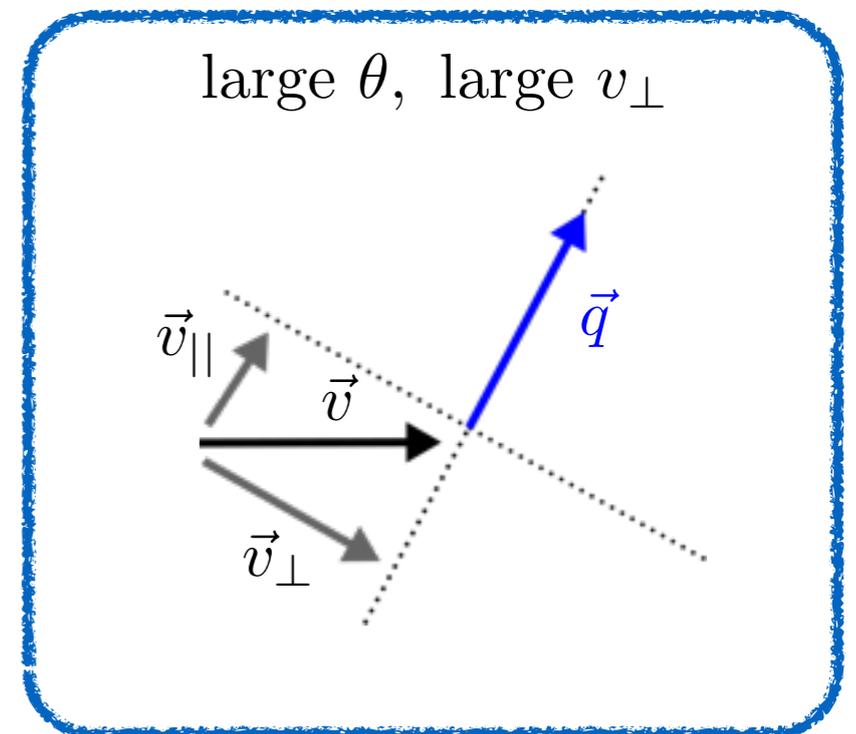
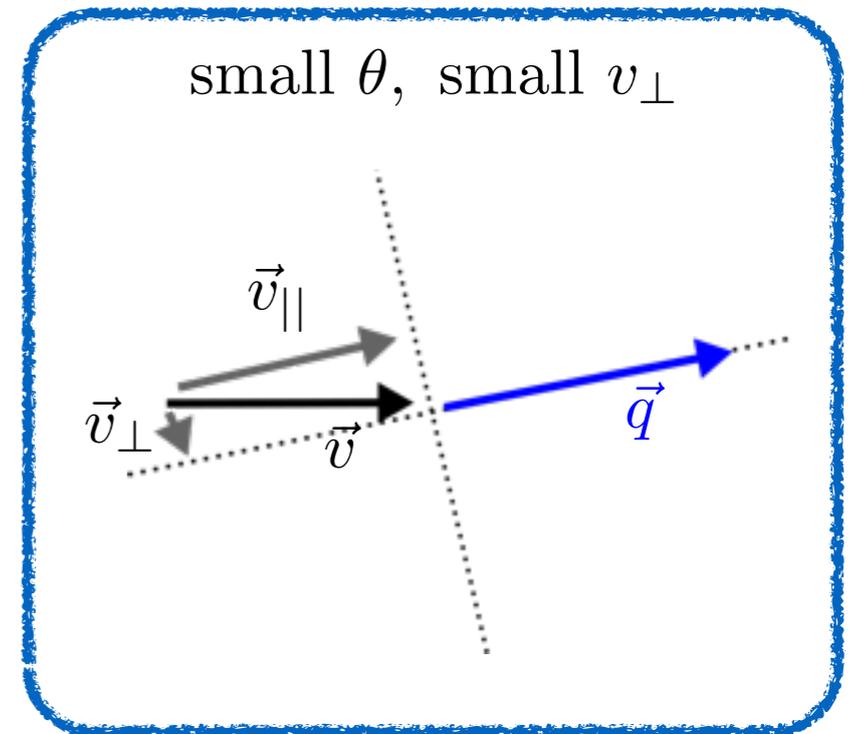
*So, what does the directional spectrum look like?*

# Directional spectra of NREFT operators

Total distribution of recoils as a function of  $\theta$ :

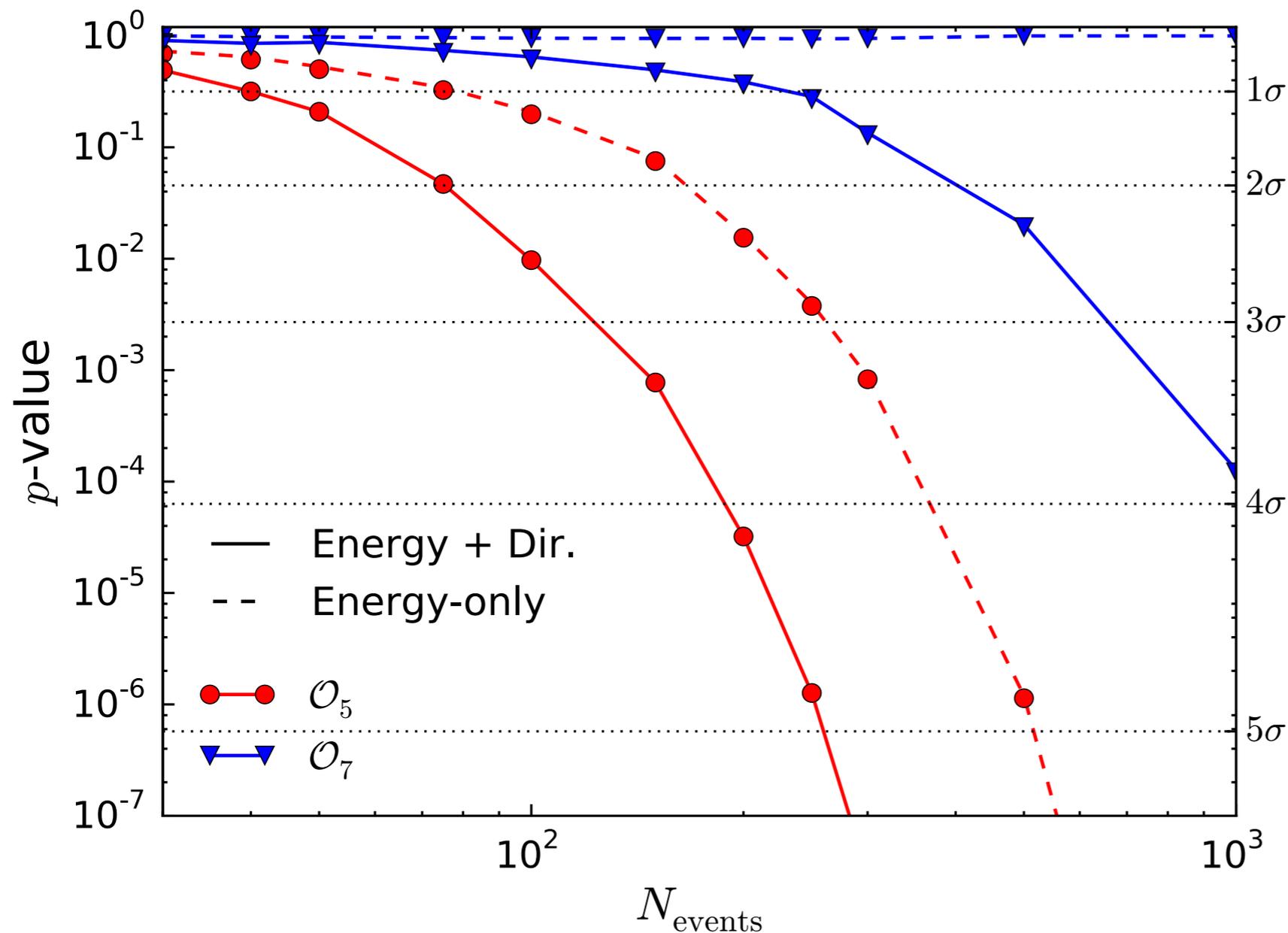


Spectra of all operators given in [1505.07406, 1505.06441].



# Distinguishing operators: Energy + Directionality

With what significance can we reject 'standard' SI/SD interactions in 95% of experiments?



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Input WIMP mass:

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SHM velocity distribution

$$F_1 \sim q^0 v^0$$

$$F_5 \sim q^2 (v_\perp^2 + q^2)$$

$$F_7 \sim v_\perp^2$$

## Summary: a final example

NREFT framework allows us to compare the different possible direct detection signals.

Some operators can be distinguished in a single experiment from their energy spectra alone (e.g. if the form factor goes as  $F \sim q^n$ )

*But*, this is not true for all operators. Consider:

$$\begin{aligned}\mathcal{L}_1 = \bar{\chi}\chi\bar{N}N &\longrightarrow F \sim v^0 \\ \mathcal{L}_6 = \bar{\chi}\gamma^\mu\gamma^5\chi\bar{N}\gamma_\mu N &\longrightarrow F \sim v_\perp^2\end{aligned}$$

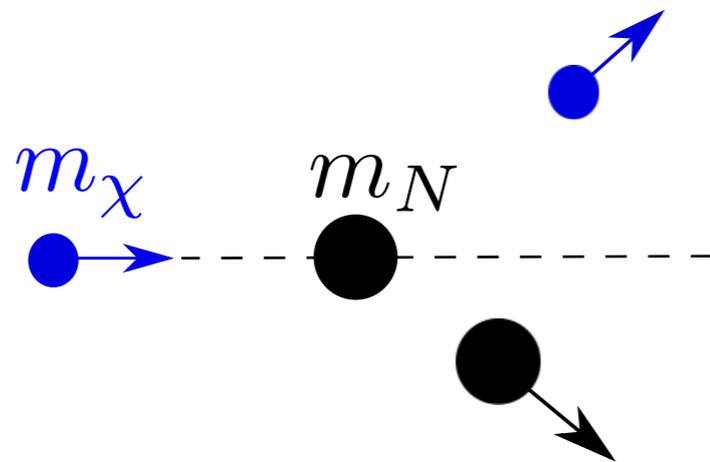
These operators cannot be distinguished in a single non-directional experiment.

*Directional detection will be powerful and crucial tool for determining how DM interacts with the Standard Model!*

# Backup Slides

# The Directional Spectrum

Recoil distribution for WIMP-nucleus recoils in direction  $\hat{q}$  with fixed WIMP speed  $\vec{v}$  :



$$\mu_{\chi N} = \frac{m_{\chi} m_N}{m_{\chi} + m_N}$$

$$v_{\min} = \sqrt{\frac{m_N E_R}{2\mu_{\chi N}^2}}$$

$$\frac{dR}{dE_R d\Omega_q} = \frac{\rho_0 v}{m_{\chi}} \frac{\langle |\mathcal{M}|^2 \rangle}{32\pi m_N^2 m_{\chi}^2 v^2} \frac{v \delta(\vec{v} \cdot \hat{q} - v_{\min})}{2\pi}$$

WIMP flux

Cross section

Kinematics

For standard SI and SD interactions:  $\langle |\mathcal{M}|^2 \rangle \sim v^0 q^0$

# NREFT event rate

The matrix element for operator  $i$  can now be written as:

$$\langle |\mathcal{M}_i|^2 \rangle = |\langle c_i \mathcal{O}_i \rangle_{\text{nucleus}}|^2 = c_i^2 F_{i,i}(v_{\perp}^2, q^2)$$

[Assuming for now:  $c^p = c^n$ ]

