



Stockholm  
University

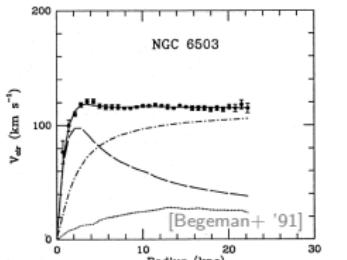
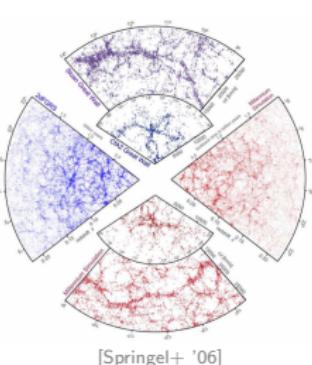
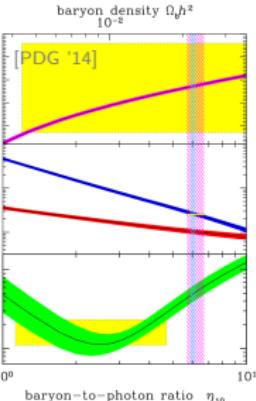
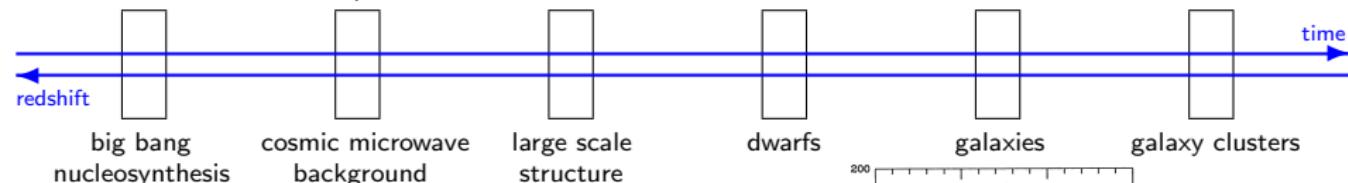
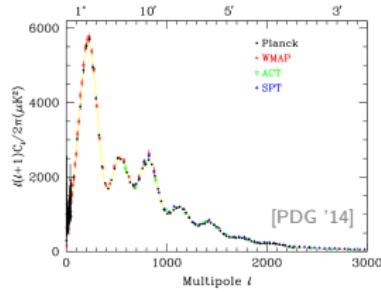
# MAPPING DARK MATTER IN THE MILKY WAY

Miguel Pato

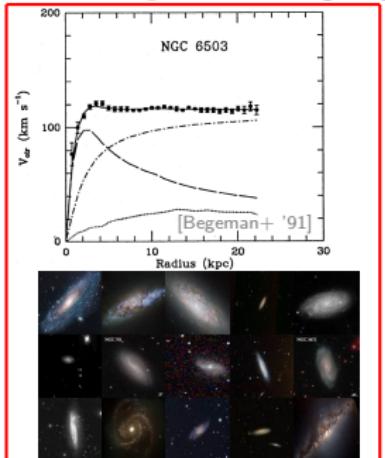
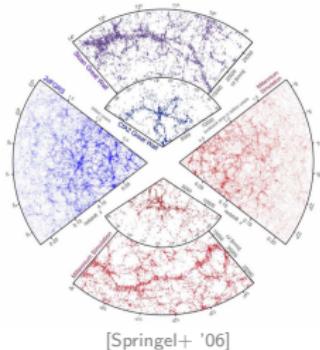
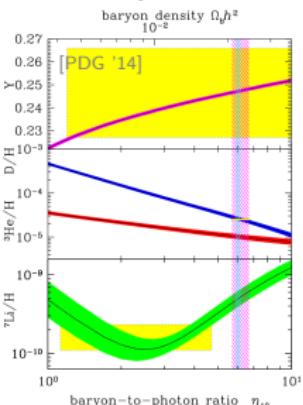
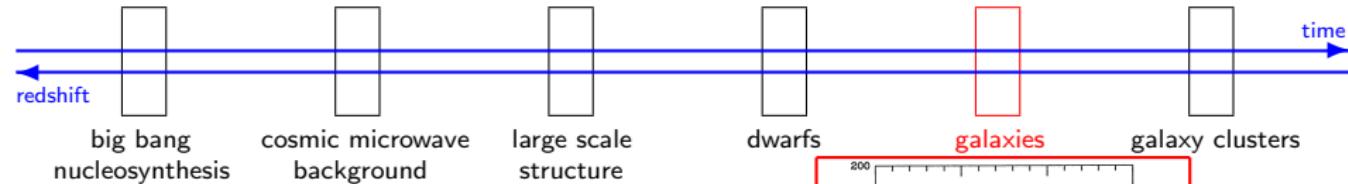
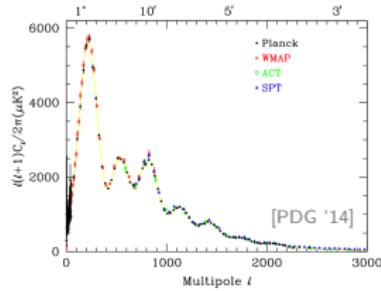
Wenner-Gren Fellow

The Oskar Klein Centre for Cosmoparticle Physics, Stockholm University

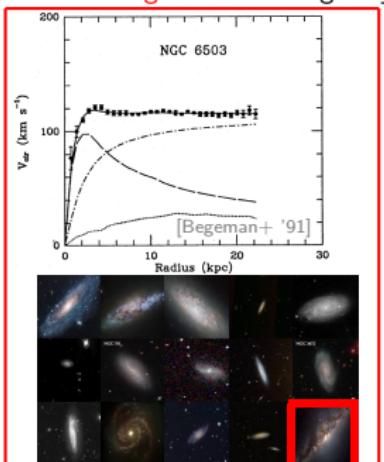
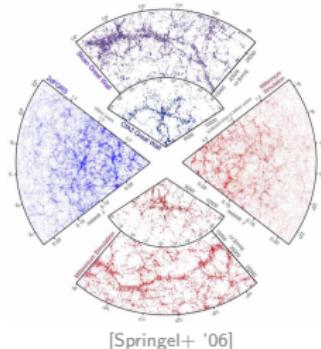
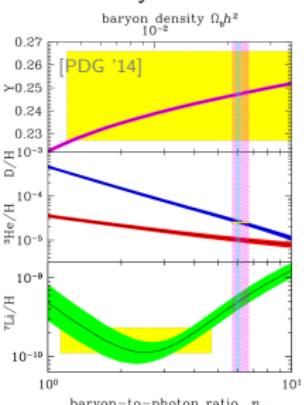
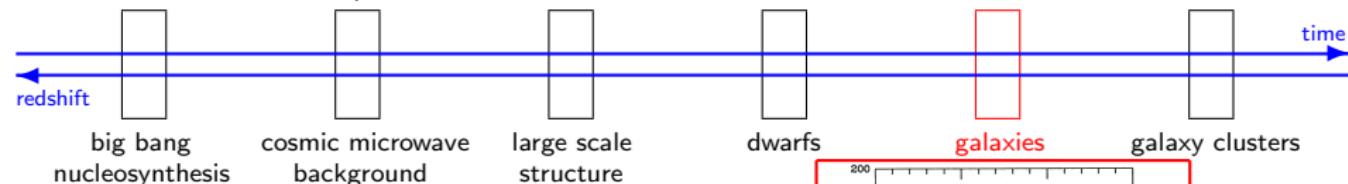
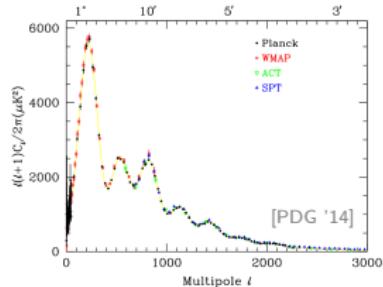
# DARK MATTER IN THE UNIVERSE



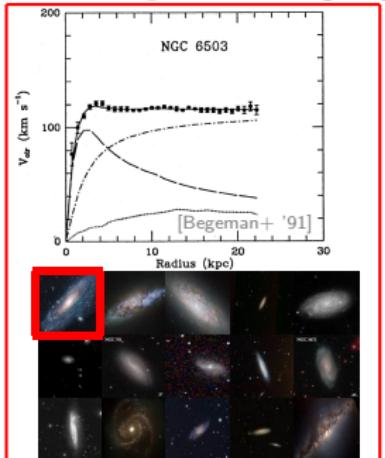
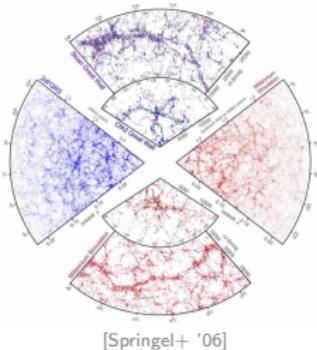
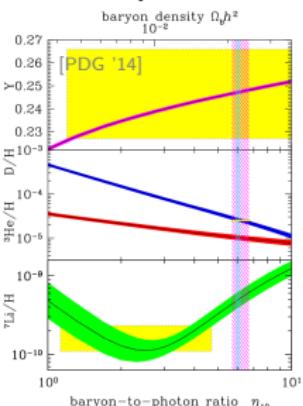
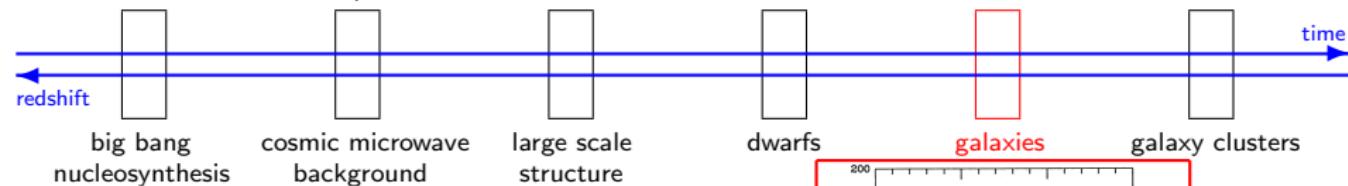
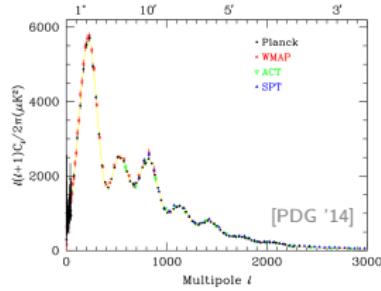
# DARK MATTER IN GALAXIES



# DARK MATTER IN THE MILKY WAY

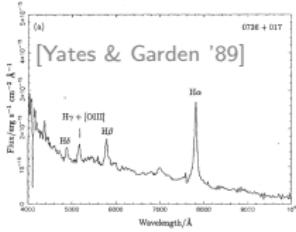


# DARK MATTER IN ANDROMEDA



# HISTORICAL PARENTHESIS: ANDROMEDA

The kinematics of an object is a prime tool to learn about its mass.