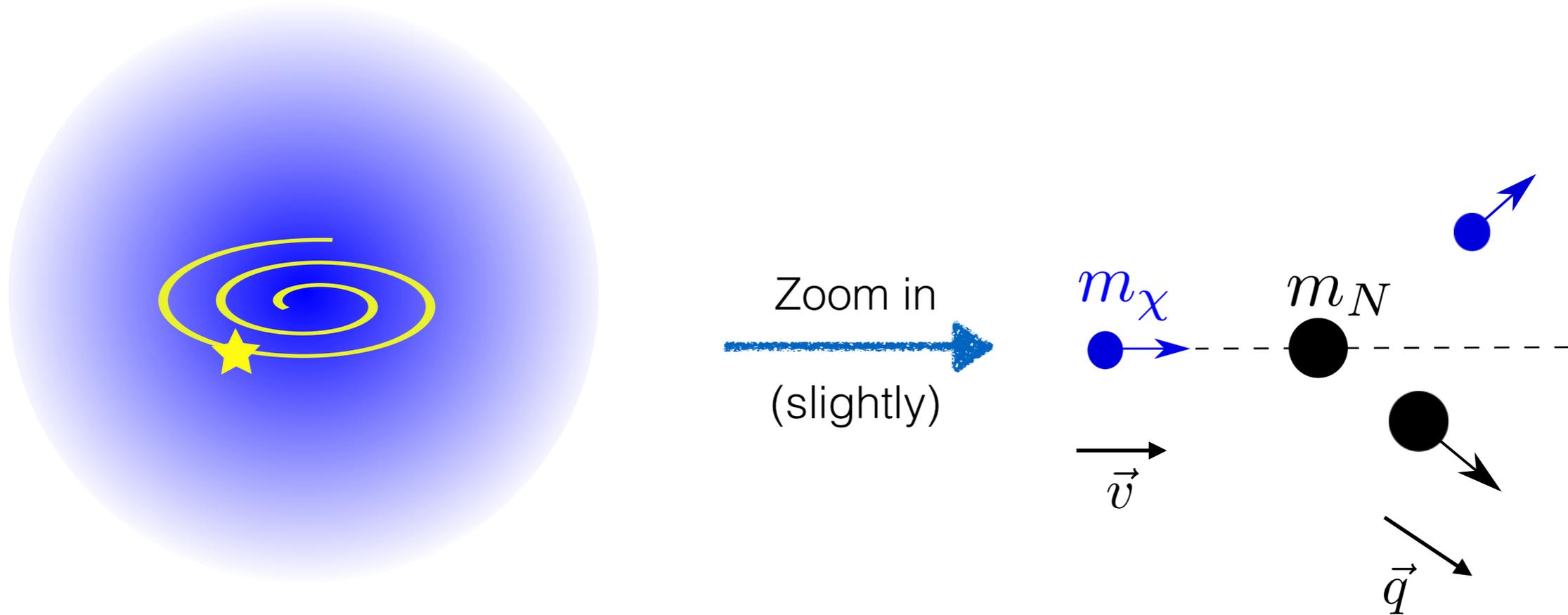
The nuclear response functions  $F_{i,i}(v_{\perp}^2, q^2)$  are the expectation values of the operators summed over all nucleons in the nucleus.

They are proportional to  $(v_{\perp})^0$  or  $(v_{\perp})^2$ .

$$\frac{dR_i}{dE_R d\Omega_q} = \frac{\rho_0}{64\pi^2 m_N^2 m_{\chi}^3} c_i^2 \int_{\mathbb{R}^3} F_{i,i}(v_{\perp}^2, q^2) f(\vec{v}) \delta(\vec{v} \cdot \hat{q} - v_{\min}) d^3\vec{v}$$

Framework previously applied to non-directional direct detection and solar capture [[1211.2818](#), [1406.0524](#), [1503.03379](#), [1503.04109](#) and [others](#)].

# Direct detection

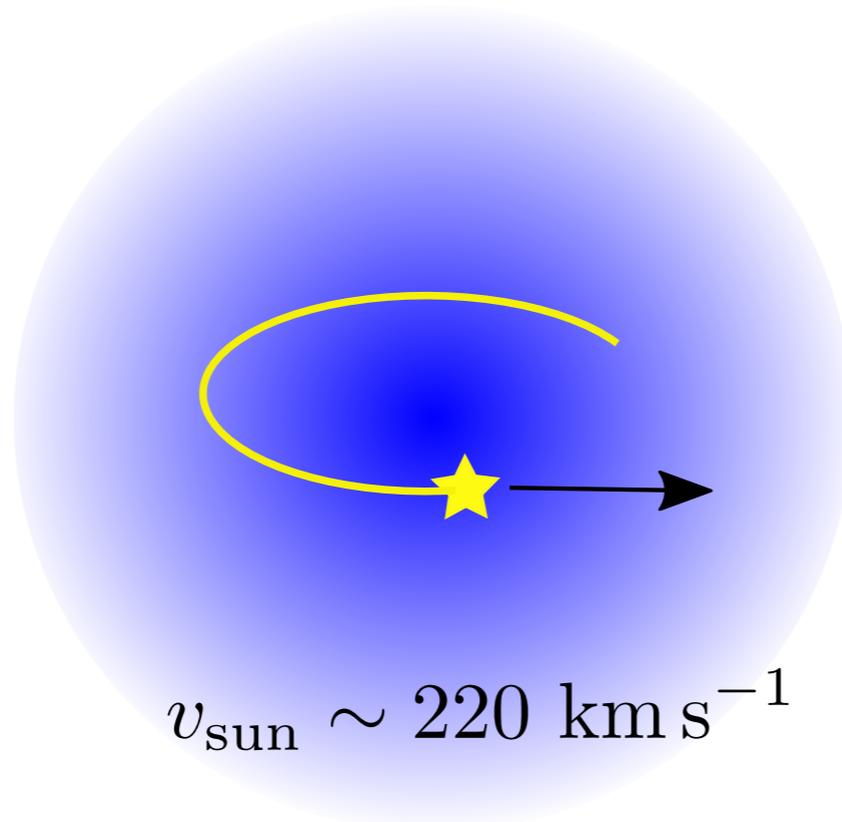


Look for interactions of DM particles from the halo with nuclei in a detector - measure **energy** of the recoiling nucleus.

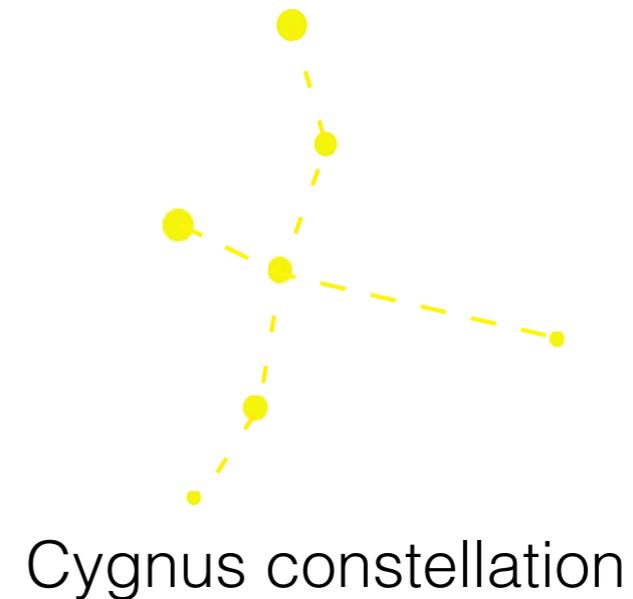
Expect lots of low energy backgrounds  $\rightarrow$  background discrimination can be...*problematic*...

# The WIMP Wind

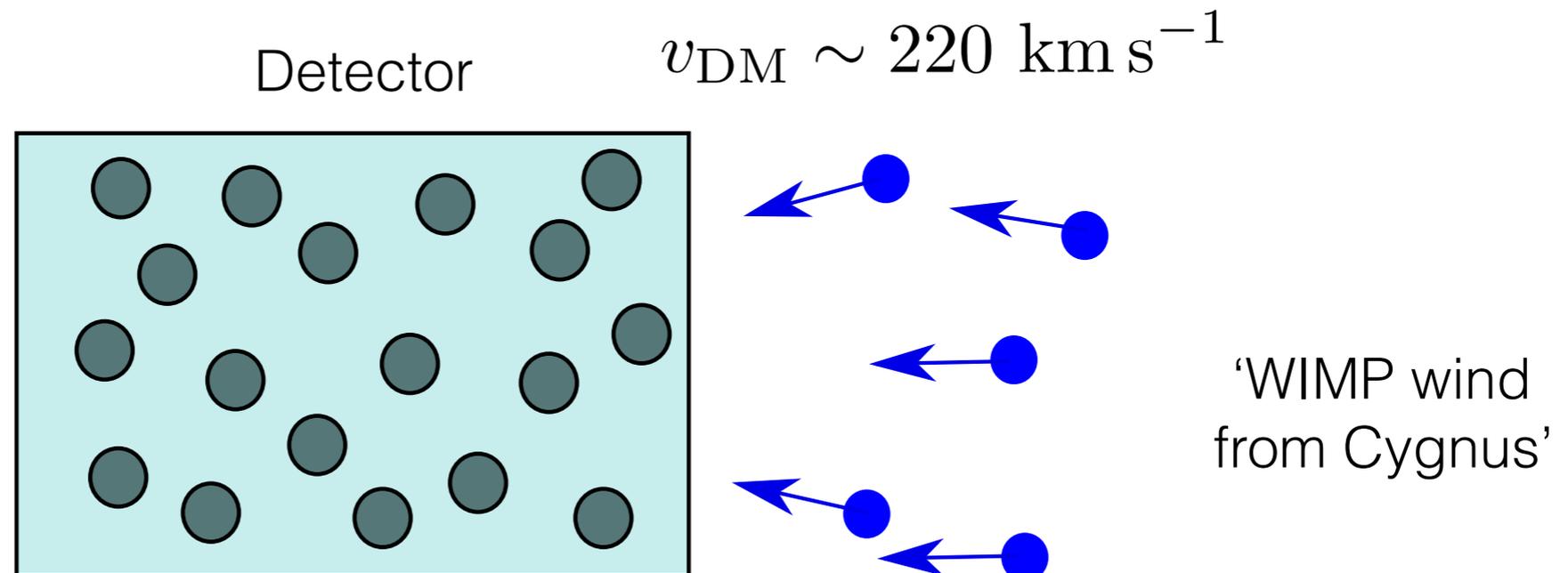
In the halo:



*WIMP*: Weakly Interacting Massive Particle



In the lab:



# Radon Transform

For standard SI/SD, for fixed DM speed:  $\frac{dR}{dE_R d\Omega_q} \propto \delta(\vec{v} \cdot \hat{q} - v_{\min})$

So integrating over all DM speeds:

$$\frac{dR}{dE_R d\Omega_q} \propto \int_{\mathbb{R}^3} f(\vec{v}) \delta(\vec{v} \cdot \hat{q} - v_{\min}) d^3\vec{v} \equiv \hat{f}(v_{\min}, \hat{q})$$