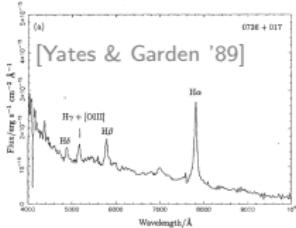
The kinematics of Andromeda has been studied since the 1930s through the Doppler shift of spectral lines in the gas.

$$\Delta\nu = -\frac{v_{\text{los}}}{c} \nu_0$$

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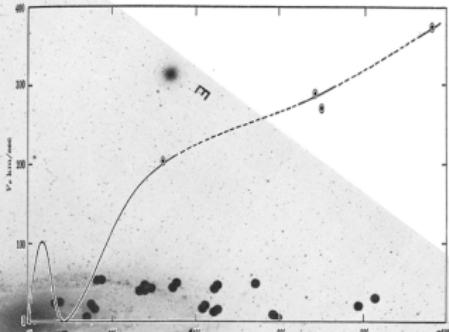


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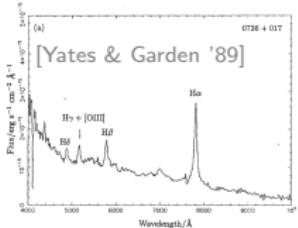
$$\Delta\nu = -\frac{v_{\text{los}}}{c} \nu_0$$



[Babcock '39, Rubin & Ford '70, Freeman '70, Rogstad & Shostak '72, Bosma '78, Rubin+ '80, '82, '85]

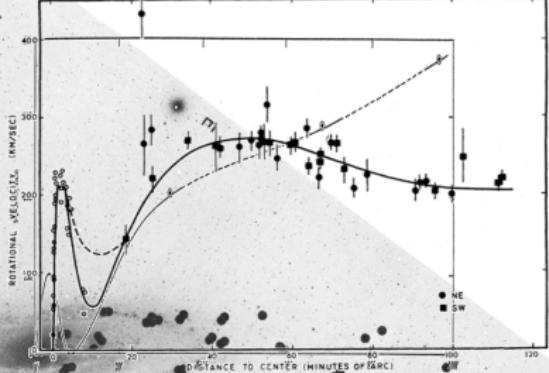
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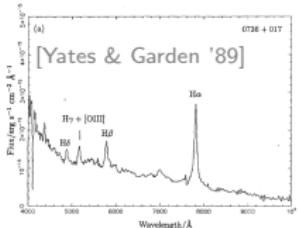


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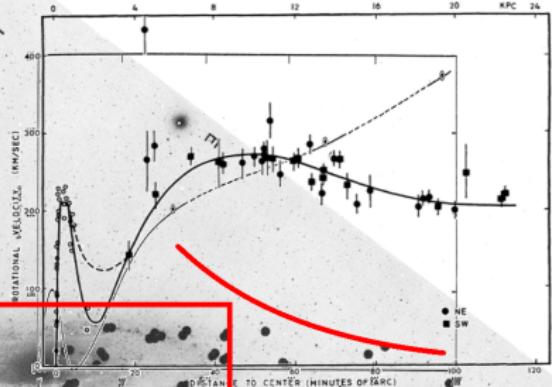
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visible matter

[Babcock '39, Rubin & Ford '70, Freeman '70, Rogstad & Shostak '72, Bosma '78, Rubin+ '80, '82, '85]

Under Newtonian gravity, a spherical mass induces

$$v_c^2 = \frac{GM(< r)}{r}$$

The rotation provided by the visible mass falls off as  $v_c \propto 1/\sqrt{r}$  at large  $r$ . A flat rotation curve implies\* a dark matter halo with  $M(< r) \propto r$ .

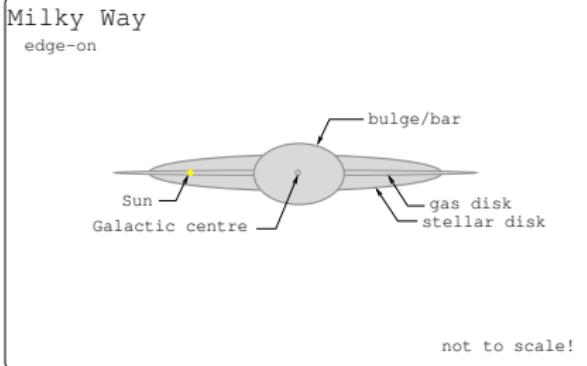
\* Modifications of gravity at galactic scales are also feasible. [Milgrom x3 '83]

# 1. TOUR OF THE GALAXY

The Milky Way is a complex bound system of stars, gas and dark matter.

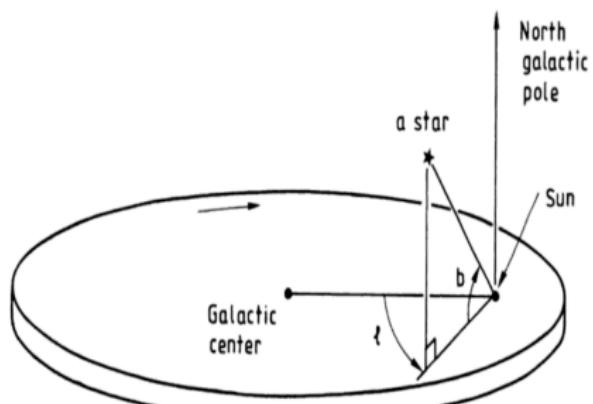


[Brunier]



We can identify the following main components:

- supermassive black hole, with mass  $4 \times 10^6 M_\odot$ ;
- stellar bulge, with barred shape of scale length  $2 - 3 \text{ kpc}$  and mass  $10^{10} M_\odot$ ;
- stellar disc, decomposed into thin and thick components of scale length  $10 \text{ kpc}$  and total mass  $10^{10} M_\odot$  with a marked spiral structure;
- gas, in molecular, atomic and ionised phases (mainly H) with a patchy distribution towards the centre and a disc-like structure otherwise; and

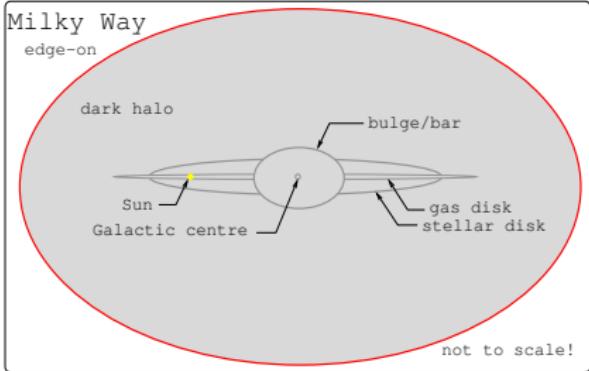


The Sun is located slightly above the Galactic plane at  $R_0 \simeq 8 \text{ kpc}$  from the Galactic centre, in between two major spiral arms, and travels together with the local standard of rest at about  $220 \text{ km/s}$  in a roughly circular orbit.

[Binney & Tremaine '87]

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- gas, in molecular, atomic and ionised phases (mainly H) with a patchy distribution towards the centre and a disc-like structure otherwise; and
- dark matter halo, extending hundreds of kpc.

$$\phi_{\text{tot}} = \phi_{\text{bulge}} + \phi_{\text{disc}} + \phi_{\text{gas}} + \phi_{\text{dm}}$$

how can we constrain the parameters of a galactic mass model?

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# 1. TOUR OF THE GALAXY

$$\phi_{\text{tot}} = \phi_{\text{bulge}} + \phi_{\text{disc}} + \phi_{\text{gas}} + \phi_{\text{dm}}$$

**kinematics** traces total potential

- |                                |                         |
|--------------------------------|-------------------------|
| $R \sim 0.1 - 30 \text{ kpc}$  | rotation curve tracers  |
| $R \sim 8 - 60 \text{ kpc}$    | star population tracers |
| $R \sim 100 - 300 \text{ kpc}$ | satellite kinematics    |
| $R \sim 300+ \text{ kpc}$      | timing in Local Group   |

**photometry** traces individual baryonic components

- |       |   |
|-------|---|
| bulge | star counts, luminosity, microlensing     |
| disc  | star counts, luminosity, stellar dynamics |
| gas   | emission lines, dispersion measure        |

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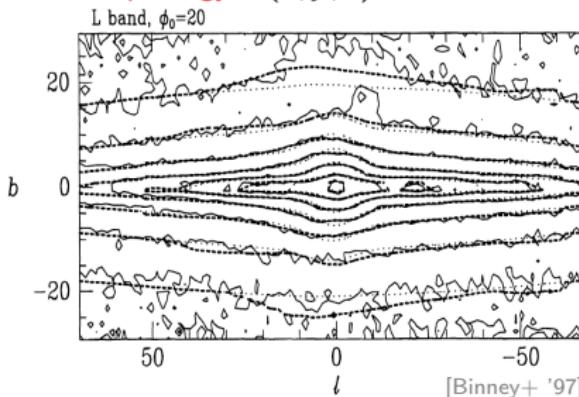
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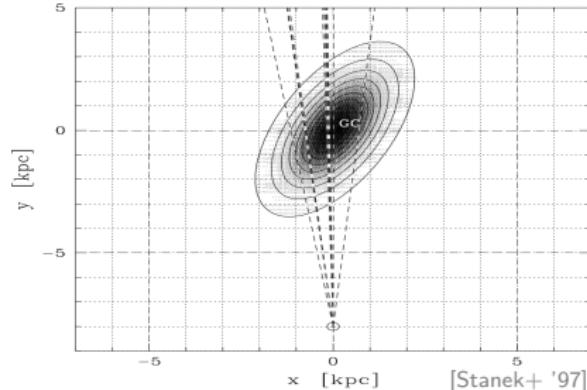
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# 1. TOUR OF THE GALAXY: STELLAR BULGE

**morphology**  $f(x, y, z)$

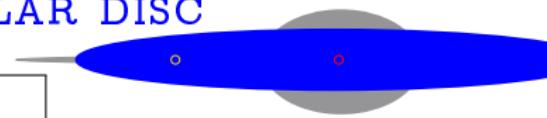


$$\rho_{\text{bulge}} = \rho_0 f(x, y, z)$$



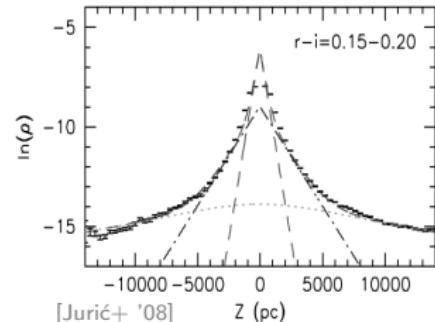
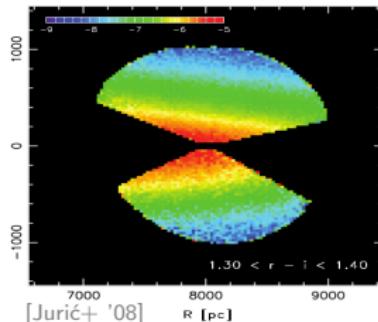
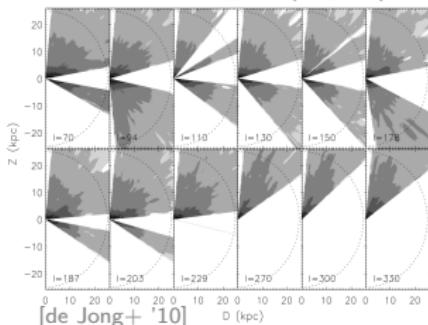
Stanek+ '97 (E2)	$e^{-r}$	0.9:0.4:0.3	24°	optical
Stanek+ '97 (G2)	$e^{-r_s^2/2}$	1.2:0.6:0.4	25°	optical
Zhao '96	$e^{-r_s^2/2} + r_a^{-1.85} e^{-r_a}$	1.5:0.6:0.4	20°	infrared
Bissantz & Gerhard '02	$e^{-r_s^2/(1+r)^{1.8}}$	2.8:0.9:1.1	20°	infrared
Lopez-Corredoira+ '07	Ferrer potential	7.8:1.2:0.2	43°	infrared/optical
Vanhollebeke+ '09	$e^{-r_s^2/(1+r)^{1.8}}$	2.6:1.8:0.8	15°	infrared/optical
Robin+ '12	$\operatorname{sech}^2(-r_s) + e^{-r_s}$	1.5:0.5:0.4	13°	infrared

# 1. TOUR OF THE GALAXY: STELLAR DISC



$$\rho_{\text{disc}} = \rho_0 f(x, y, z)$$

**morphology**  $f(x, y, z)$



Han & Gould '03

$$e^{-R} \operatorname{sech}^2(z)$$

2.8:0.27

thin

optical

$$e^{-R-|z|}$$

2.8:0.44

thick

Calchi-Novati & Mancini '11

$$e^{-R-|z|}$$

2.8:0.25

thin

optical

$$e^{-R-|z|}$$

4.1:0.75

thick

de Jong+ '10

$$e^{-R-|z|}$$

2.8:0.25

thin

optical

$$e^{-R-|z|}$$

4.1:0.75

thick

$$(R^2 + z^2)^{-2.75/2}$$

1.0:0.88

halo

Jurić+ '08

$$e^{-R-|z|}$$

2.2:0.25

thin

optical

$$e^{-R-|z|}$$

3.3:0.74

thick

$$(R^2 + z^2)^{-2.77/2}$$

1.0:0.64

halo

Bovy & Rix '13

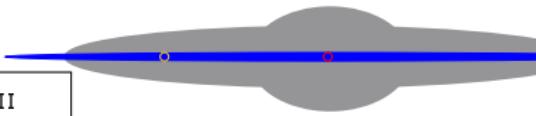
$$e^{-R-|z|}$$

2.2:0.40

single

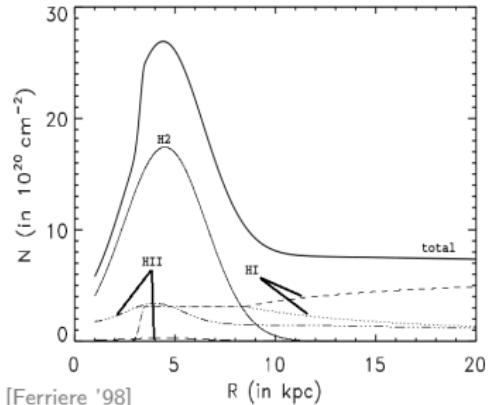
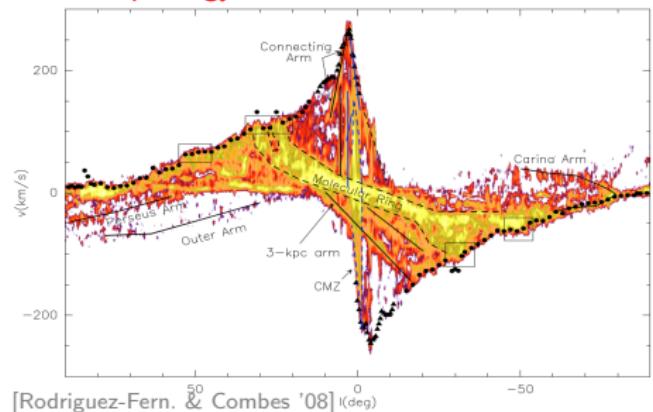
optical

# 1. TOUR OF THE GALAXY: GAS



$$n_{\text{H}} = 2n_{\text{H}_2} + n_{\text{HI}} + n_{\text{HII}}$$

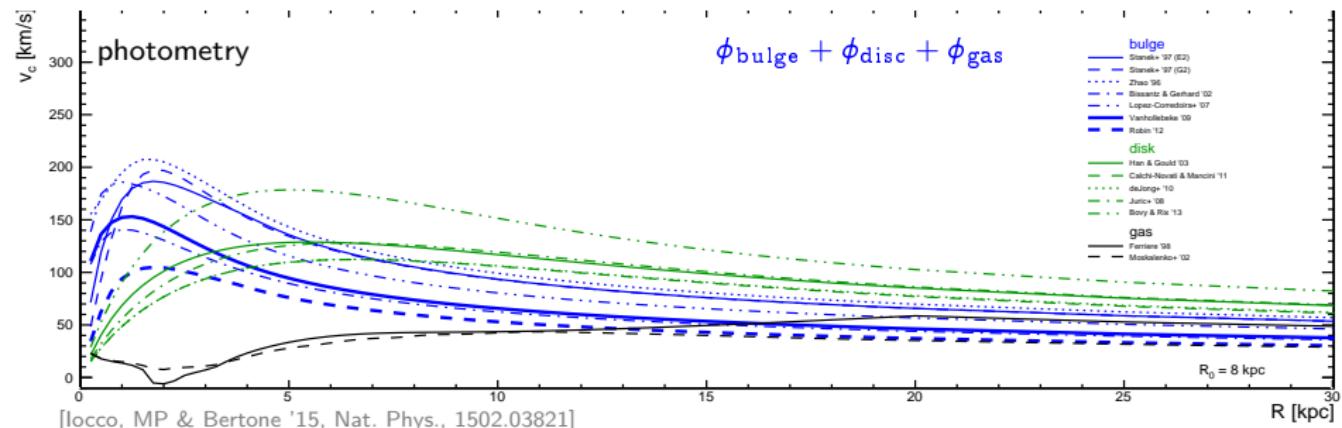
**morphology**



Ferrière '12	$r < 0.01 \text{ kpc}$	$M_{\text{gas}} \sim 7 \times 10^5 M_{\odot}$	CO, 21cm, H $\alpha$ , ...
Ferrière+ '07	$r = 0.01 - 2 \text{ kpc}$	CMZ, holed disc	H <sub>2</sub> CO
		CMZ, holed disc	H I 21cm
		warm, hot, very hot	H II disp. meas.
Ferrière '98	$r = 3 - 20 \text{ kpc}$	molecular ring	H <sub>2</sub> CO
		cold, warm	H I 21cm
		warm, hot	H II disp. meas., H $\alpha$
Moskalenko+ '02	$r = 3 - 20 \text{ kpc}$	molecular ring	H <sub>2</sub> CO
			H I 21cm
			H II disp. meas.

# 1. TOUR OF THE GALAXY: PHOTOMETRY

$$\phi_{\text{tot}} = \phi_{\text{bulge}} + \phi_{\text{disc}} + \phi_{\text{gas}} + \phi_{\text{dm}}$$



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bulge star counts, luminosity, microlensing

disc star counts, luminosity, stellar dynamics

gas emission lines, dispersion measure

# 1. TOUR OF THE GALAXY: ROTATION CURVE

$$v_c^2 = r \frac{d\phi_{\text{tot}}}{dr} \stackrel{\text{sph.}}{\equiv} \frac{G M_{\text{tot}}(< r)}{r}$$

Rotation curve tracers are young objects or regions that track galactic rotation. In external galaxies the only available tracer is the gas, while in our Galaxy we can use also some stars and star-forming regions. However, the case of our Galaxy is much more challenging due to our position.



[Credit: HST]

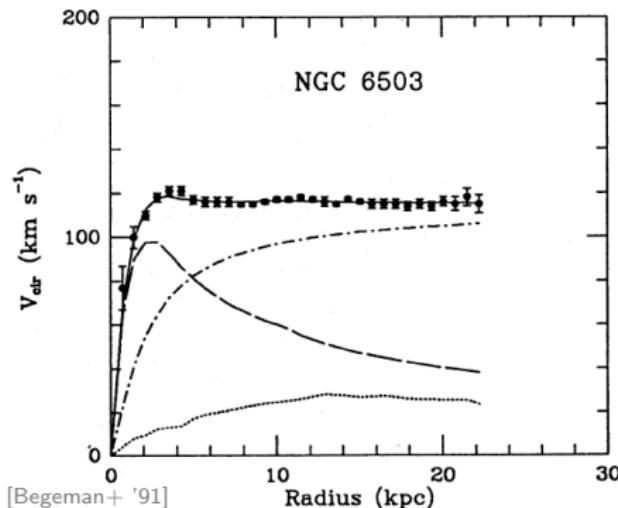


[Credit: Brunier / NASA]

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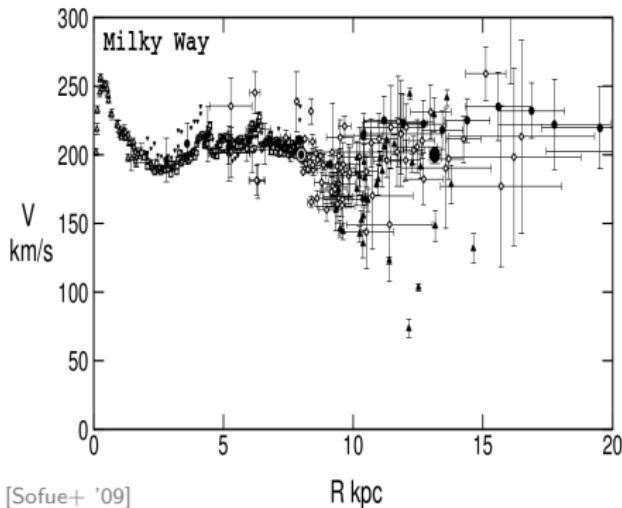
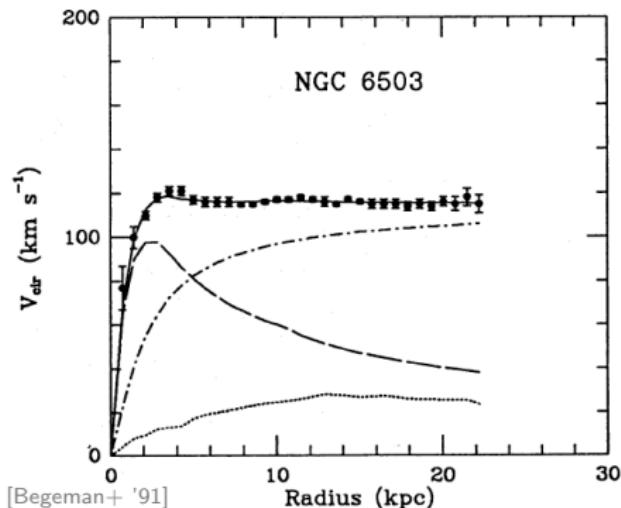
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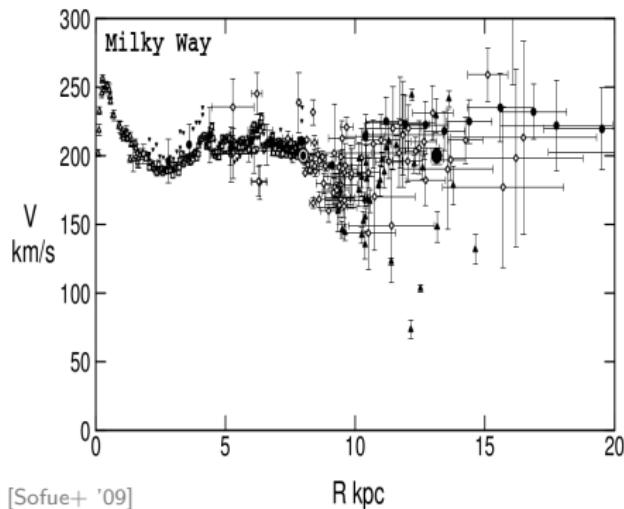
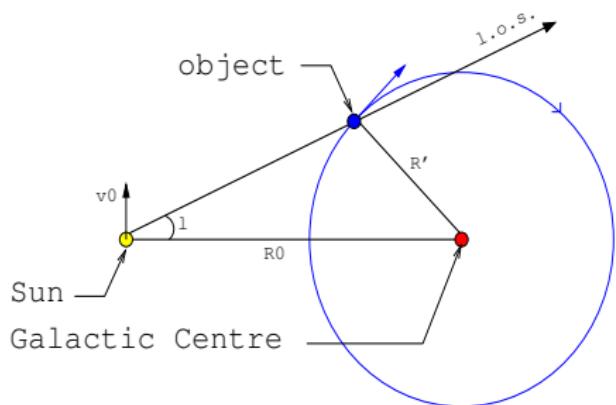
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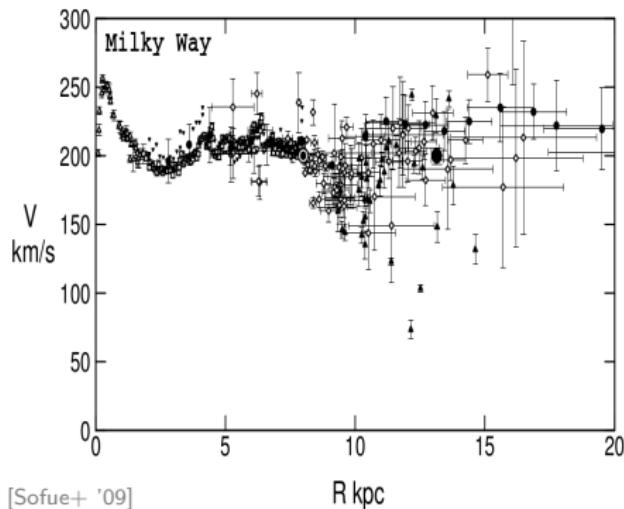
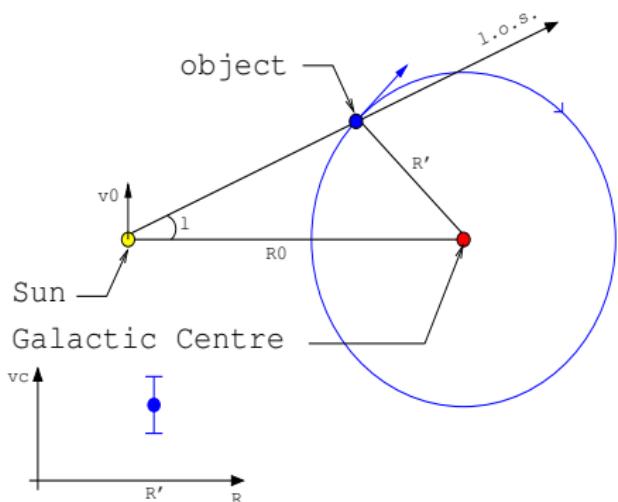


$$v_{\text{los}}^{\text{ISR}} = \left( \frac{v_c(R')}{R'/R_0} - v_0 \right) \cos b \sin \ell$$