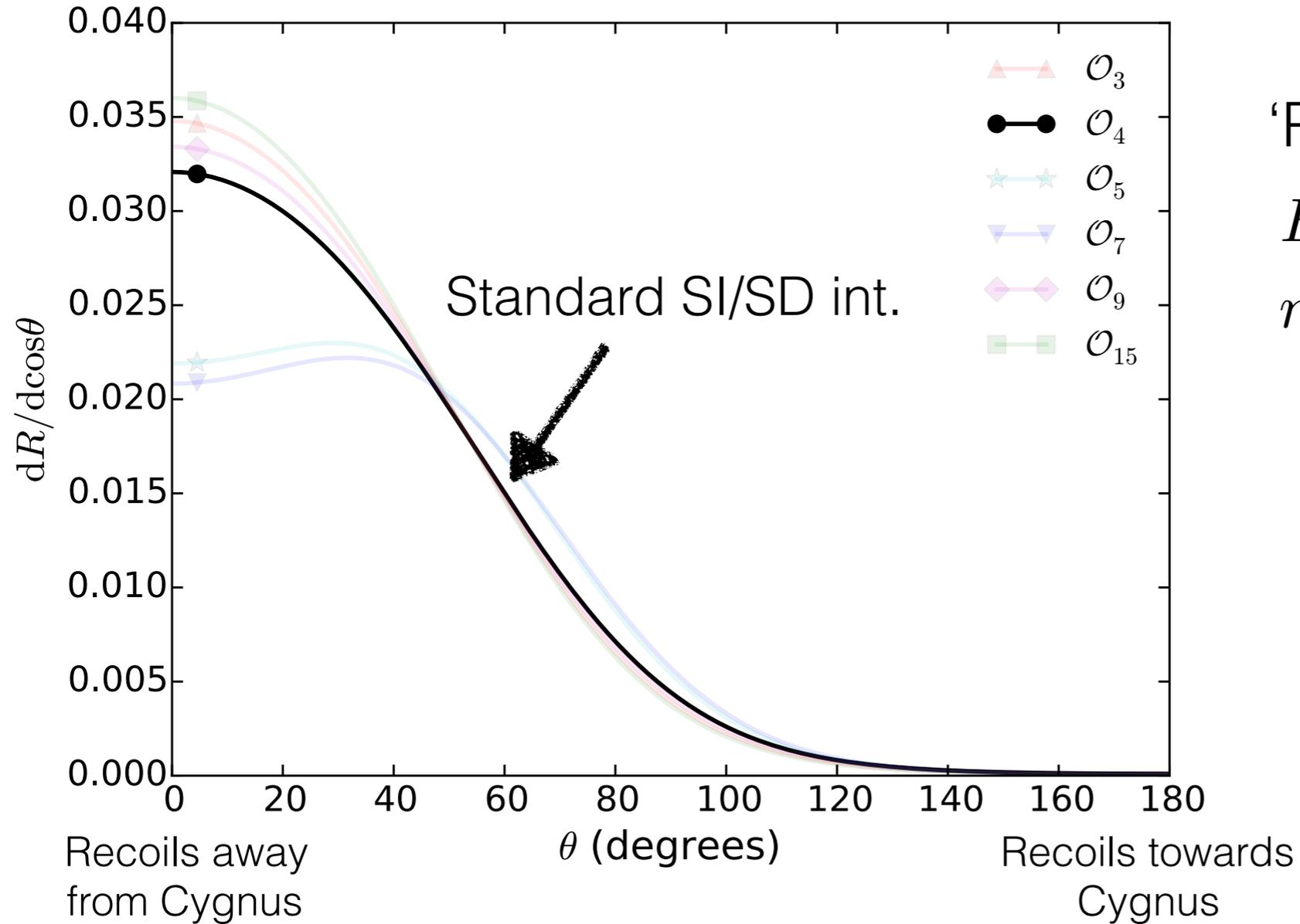
'Radon Transform' (RT) 

For the SHM:

$$f(\vec{v}) = \frac{1}{(2\pi\sigma^2)^{3/2}} \exp\left[-\frac{(\vec{v} - \vec{v}_{\text{lag}})^2}{2\sigma_v^2}\right]$$

$$\hookrightarrow \hat{f}(v_{\min}, \hat{q}) = \frac{1}{\sqrt{2\pi\sigma_v^2}} \exp\left[-\frac{(v_{\min} - \vec{v}_{\text{lag}} \cdot \hat{q})^2}{2\sigma_v^2}\right]$$

# Directional Spectra



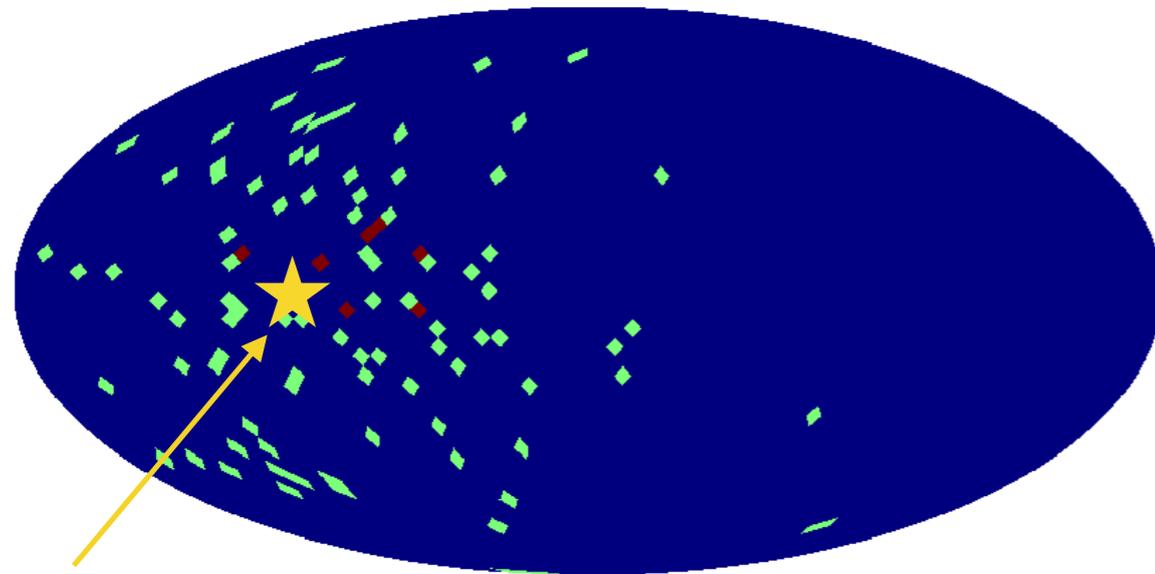
'Perfect'  $\text{CF}_4$  detector

$$E_R \in [20, 50] \text{ keV}$$

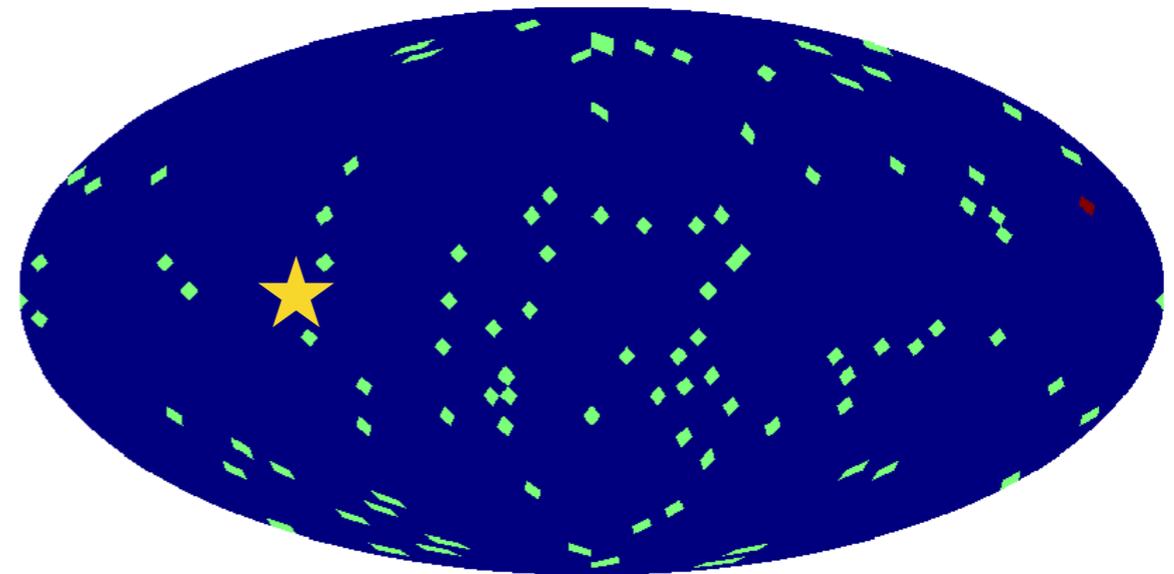
$$m_\chi = 100 \text{ GeV}$$

# The Smoking Gun

Aim to measure the **energy** and **direction** of the recoiling nucleus.



WIMP signal

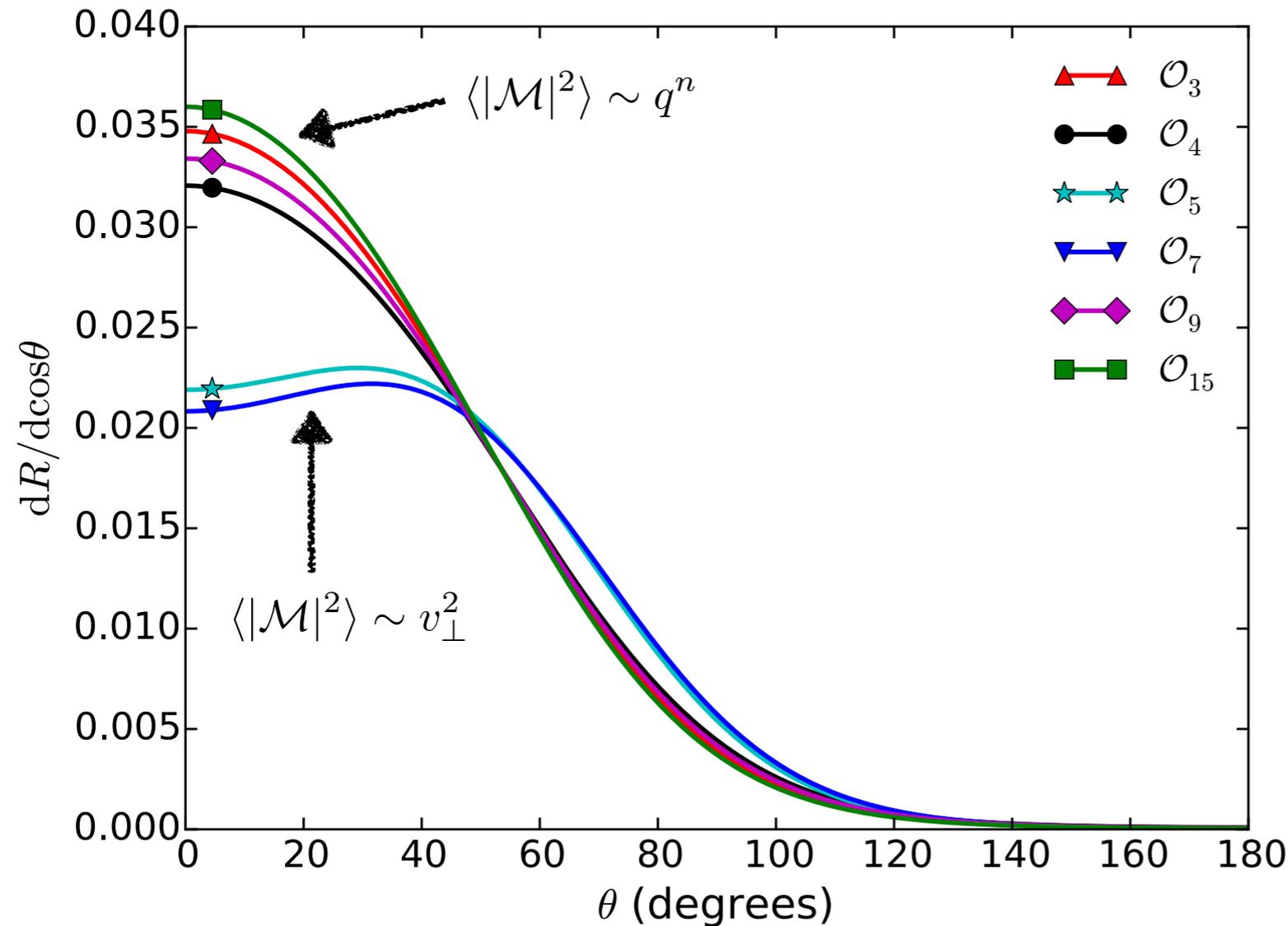


Backgrounds

Only need around 10 events to distinguish signal from background, and around 30 events to confirm the median direction of the flux [[astro-ph/0408047,1002.2717](#)].

Can also exploit time-dependence of the signal due to the motion of the Earth around the Sun [[1205.2333](#)].