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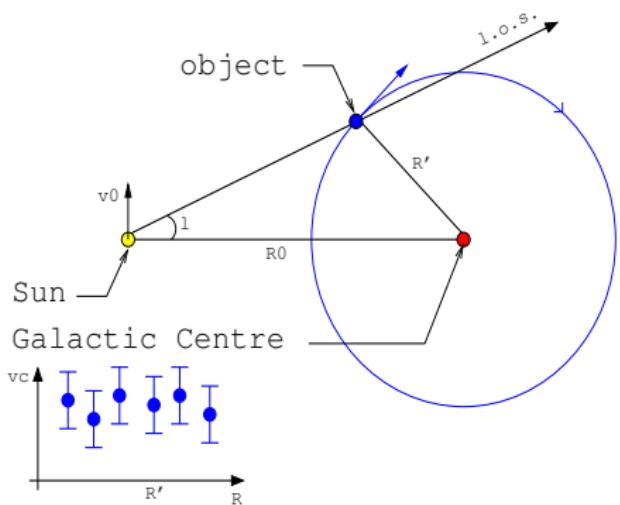


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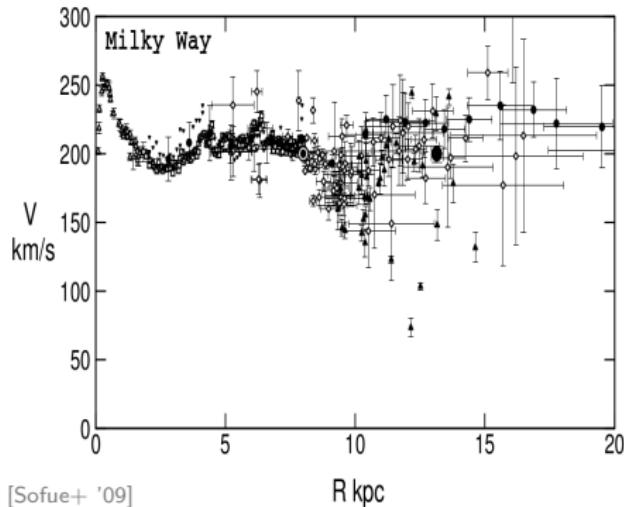
# 1. TOUR OF THE GALAXY: ROTATION CURVE

$$v_c^2 = r \frac{d\phi_{\text{tot}}}{dr} \stackrel{\text{sph.}}{=} \frac{GM_{\text{tot}}(< r)}{r}$$

Rotation curve tracers are young objects or regions that track galactic rotation. In external galaxies the only available tracer is the gas, while in our Galaxy we can use also some stars and star-forming regions. However, the case of our Galaxy is much more challenging due to our position.

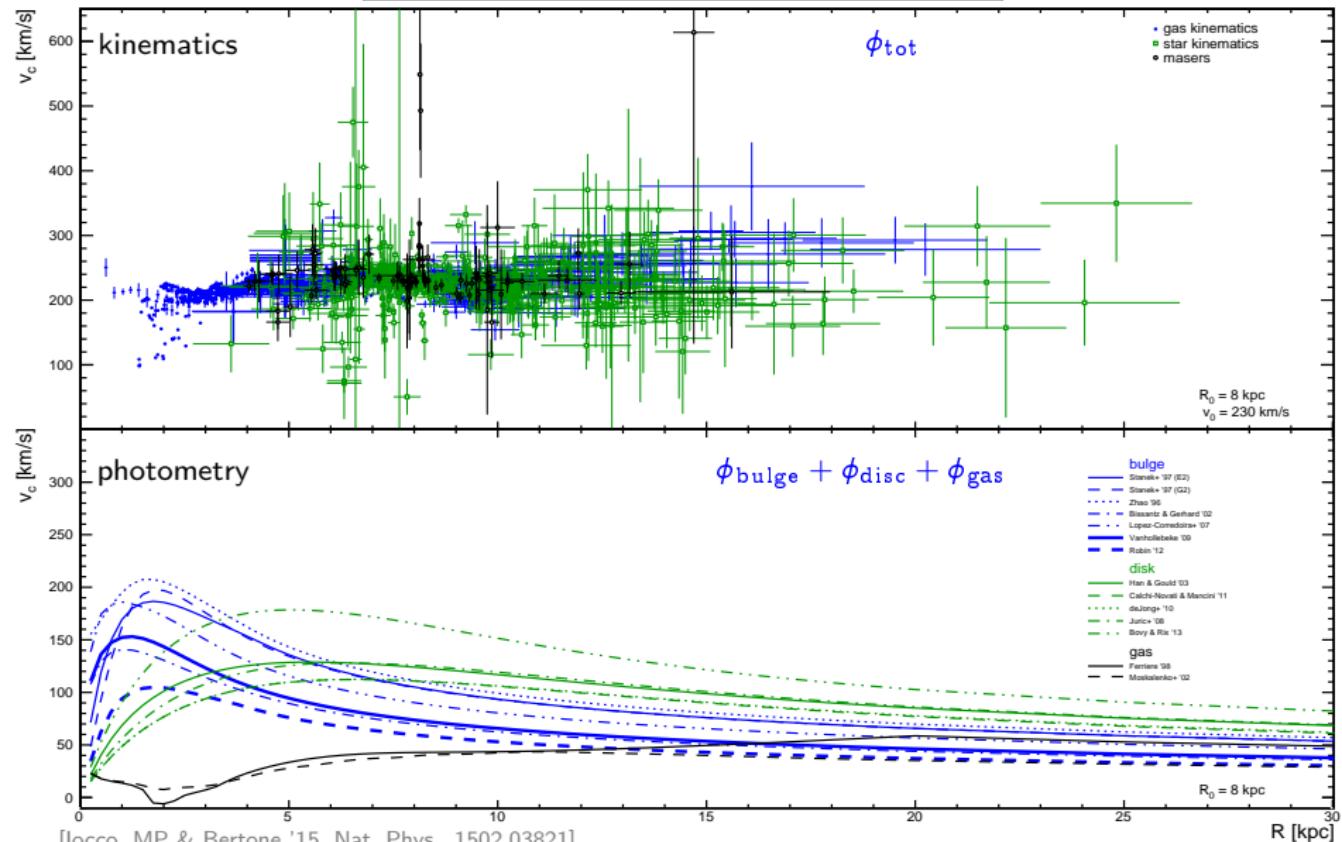


$$v_{\text{los}}^{\text{ISR}} = \left( \frac{v_c(R')}{R'/R_0} - v_0 \right) \cos b \sin \ell$$



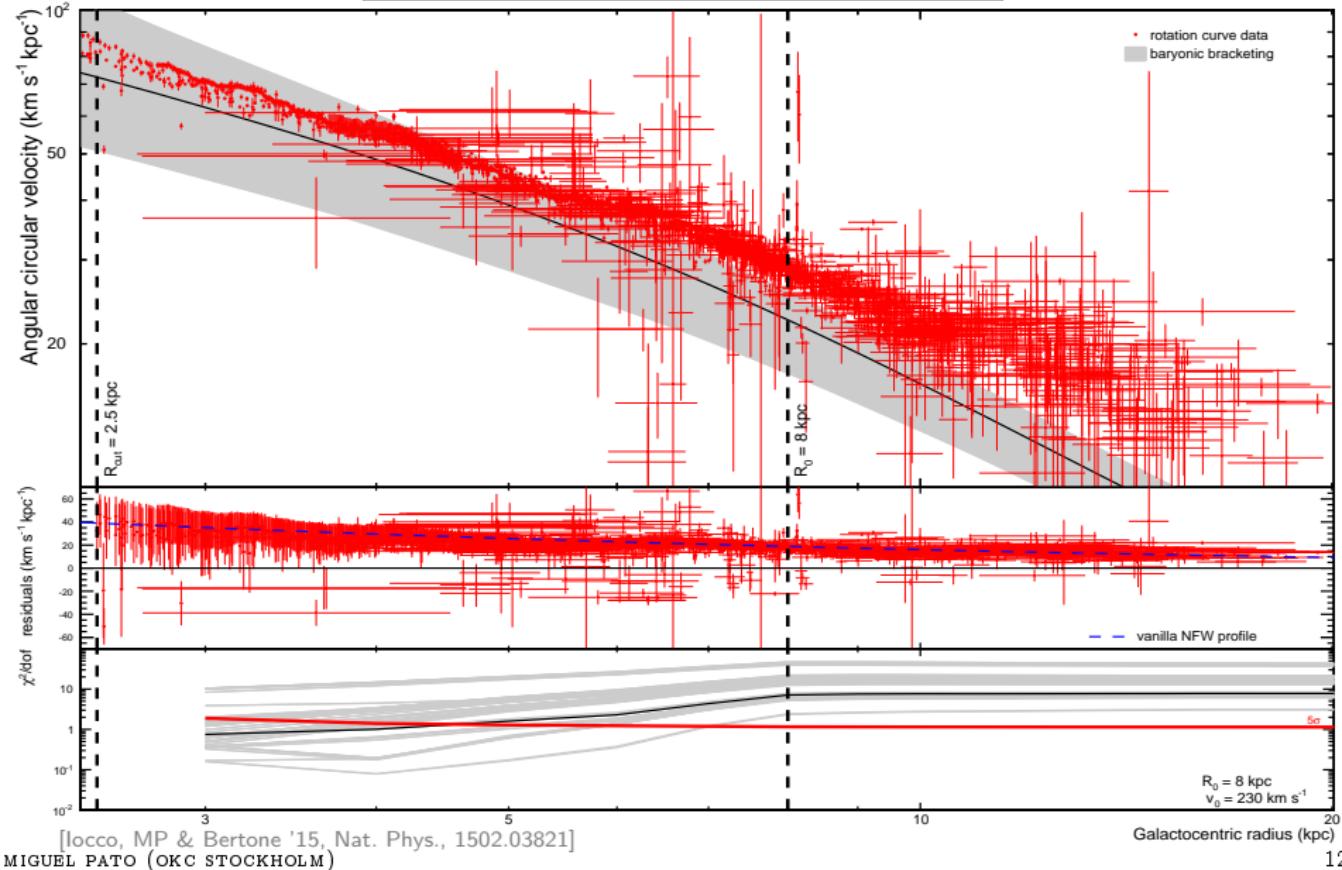
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## 2. DARK MATTER: LOCALISE OR GLOBALISE?