# Directional Spectra



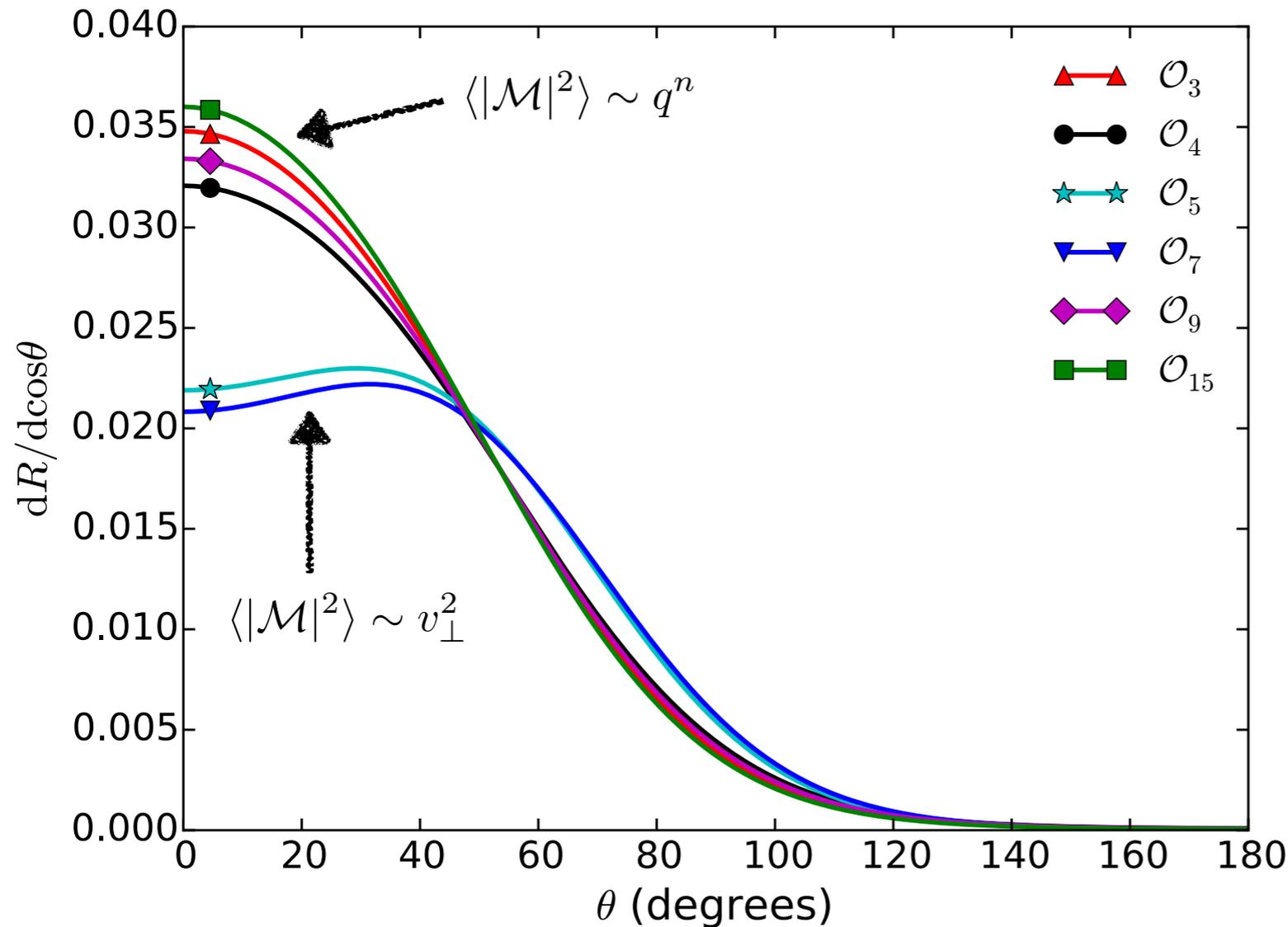
'Perfect'  $\text{CF}_4$  detector

$$E_R \in [20, 50] \text{ keV}$$

$$m_\chi = 100 \text{ GeV}$$

Note:  $q = 2\mu_{\chi N} \vec{v} \cdot \hat{q}$   
 $= 2\mu_{\chi N} v \cos \theta$

# Directional Spectra



'Perfect'  $\text{CF}_4$  detector

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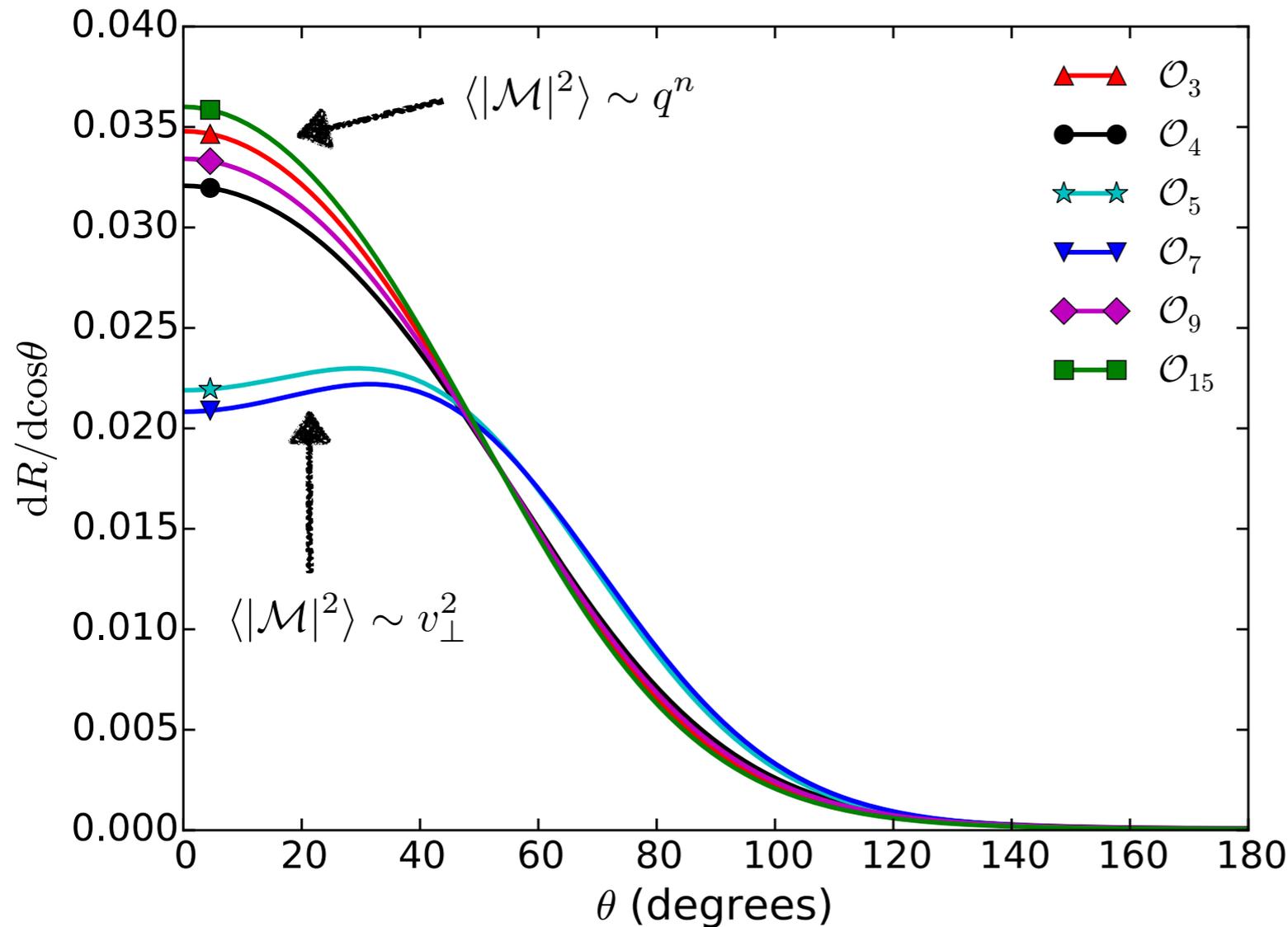
$$m_\chi = 100 \text{ GeV}$$

Note:  $q = 2\mu_{\chi N} \vec{v} \cdot \hat{q}$   
 $= 2\mu_{\chi N} v \cos \theta$

Most isotropic:  $\mathcal{O}_7 = \vec{S}_n \cdot \vec{v}_\perp \rightarrow \sigma_7 \sim v_\perp^2$

Least isotropic:  $\mathcal{O}_{15} = \left(\vec{S}_\chi \cdot \frac{\vec{q}}{m_n}\right) \left((\vec{S}_n \times \vec{v}_\perp) \cdot \frac{\vec{q}}{m_n}\right) \rightarrow \sigma_{15} \sim q^4 (q^2 + v_\perp^2)$

# A (new) ring-like feature



Operators which give

$$\langle |\mathcal{M}|^2 \rangle \sim (v_{\perp})^2$$

lead to a 'ring' in the directional rate.

A ring in the standard rate has been previously studied [Bozorgnia et al. - 1111.6361], but *this* ring occurs for lower WIMP masses (down to 10 GeV) and higher threshold energies (up to 10 keV).

# Likelihood Analysis

Generate mock data assuming an NREFT operator  
(  $\mathcal{O}_7$  or  $\mathcal{O}_{15}$  ).

Assume data is a combination of standard SD interaction and non-standard NREFT interaction. Fit to data with two free parameters  $m_\chi$  and  $A$  .

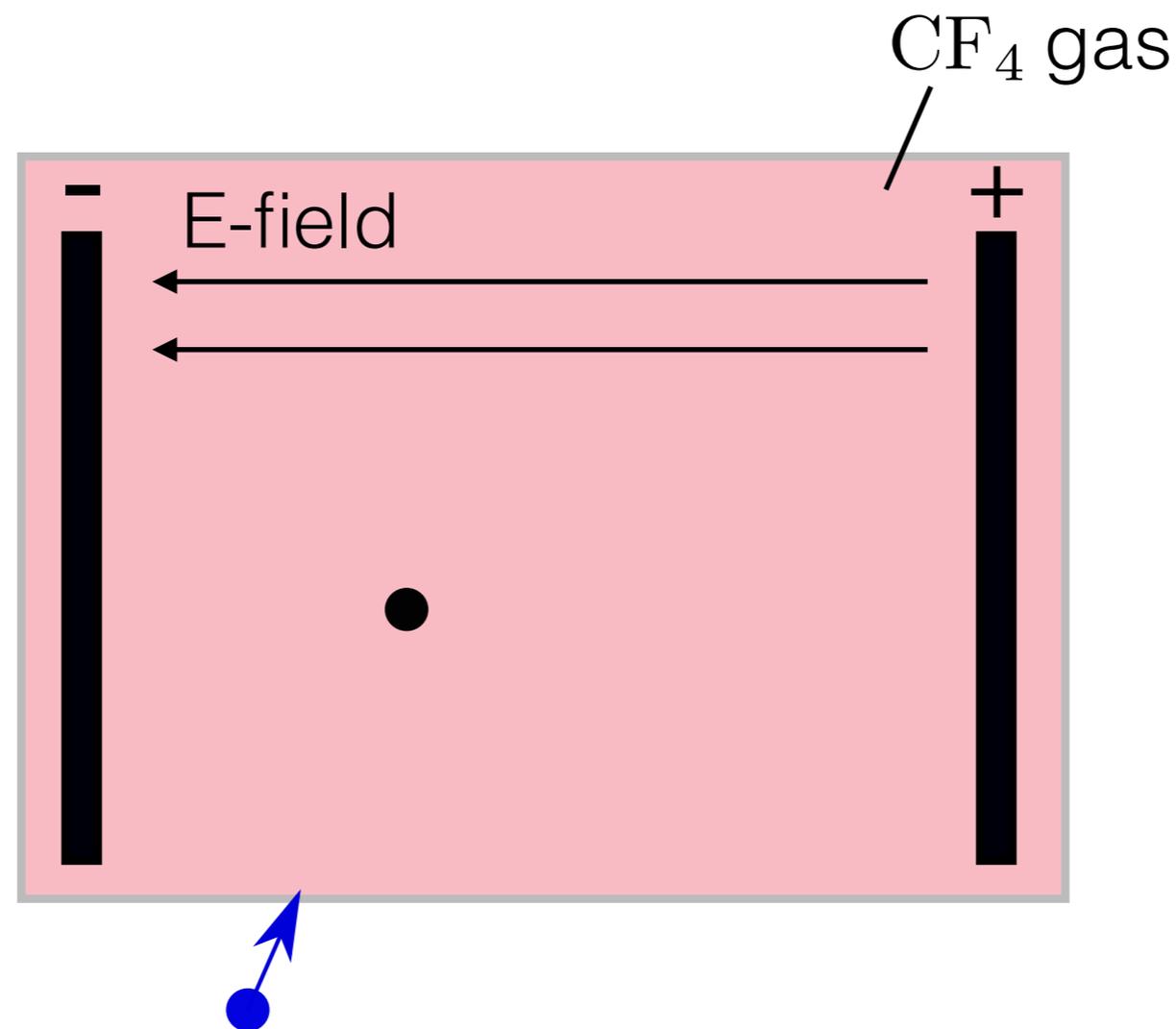
$A$  : fraction of events which are due to non-standard NREFT interaction.