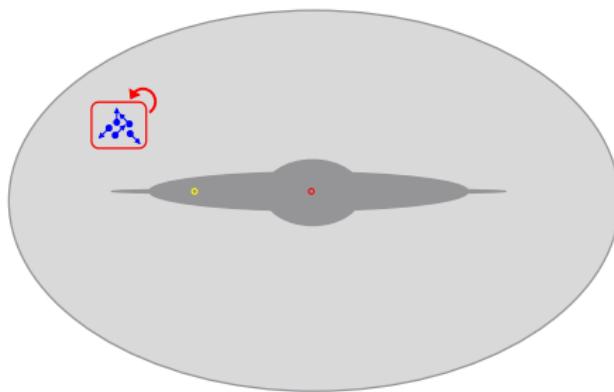
local methods

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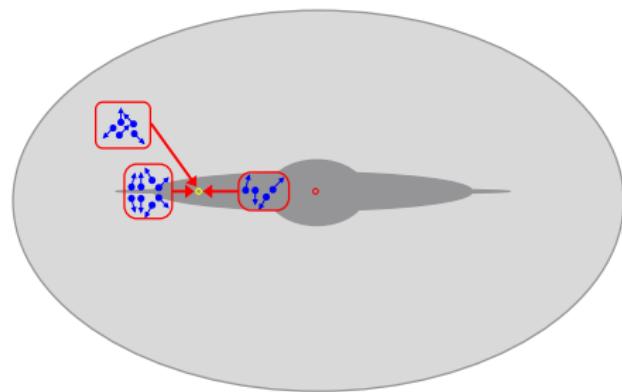
aim: use data from a patch of the sky to derive dynamics there.

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## 2. LOCAL METHODS

In a galaxy star encounters are rare and stars feel on average the smooth gravitational potential. We can therefore treat a set of stars as a collisionless gas and apply the collisionless Boltzmann equation, whose first momentum gives the **Jeans equations**:

$$-\rho_s \frac{\partial \phi_{\text{tot}}}{\partial x_j} = \frac{\partial(\rho_s \bar{v}_j)}{\partial t} + \sum_i \frac{\partial(\rho_s \bar{v}_i \bar{v}_j)}{\partial x_i} , \quad j = 1, 2, 3 \text{ (cartesian)} .$$

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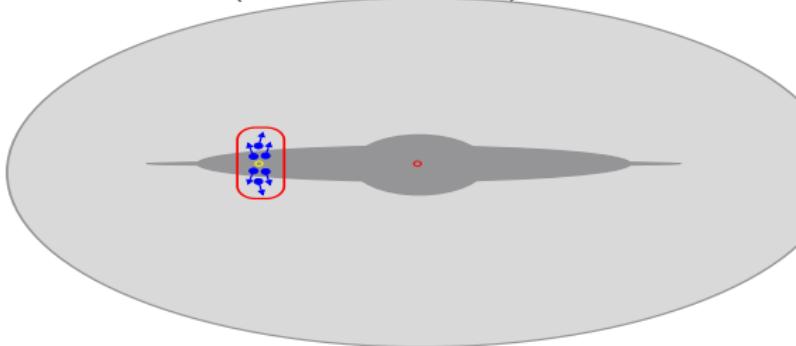
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$$-4\pi G \rho_{\text{tot}} = \frac{\partial}{\partial z} \left( \frac{1}{\rho_s} \frac{\partial(\rho_s \bar{v}_z^2)}{\partial z} \right)$$



This is the so-called Oort limit.

[Oort '32]

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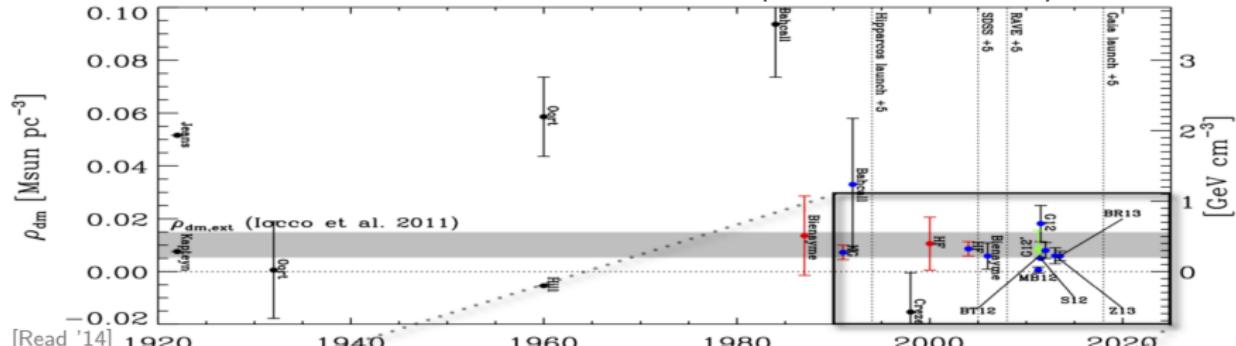
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$$[ \text{see talk by H. Silverwood} ] \quad F_z = \frac{1}{\rho_s} \left( \frac{\partial(\rho_s \bar{v}_R \bar{v}_z)}{\partial R} + \frac{\partial(\rho_s \bar{v}_z^2)}{\partial z} \right) + \frac{\bar{v}_R \bar{v}_z}{R}$$



[Read '14], [Biennemeier '87, Kuijken & Gilmore '89, Creze+ '98, Holmberg & Flynn '00, Garbari+ '11 '12, Smith+ '12, Zhang+ '13]

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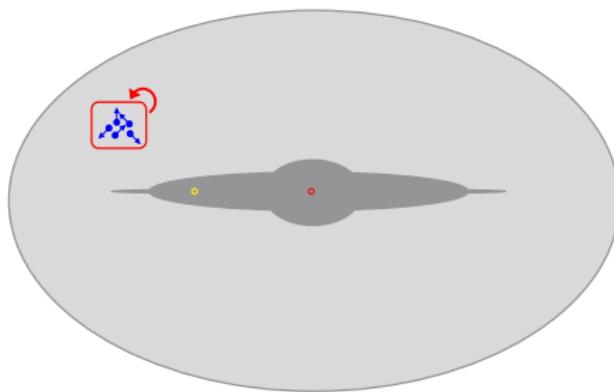
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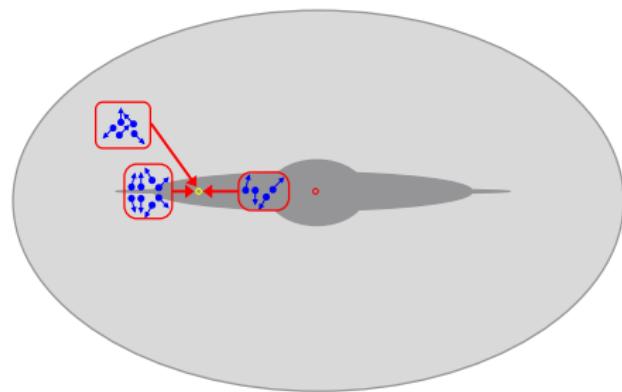
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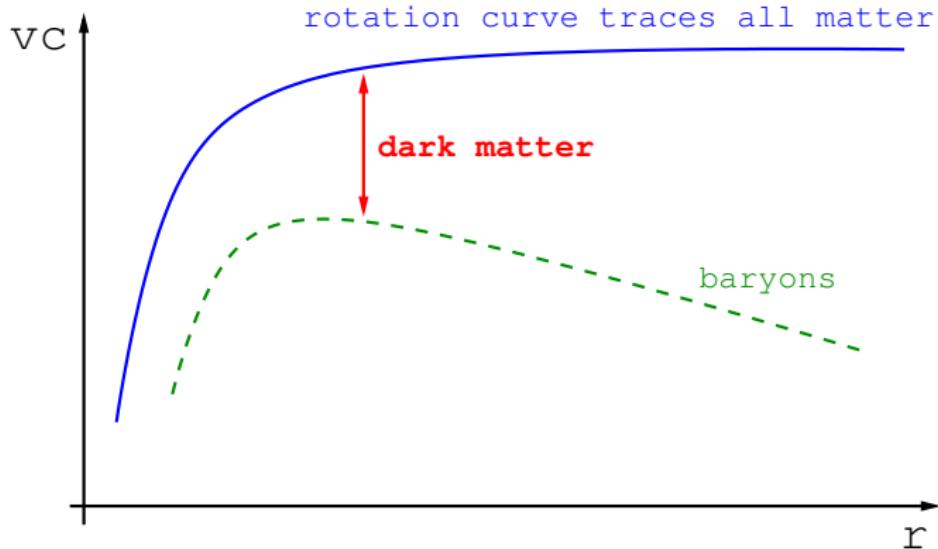


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## 2. GLOBAL METHODS

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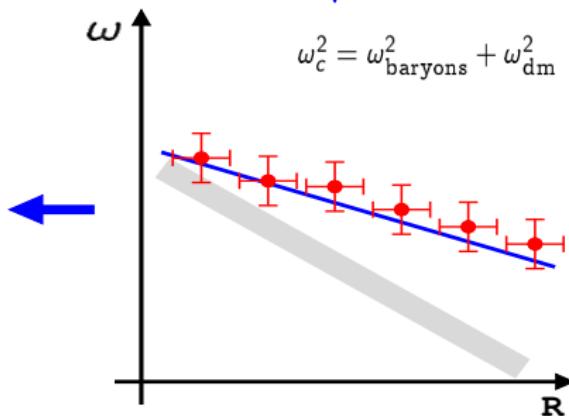
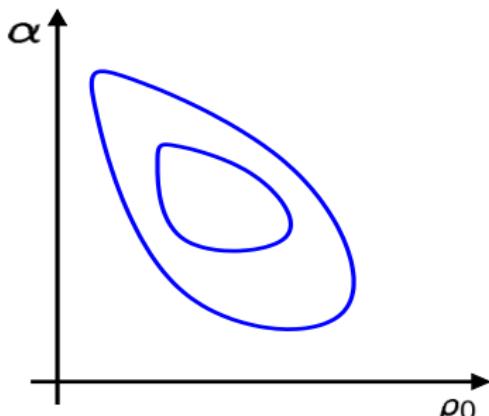
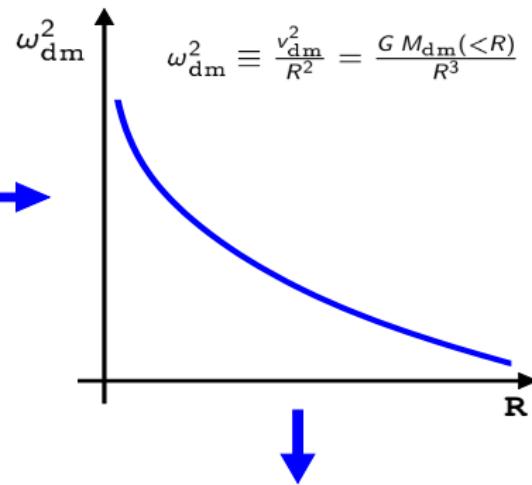
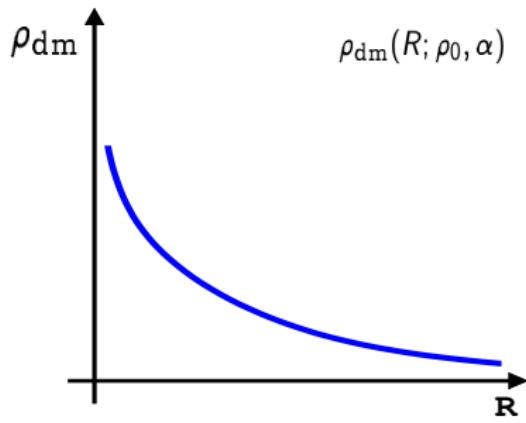


$$v_c^2 = v_b^2 + v_{\text{dm}}^2$$

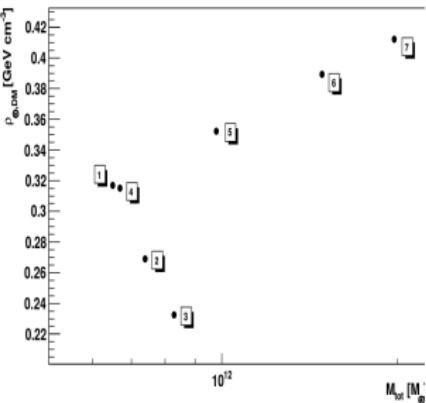
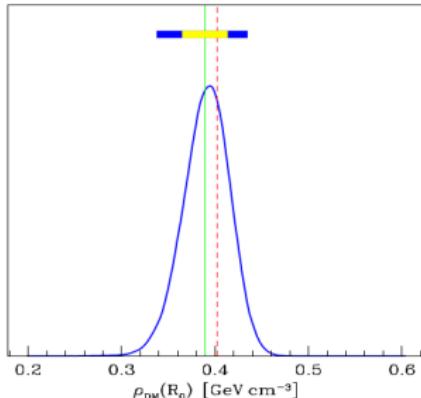
$$v_{\text{dm}}^2 \stackrel{\text{sph.}}{=} G M_{\text{dm}}() / r \rightarrow \rho_{\text{dm}}$$

[Dehnen & Binney '98, Sofue+ '09, Catena & Ullio '10, Weber & de Boer '10, Salucci+ '10, McMillan '11, Iocco+ '11, Nesti & Salucci '13, Sofue '15]

## 2. PROFILE FITTING



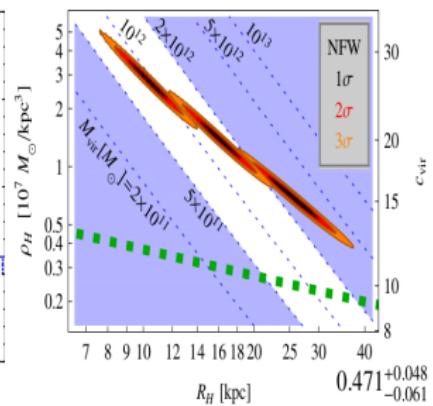
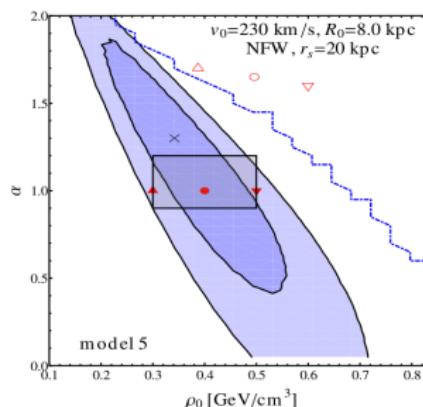
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$$\rho_\odot = (0.430 \pm 0.113_{(a_\odot)} \pm 0.096_{(r_\odot D)}) \frac{\text{GeV}}{\text{cm}^3}$$

[Salucci '10]

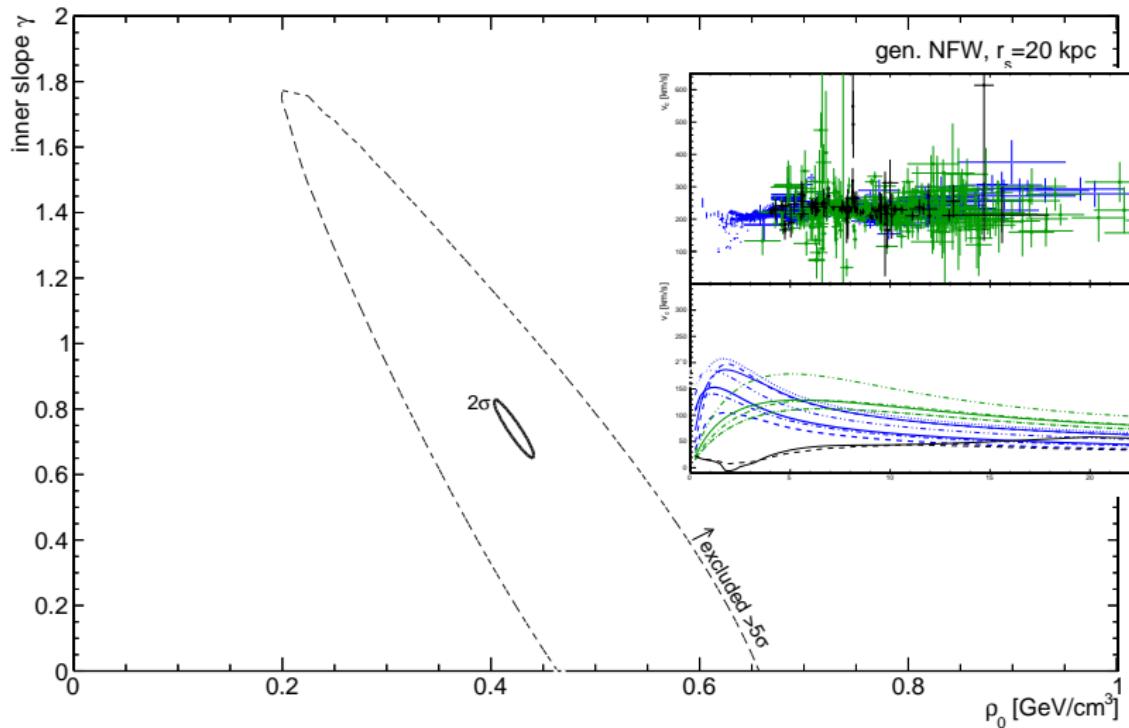
$$0.40 \pm 0.04 \text{ GeV cm}^{-3}$$



[McMillan '11]

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$$\rho_{\text{dm}} \propto (r/r_s)^{-\gamma} (1+r/r_s)^{-3+\gamma} \quad [\text{MP, Iocco \& Bertone '15, 1504.06324}]$$



NFW:  $\rho_0 = 0.420^{+0.021}_{-0.018}$  ( $2\sigma$ )

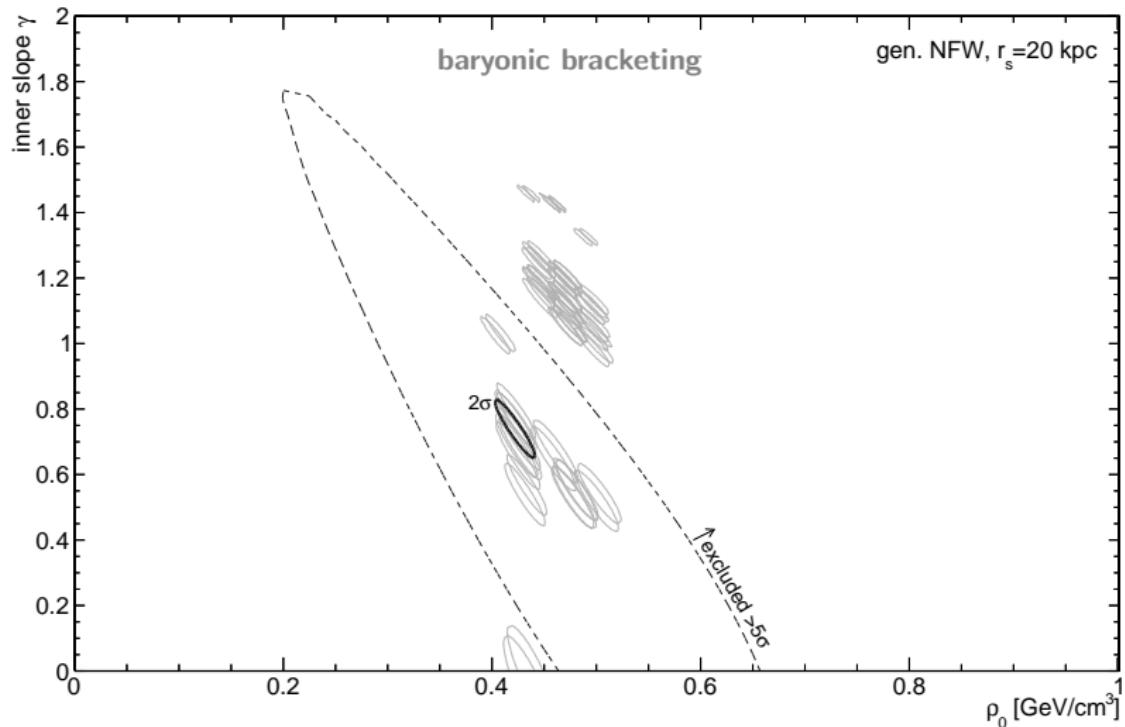
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Einasto:  $\rho_0 = 0.420^{+0.019}_{-0.021}$  ( $2\sigma$ )

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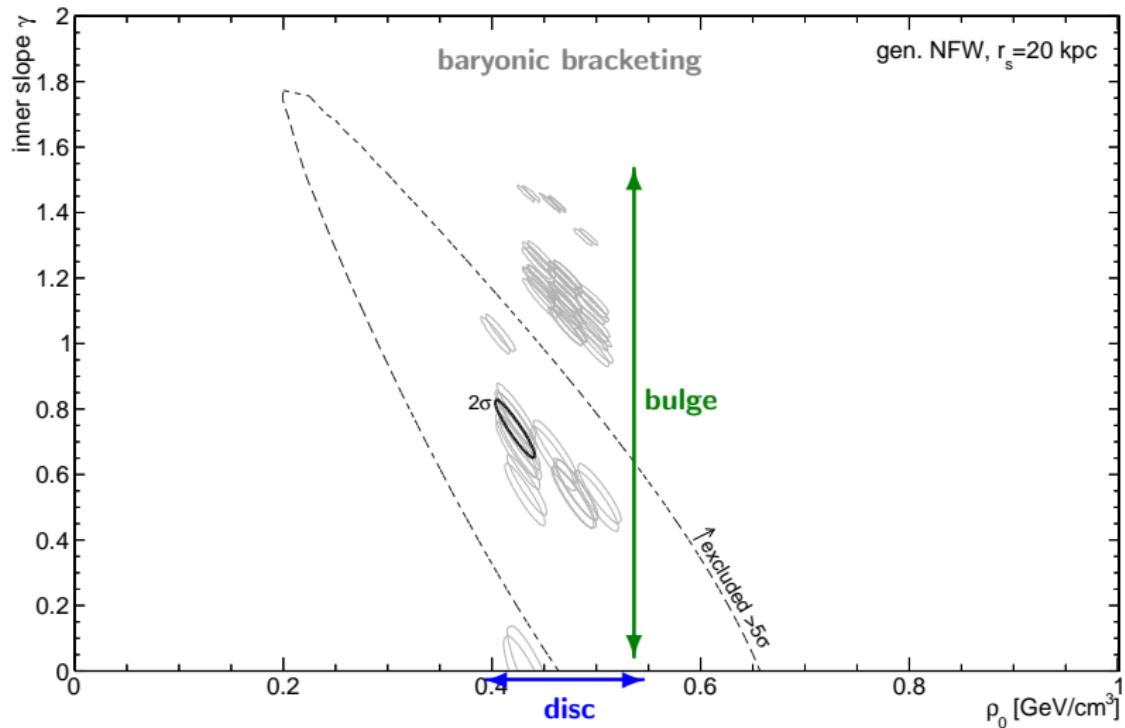


NFW:  $\rho_0 = 0.420^{+0.021}_{-0.018} (2\sigma) \pm 0.025 \text{ GeV}/\text{cm}^3$

Einasto:  $\rho_0 = 0.420^{+0.019}_{-0.021} (2\sigma) \pm 0.026 \text{ GeV}/\text{cm}^3$