Perform likelihood ratio test to determine the significance with which we can reject SD-only interactions (i.e. reject  $A = 0$ ) in 95% of pseudo-experiments.

Plot as a function of the number of signal events  $N_{\text{WIMP}}$ .

# Directional detection - TPCs

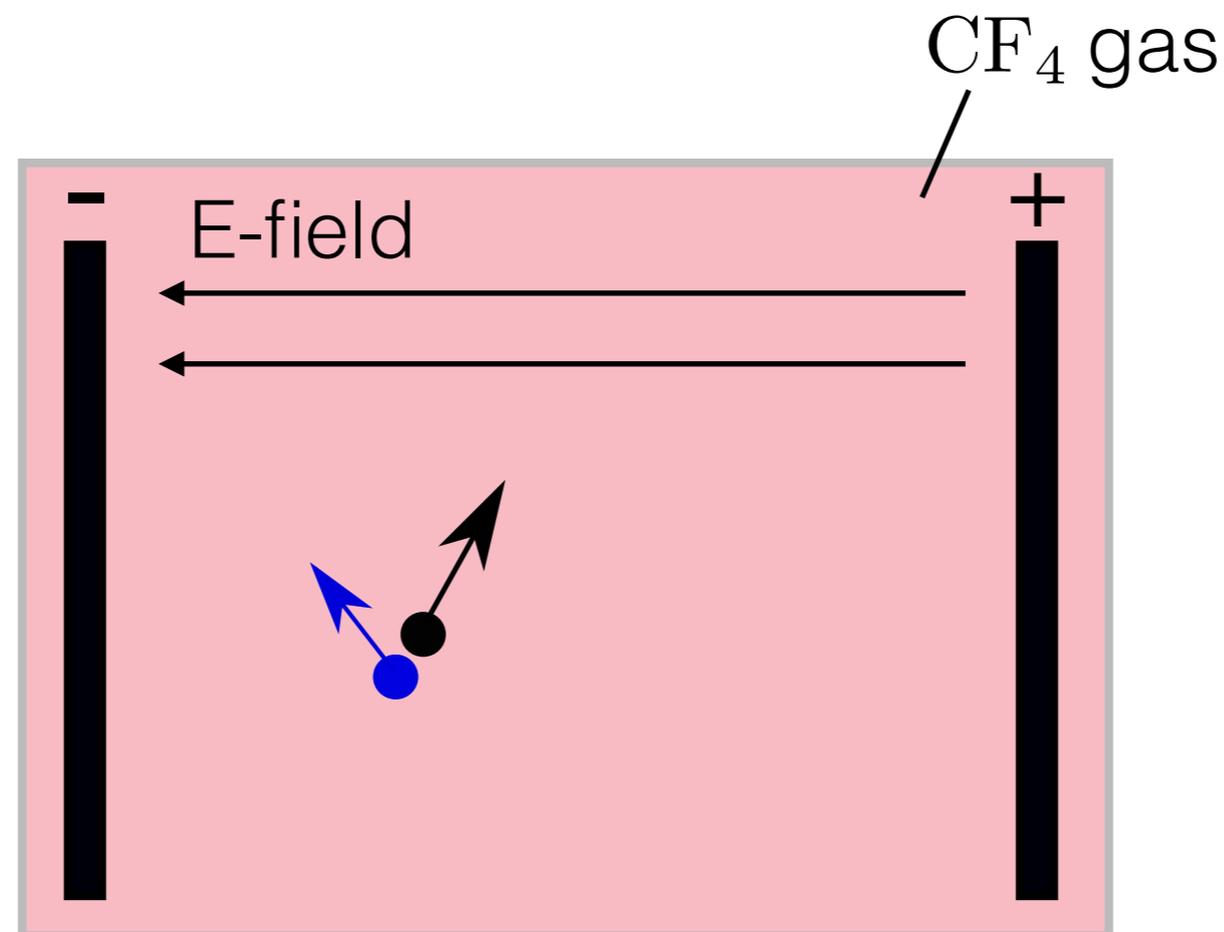
Most advanced technology is the gaseous Time Projection Chamber (TPC) : [e.g. DRIFT, MIMAC, DMTPC, NEWAGE, D3]



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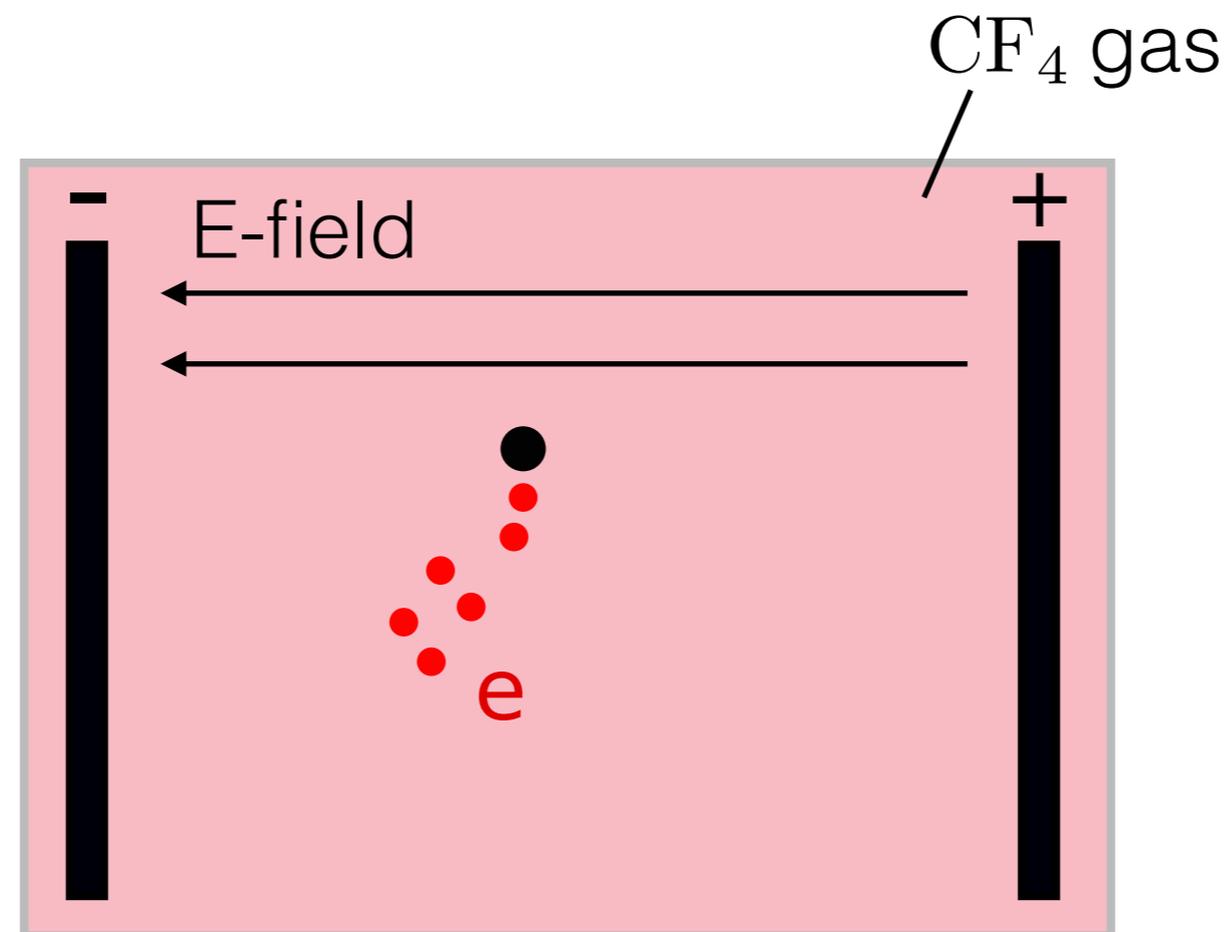
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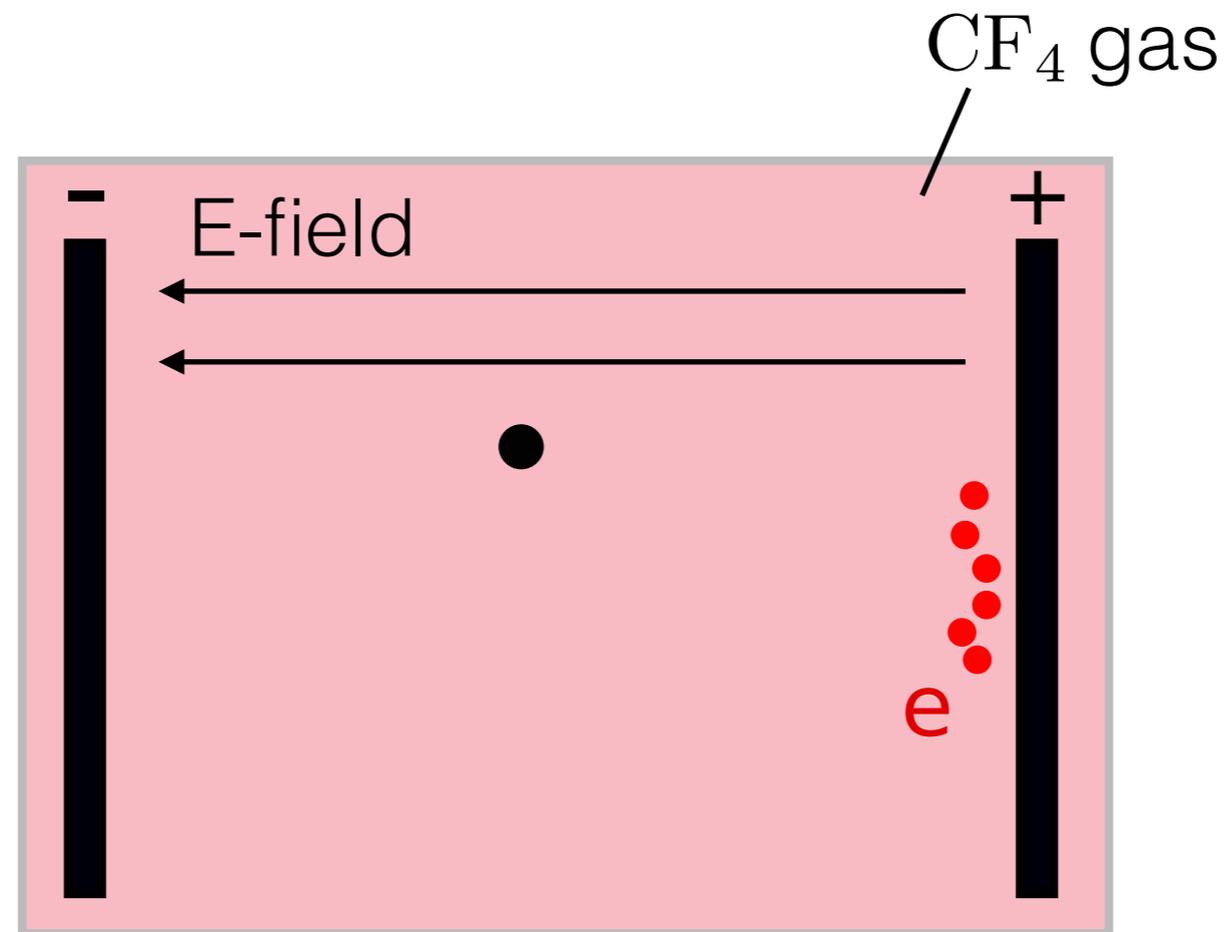
[e.g. DRIFT, MIMAC, DMTPC, NEWAGE, D3]