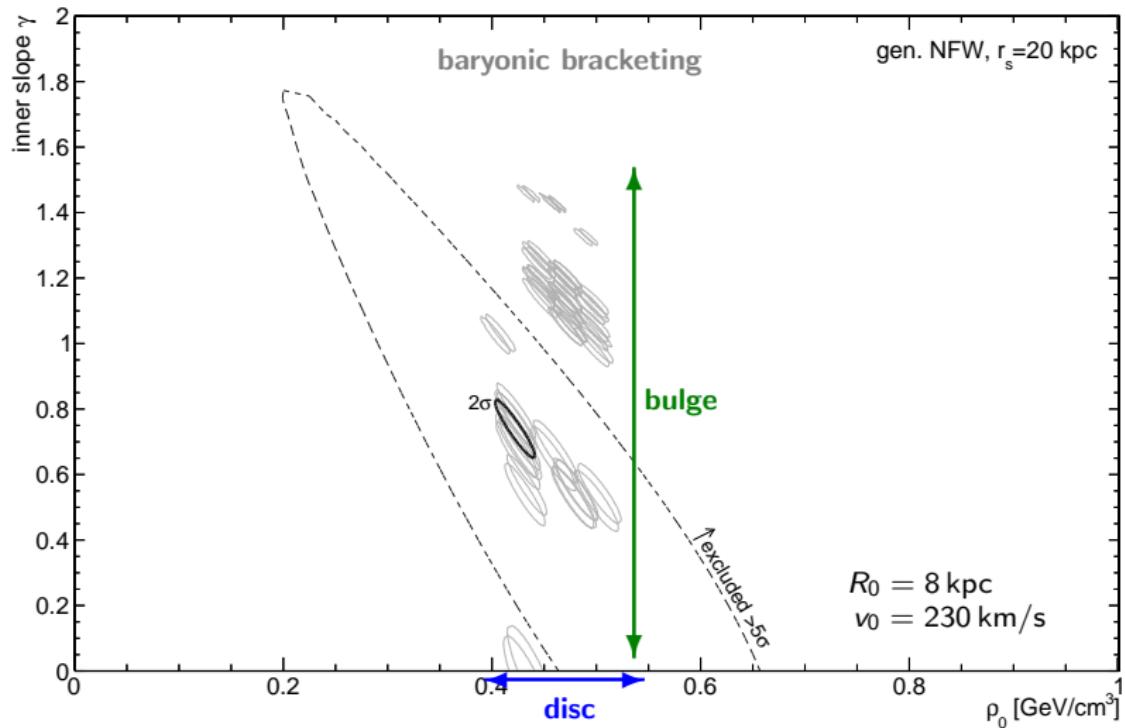
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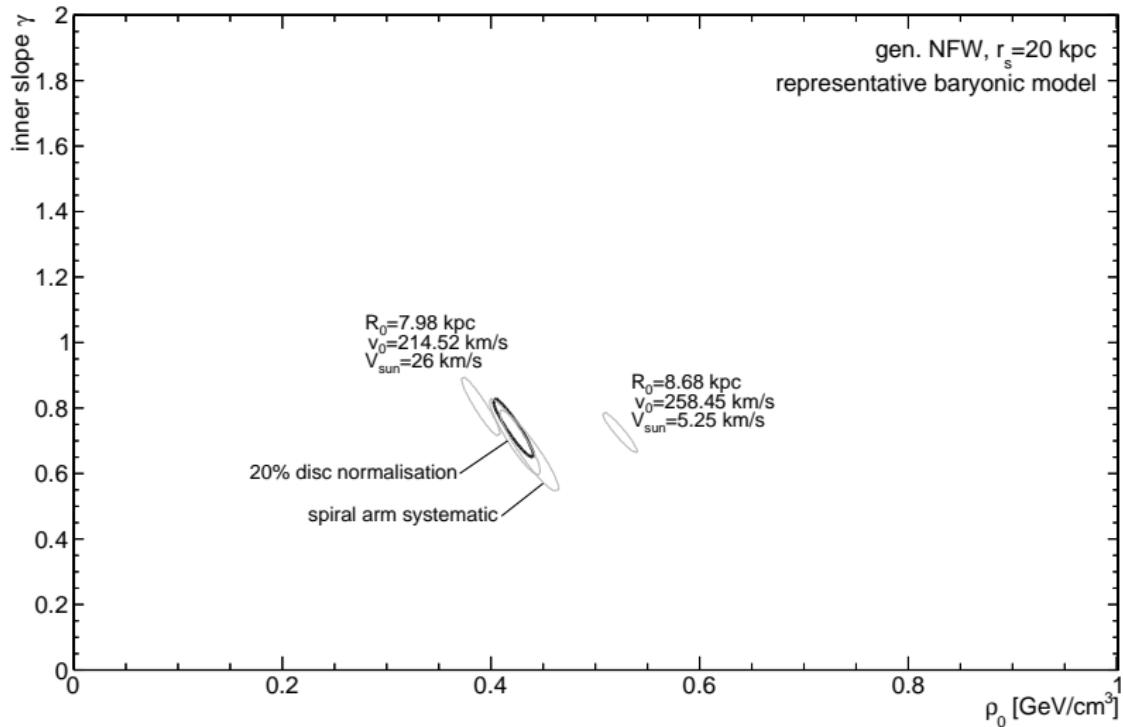
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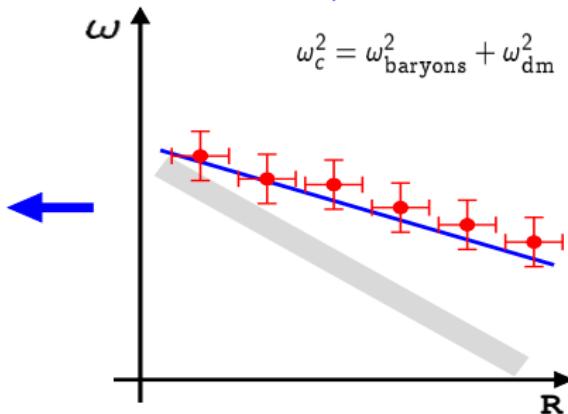
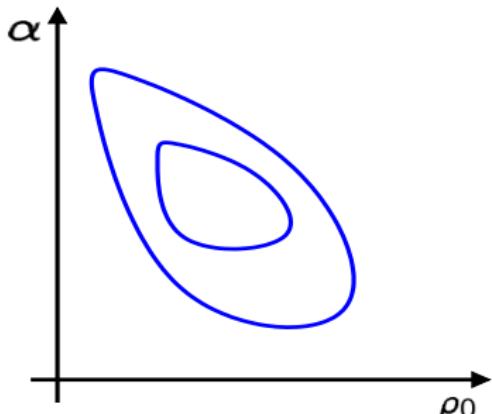
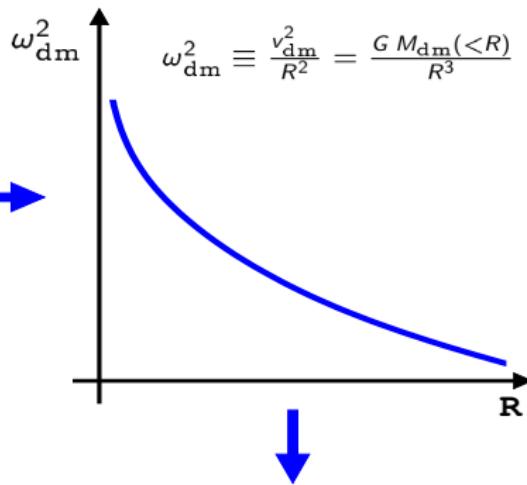
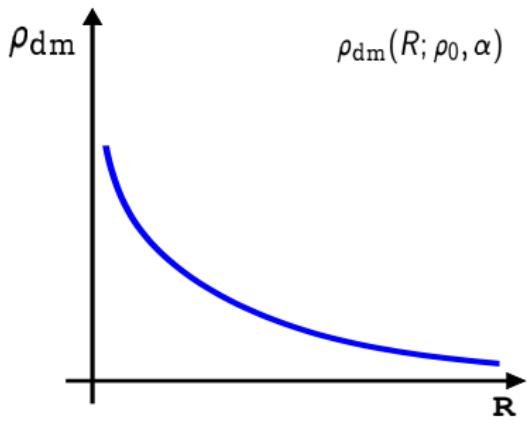


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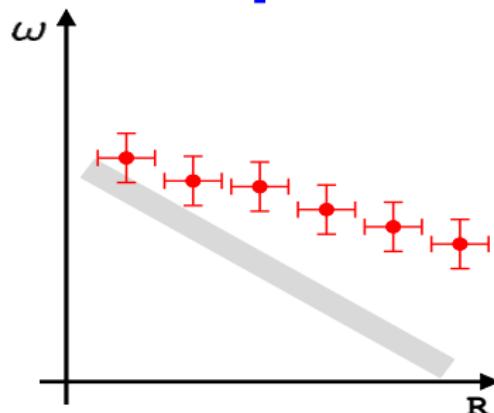
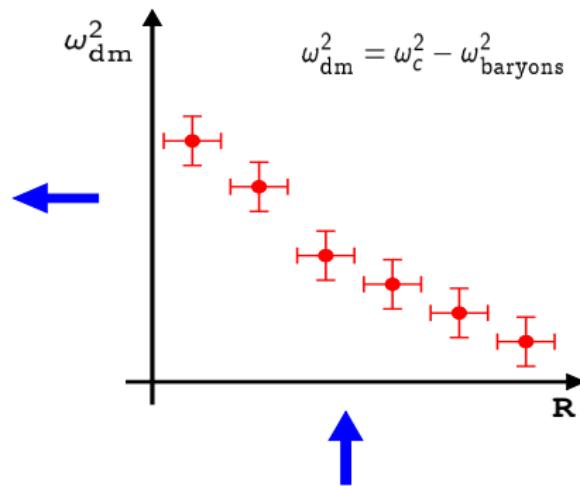
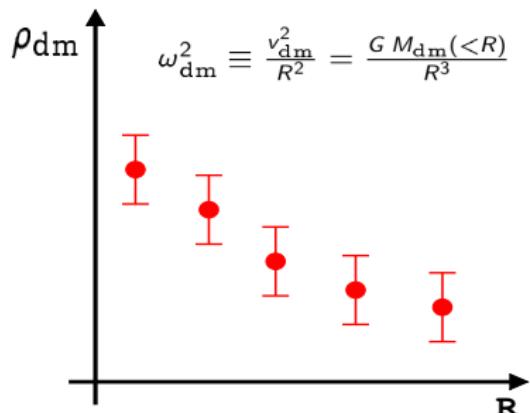
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## 2. PROFILE FITTING



## 2. PROFILE RECONSTRUCTION



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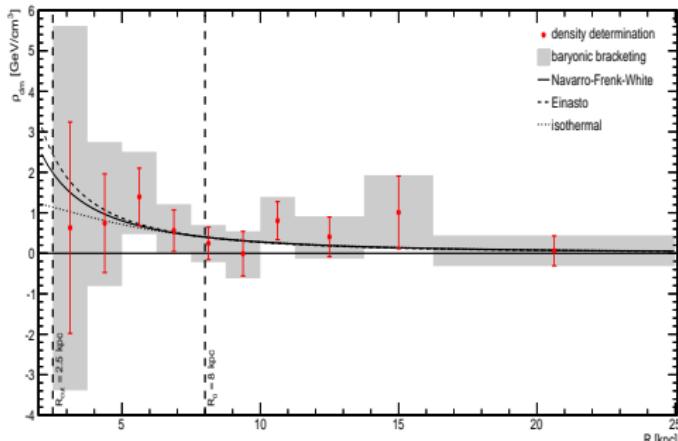
Let us take a spherical dark matter distribution. Then,

$$\omega_{\text{dm}}^2 = \omega_c^2 - \omega_{\text{baryons}}^2 \quad , \quad \omega_{\text{dm}}^2 = \frac{GM_{\text{dm}}(< R)}{R^3} = \frac{4\pi G}{R^3} \int_0^R dr r^2 \rho_{\text{dm}} .$$

Solving for  $\rho_{\text{dm}}$ ,

$$\rho_{\text{dm}}(R) = \frac{1}{4\pi G} \left( 3\omega_{\text{dm}}^2 + R \frac{d\omega_{\text{dm}}^2}{dR} \right) = \frac{\omega_{\text{dm}}^2}{4\pi G} \left( 3 + \frac{d \ln \omega_{\text{dm}}^2}{d \ln R} \right) .$$

That is, the deviation from  $\omega_{\text{dm}}^2 \propto R^{-3}$  (or  $v_{\text{dm}} \propto R^{-1/2}$ ) measures the dark matter density at each  $R$ . No assumption has been made on the functional form of  $\rho_{\text{dm}}(R)$ .