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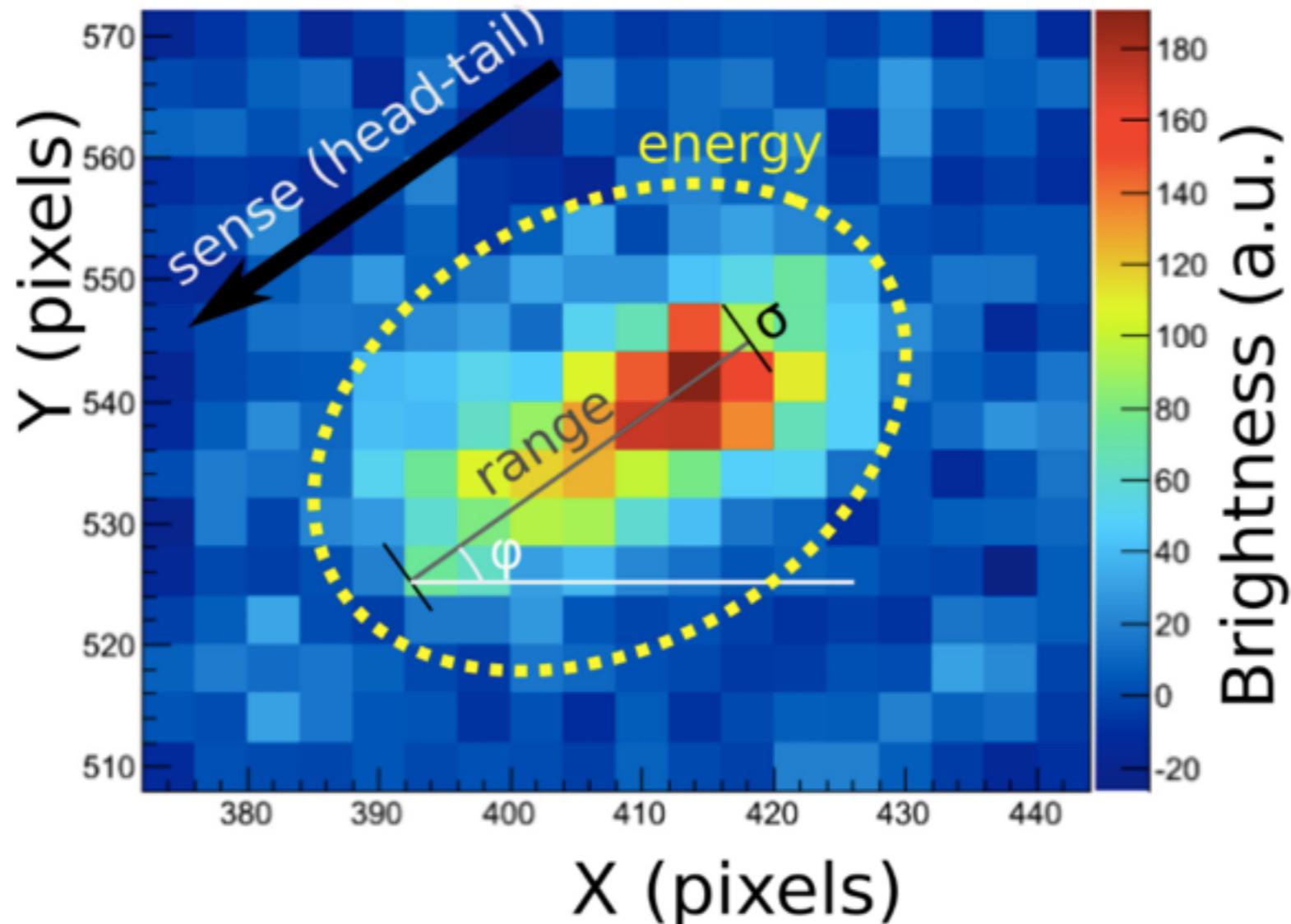


Get x,y of track from distribution of electrons hitting anode

Get z of track from timing of electrons hitting anode

# A 'Real' Signal

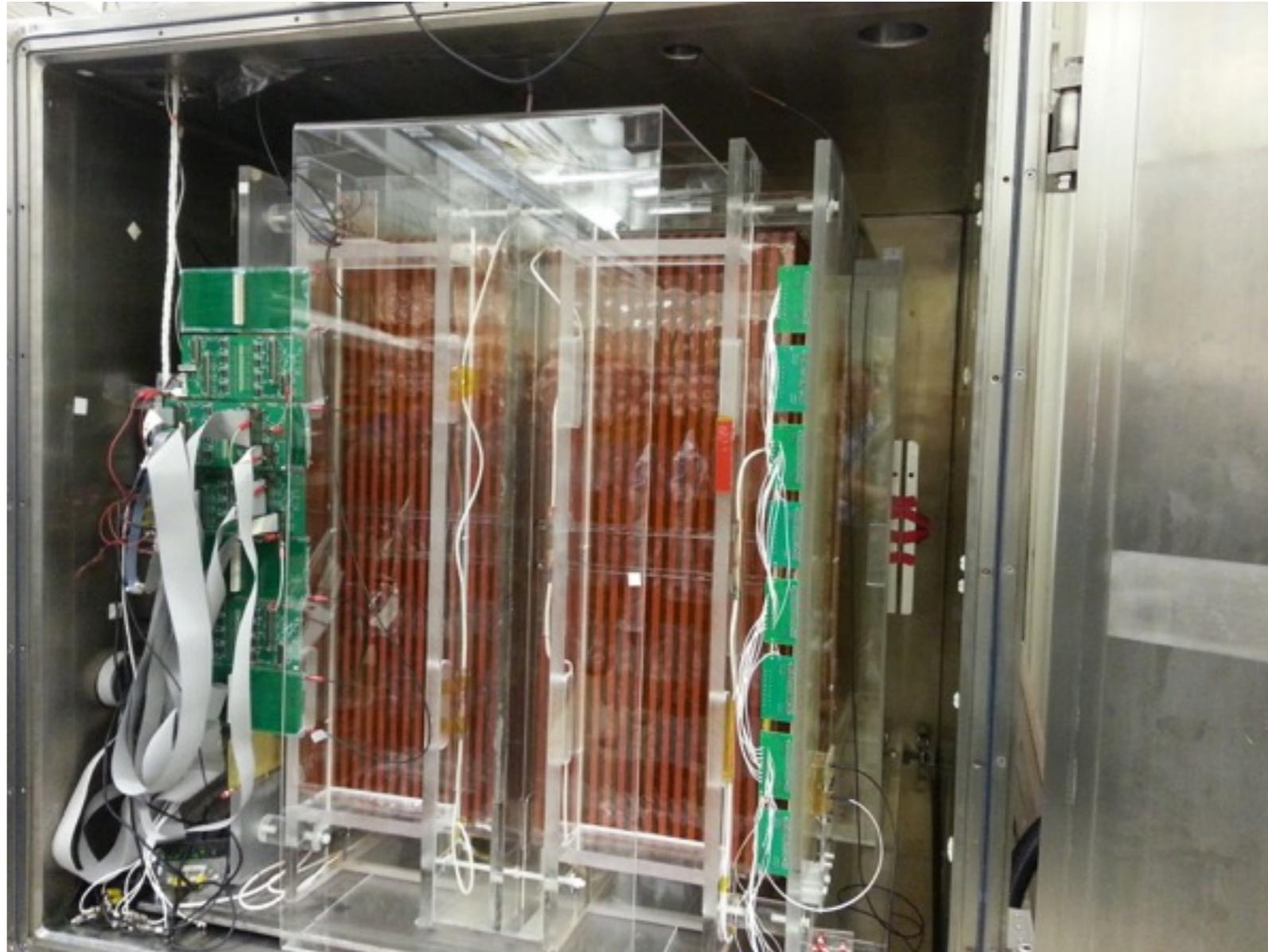
Deaconu et al. (DMTPC, 2015)



- Finite angular resolution -  $\Delta\theta \sim 20^\circ - 80^\circ$
- May not get full 3-D track information
- May not get head-tail discrimination

# A Real TPC

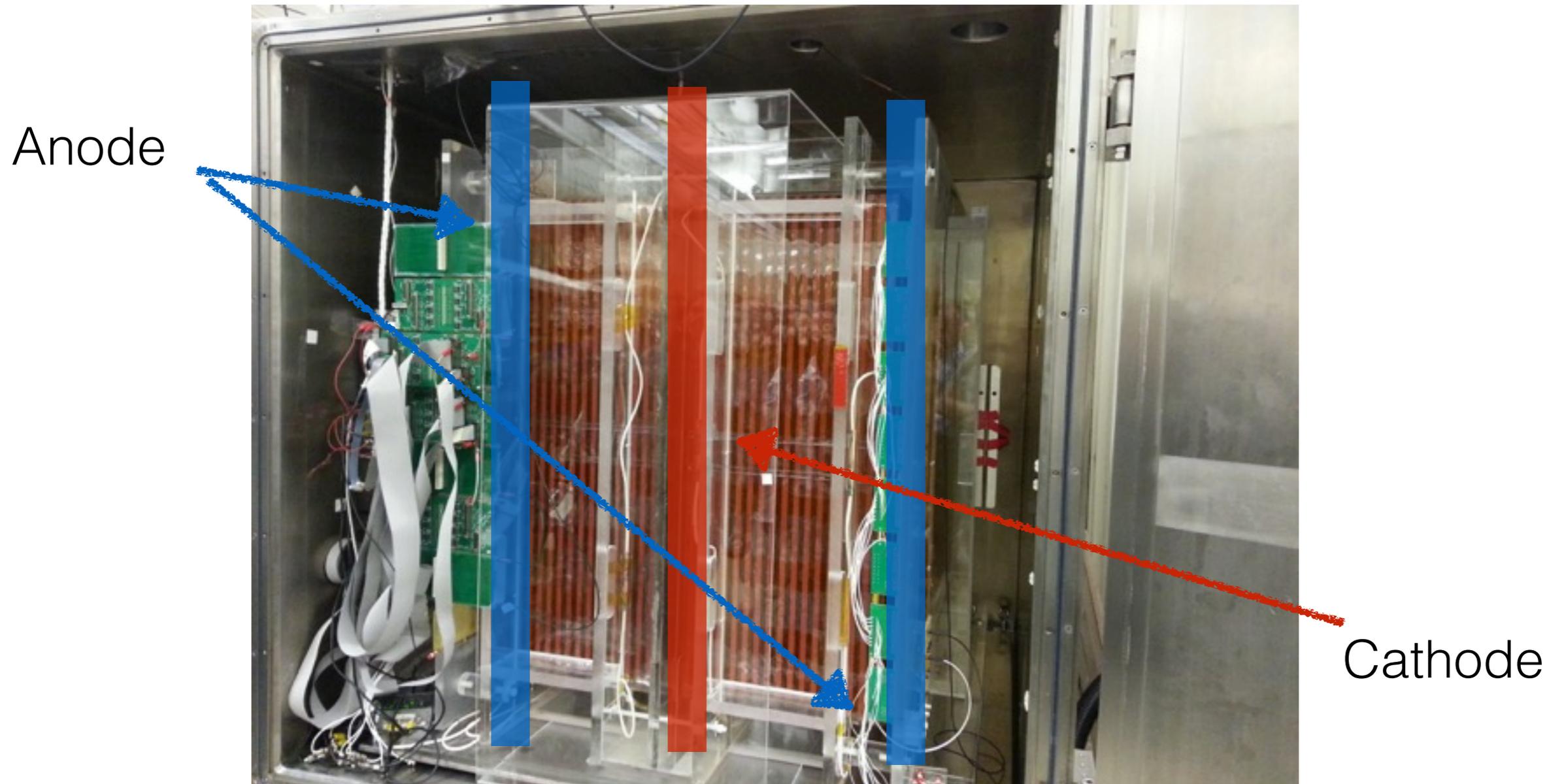
DRIFT-IIe prototype detector @ Occidental College, LA



Two back-to-back TPCs

# A Real TPC

DRIFT-IIe prototype detector @ Occidental College, LA



Two back-to-back TPCs

# Nuclear response functions

$$F_{1,1} = F_M$$

$$F_{3,3} = \frac{1}{8} \frac{q^2}{m_n^2} \left( v_{\perp}^2 F_{\Sigma'} + 2 \frac{q^2}{m_n^2} F_{\Phi''} \right)$$

$$F_{4,4} = \frac{C(j_{\chi})}{16} (F_{\Sigma'} + F_{\Sigma''})$$

$$F_{5,5} = \frac{C(j_{\chi})}{4} \frac{q^2}{m_n^2} \left( v_{\perp}^2 F_M + \frac{q^2}{m_n^2} F_{\Delta} \right)$$

$$F_{6,6} = \frac{C(j_{\chi})}{16} \frac{q^4}{m_n^4} F_{\Sigma''}$$

$$F_{7,7} = \frac{1}{8} v_{\perp}^2 F_{\Sigma'}$$

$$F_{8,8} = \frac{C(j_{\chi})}{4} \left( v_{\perp}^2 F_M + \frac{q^2}{m_n^2} F_{\Delta} \right)$$

$$F_{9,9} = \frac{C(j_{\chi})}{16} \frac{q^2}{m_n^2} F_{\Sigma'}$$

$$F_{10,10} = \frac{1}{4} \frac{q^2}{m_n^2} F_{\Sigma''}$$

$$F_{11,11} = \frac{1}{4} \frac{q^2}{m_n^2}$$

$$F_{12,12} = \frac{C(j_{\chi})}{16} \left( v_{\perp}^2 \left( F_{\Sigma''} + \frac{1}{2} F_{\Sigma'} \right) + \frac{q^2}{m_n^2} (F_{\tilde{\Phi}'} + F_{\Phi''}) \right)$$

$$F_{13,13} = \frac{C(j_{\chi})}{16} \frac{q^2}{m_n^2} \left( v_{\perp}^2 F_{\Sigma''} + \frac{q^2}{m_n^2} F_{\tilde{\Phi}'} \right)$$

$$F_{14,14} = \frac{C(j_{\chi})}{32} \frac{q^2}{m_n^2} v_{\perp}^2 F_{\Sigma'}$$

$$F_{15,15} = \frac{C(j_{\chi})}{32} \frac{q^4}{m_n^4} \left( v_{\perp}^2 F_{\Sigma'} + 2 \frac{q^2}{m_n^2} F_{\Phi''} \right)$$

$F_{M, \Sigma', \Sigma'', \tilde{\Phi}', \Phi'', \Delta}(q^2)$  are standard form factors encoding the distribution of nucleons in the nucleus - suppression at high  $q$ .

*Coupling to  $q^2$  does not affect the intrinsic directional rate.*

*But, each term in the response function is proportional to either  $(v_{\perp})^0$  or  $(v_{\perp})^2$ .*

# Transverse Radon Transform

For response functions coupling to  $(v_{\perp})^2$  we need to calculate the *Transverse Radon Transform* (TRT):

$$\hat{f}^T(v_{\min}, \hat{q}) = \int_{\mathbb{R}^3} \frac{(v_{\perp})^2}{c^2} f(\vec{v}) \delta(\vec{v} \cdot \hat{q} - v_{\min}) d^3\vec{v}$$

In the case of a Maxwell-Boltzmann distribution (e.g. SHM):

$$\hat{f}^T(v_{\min}, \hat{q}) = \frac{\left(2\sigma_v^2 + v_{\text{lag}}^2 - (\vec{v}_{\text{lag}} \cdot \hat{q})^2\right)}{\sqrt{2\pi}\sigma_v c^2} \exp\left[-\frac{(v_{\min} - \vec{v}_{\text{lag}} \cdot \hat{q})^2}{2\sigma_v^2}\right]$$

If we measure recoil angles  $\theta$  from the mean recoil direction  $\vec{v}_{\text{lag}}$ :

$$\hat{f}^T(v_{\min}, \hat{q}) = \frac{\left(2\sigma_v^2 + v_{\text{lag}}^2 \sin^2 \theta\right)}{\sqrt{2\pi}\sigma_v c^2} \exp\left[-\frac{(v_{\min} - v_{\text{lag}} \cos \theta)^2}{2\sigma_v^2}\right]$$

# Transverse Radon Transform (examples)

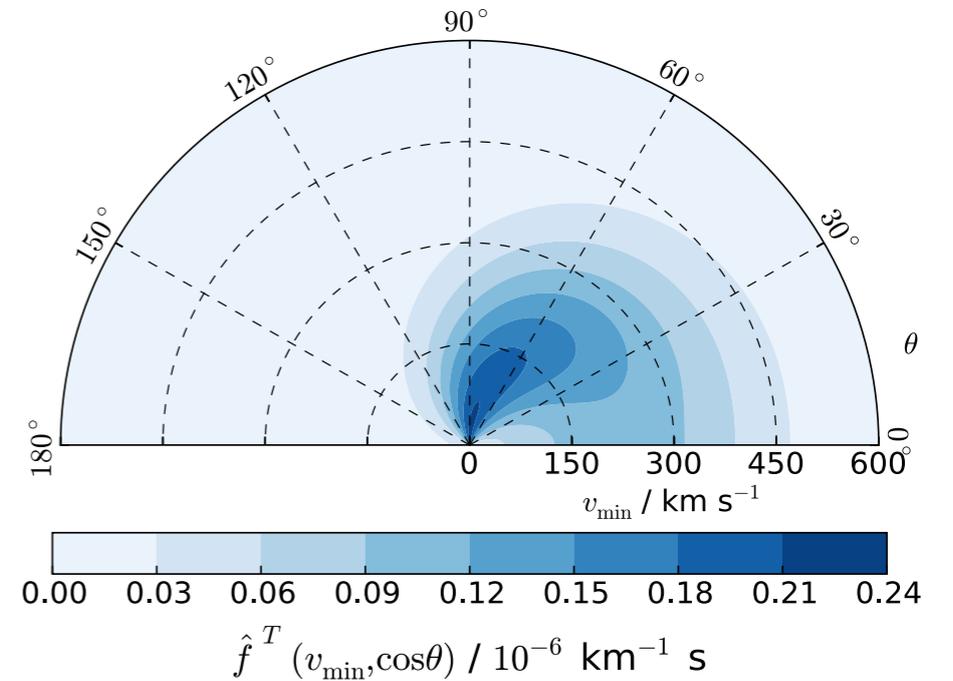
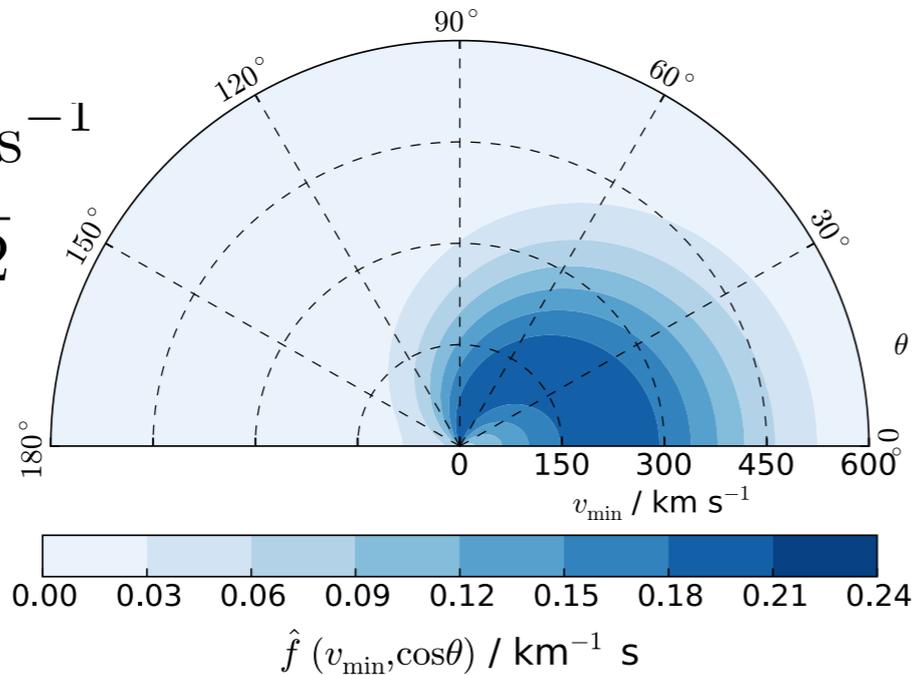
$$\hat{f}(v_{\min}, \hat{q})$$

$$\hat{f}^T(v_{\min}, \hat{q})$$

SHM:

$$v_{\text{lag}} = 220 \text{ km s}^{-1}$$

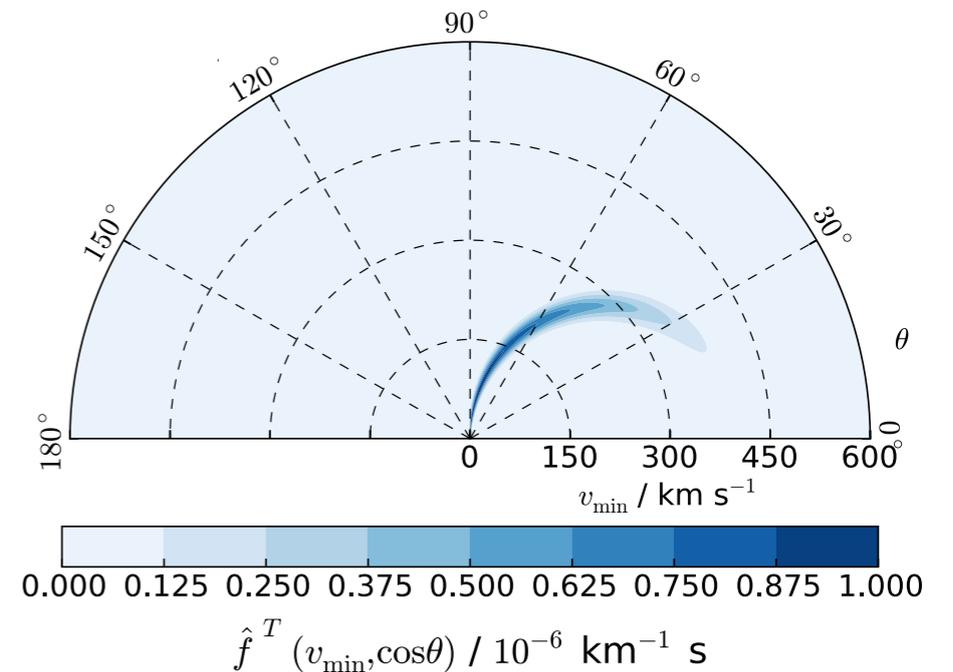
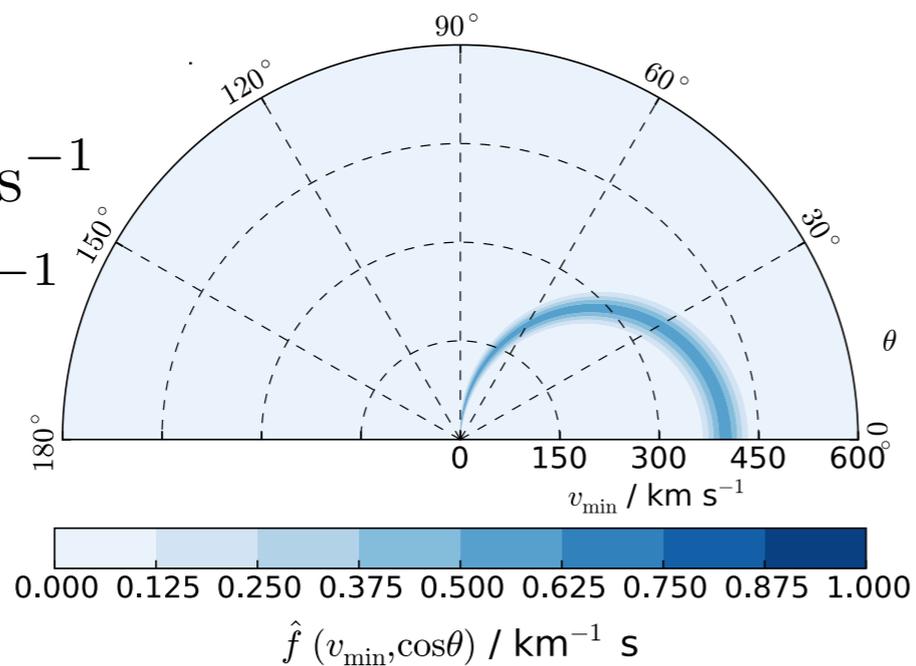
$$\sigma_v = v_{\text{lag}} / \sqrt{2}$$



Stream:

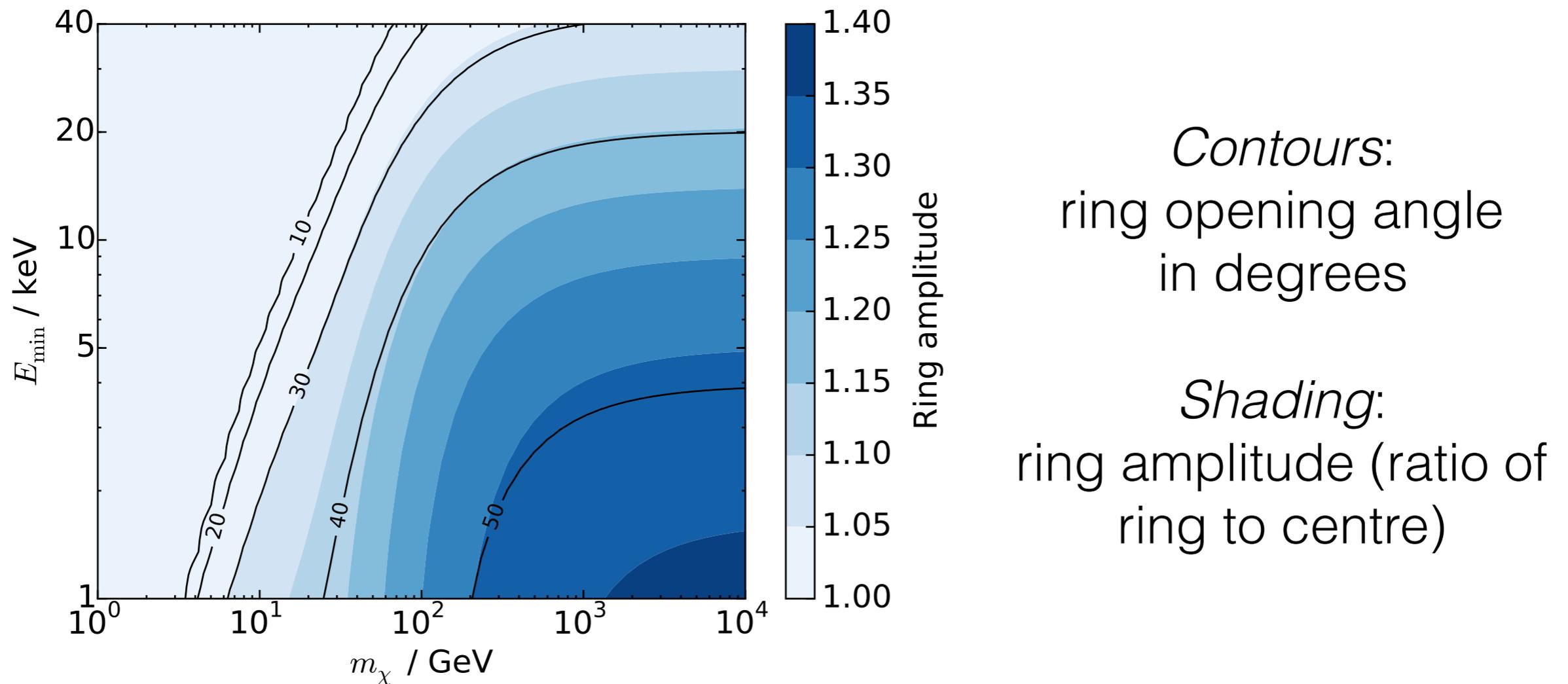
$$v_{\text{lag}} = 400 \text{ km s}^{-1}$$

$$\sigma_v = 20 \text{ km s}^{-1}$$



# A (new) ring-like feature

Operators with  $\langle |\mathcal{M}|^2 \rangle \sim (v_{\perp})^2$  lead to a 'ring' in the directional rate.



A ring in the standard rate has been previously studied [[Bozorgnia et al. - 1111.6361](#)], but *this* ring occurs for lower WIMP masses and higher threshold energies.

# Statistical tests

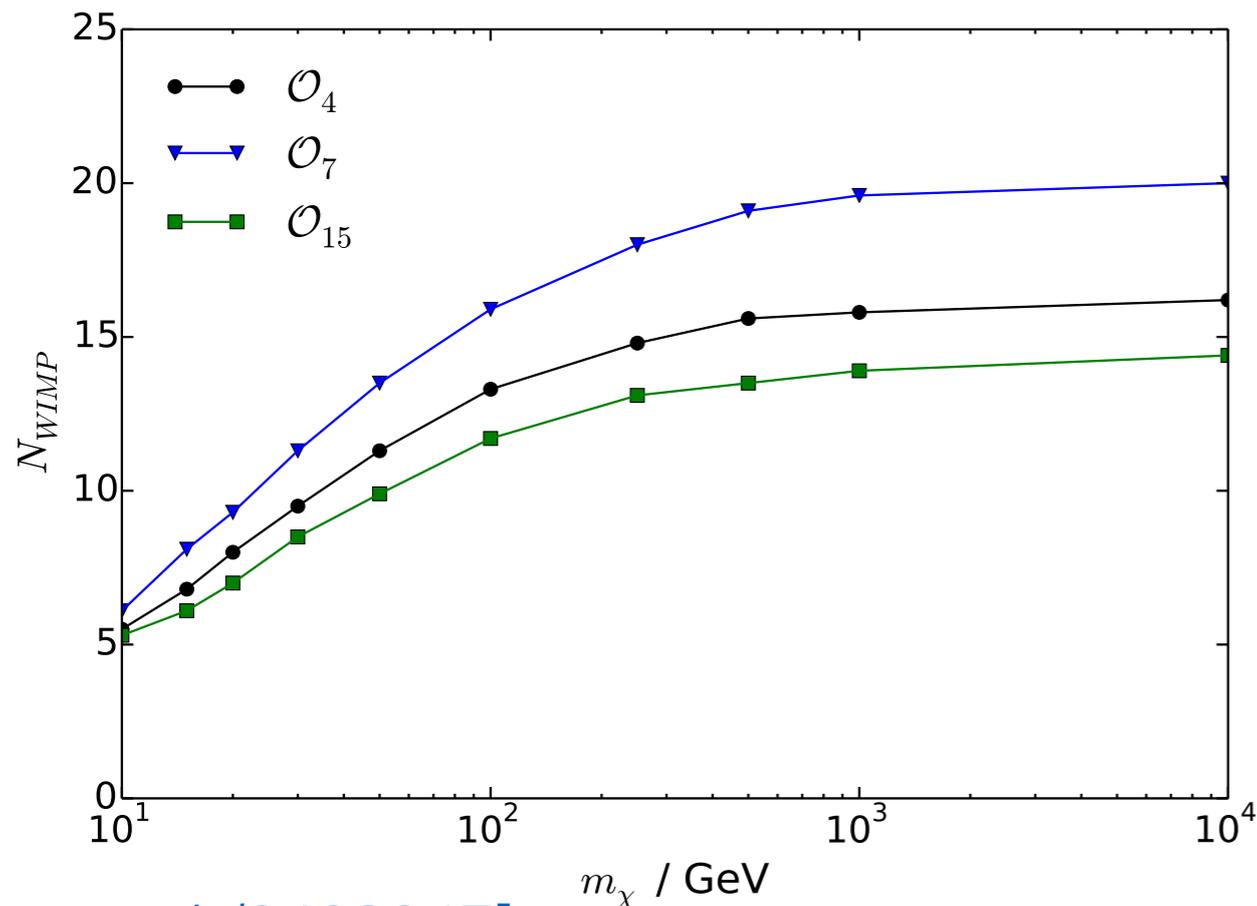
$$F_{4,4} \sim 1$$

$$F_{7,7} \sim v_{\perp}^2$$

$$F_{15,15} \sim q^4(q^2 + v_{\perp}^2)$$

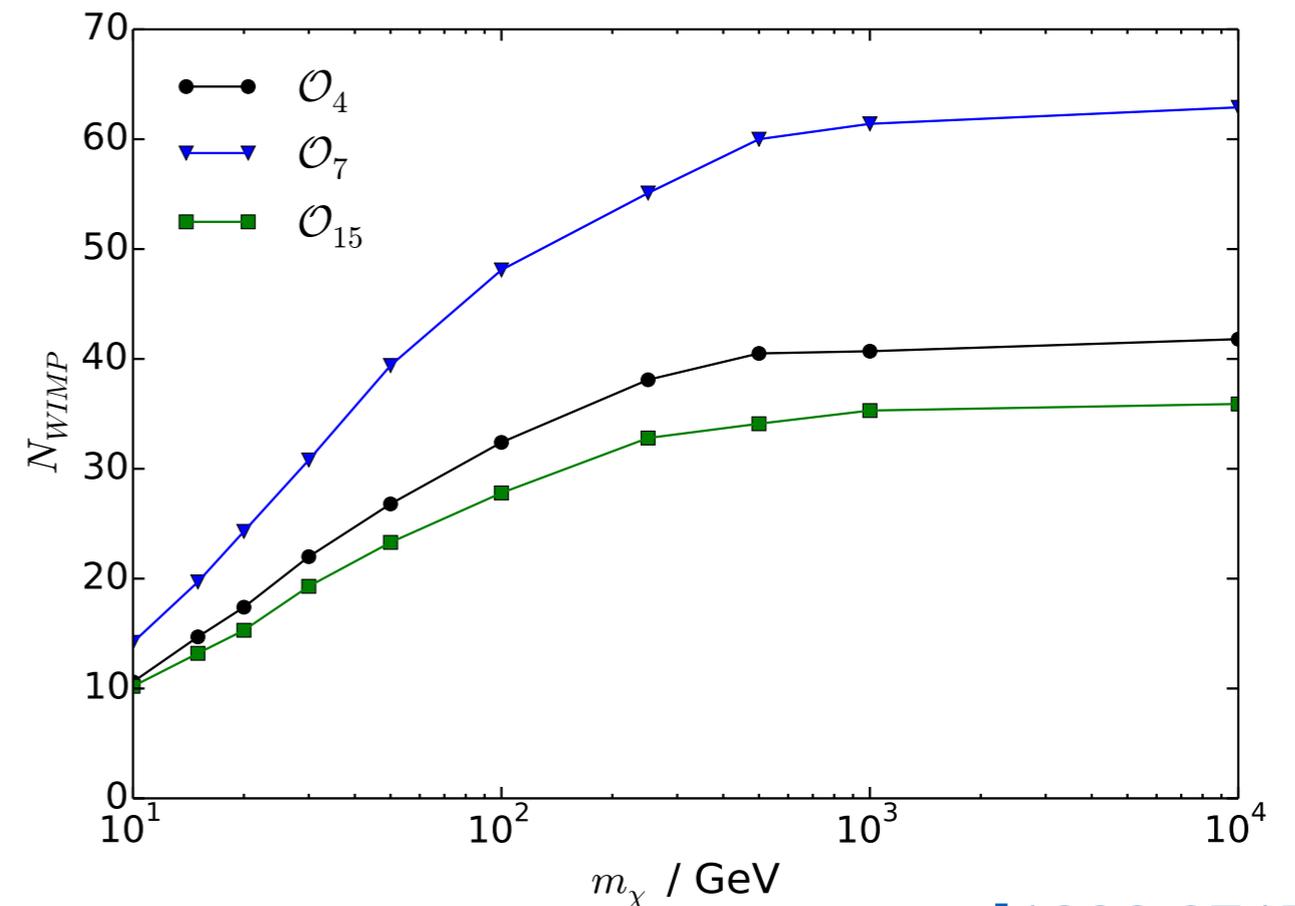
Calculate the number of signal events required to...

...reject isotropy...



[astro-ph/0408047]

...confirm the median recoil dir...



[1002.2717]

...at the  $2\sigma$  level in 95% of experiment.