### 3. FUTURE DIRECTIONS?

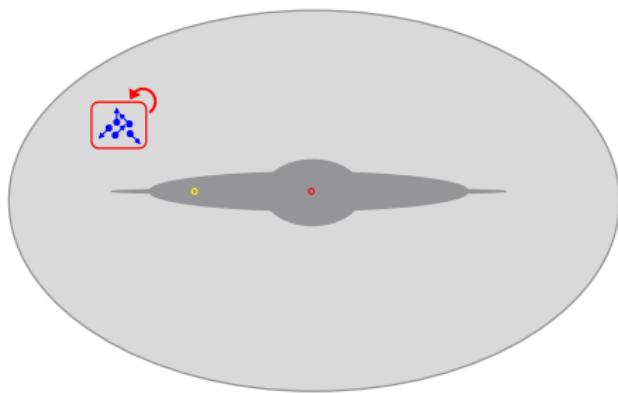
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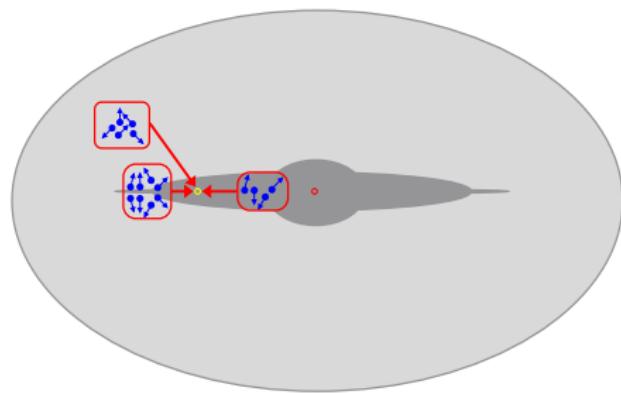
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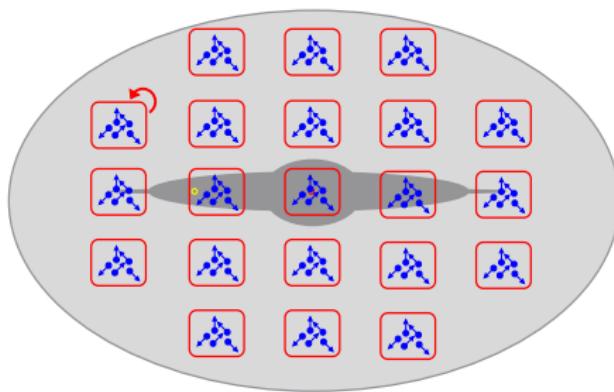
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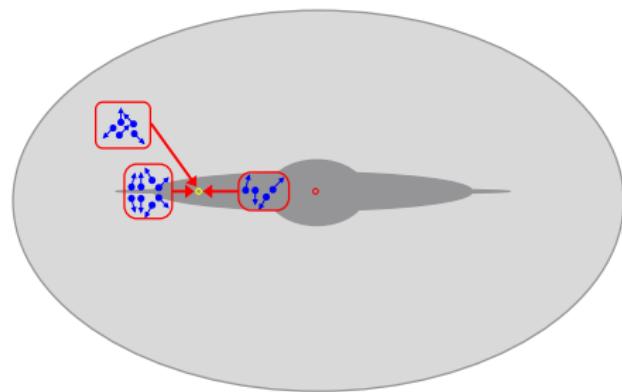
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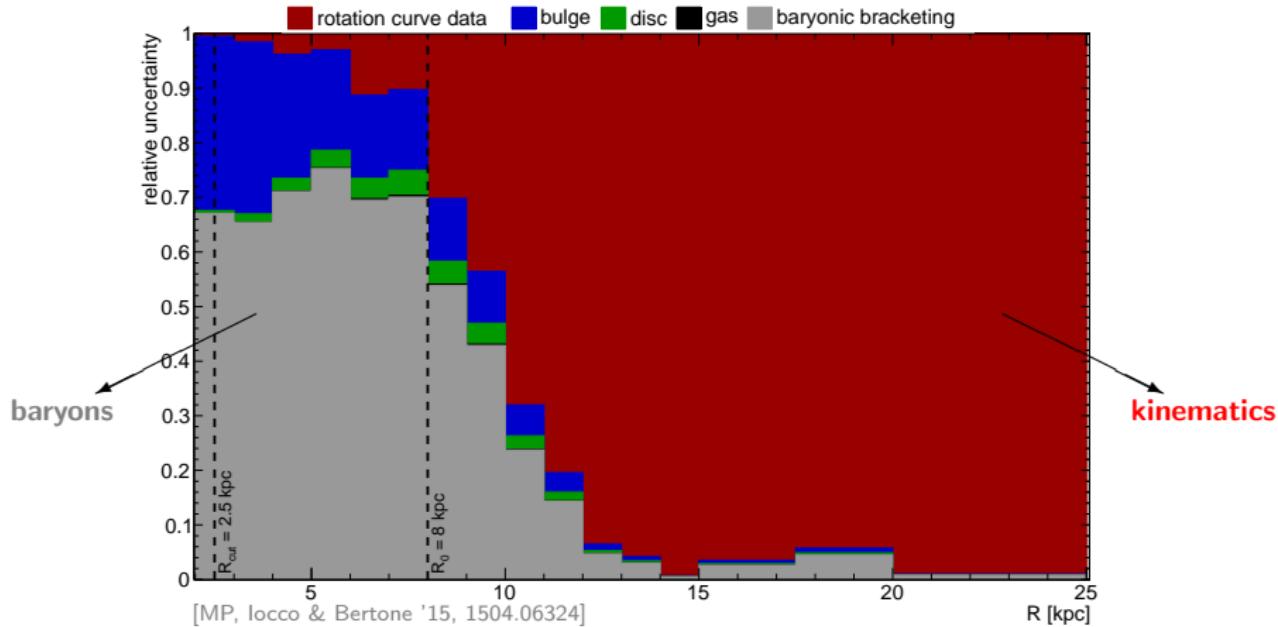
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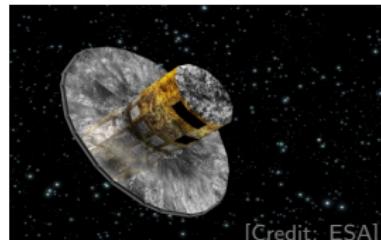
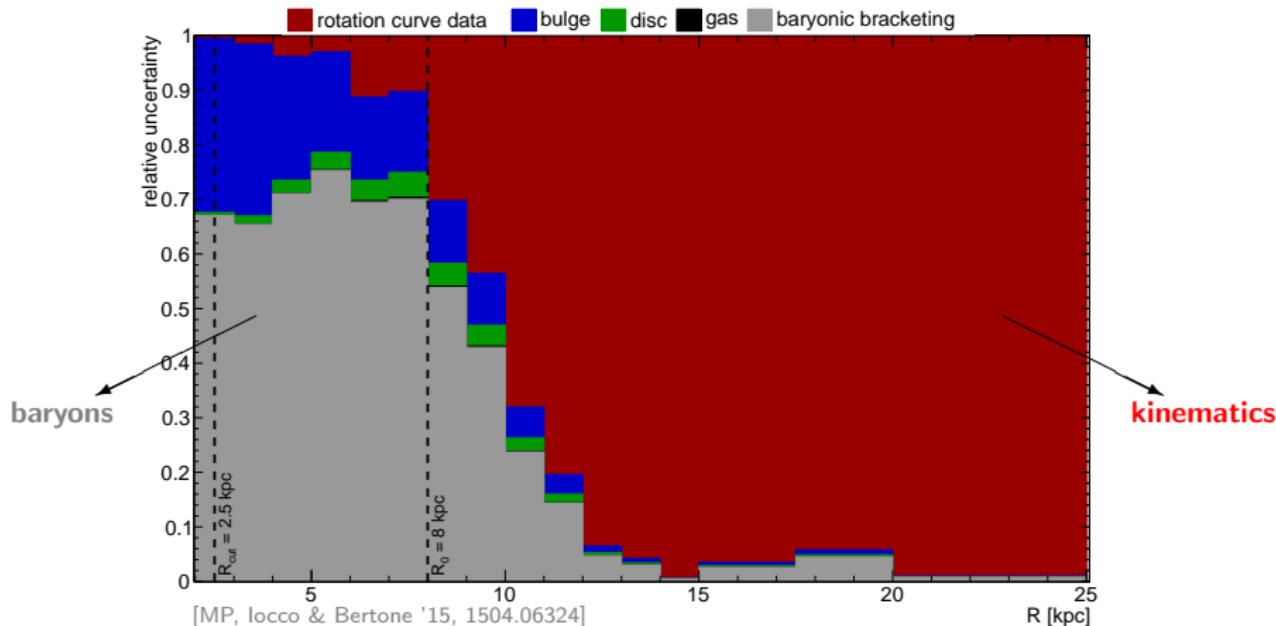
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### 3. FUTURE DIRECTIONS?



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[Credit: ESA]

Gaia

fact sheet

2013-2018

$\lambda = 320 - 1000 \text{ nm}$

$10^9$  stars  $G < 20 \text{ mag}$

parallax  $\pm 10 \mu\text{as}$

proper motion  $\pm 10 \mu\text{as/yr}$

radial velocity  $\pm 1 \text{ km/s}$

wish list

disc modelling

Oort's constants

local density

## 4. SUMMARY & CONCLUSION

photometry vs kinematics

photometry: tracks baryonic matter

kinematics: tracks total matter

kinematics – photometry: tracks dark matter

local vs global methods

local methods: robust but low precision

global methods: model-dependent but high precision

both are complementary

current uncertainties

inner Galaxy: baryons

outer Galaxy: kinematics

### bottomline

The distribution of dark matter in the Milky Way remains largely unconstrained,  
but Gaia and other surveys will shrink current uncertainties,  
leading to a new precision era in mapping dark matter in the Galaxy.

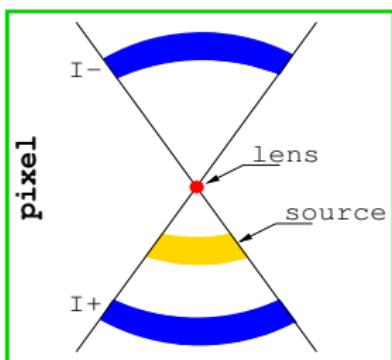
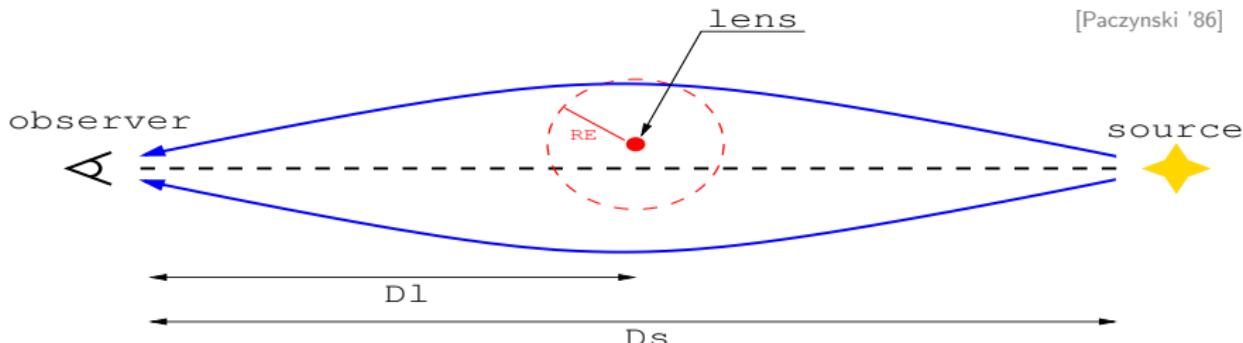
# BACKUP SLIDES

# 1. TOUR OF THE GALAXY: STELLAR BULGE

$$\rho_{\text{bulge}} = \rho_0 f(x, y, z)$$

normalisation  $\rho_0$

One possibility to normalise bulge models is to use microlensing.



Microlensing is simply a regime of gravitational lensing where the multiple images are not resolved.

$$\text{Einstein radius } R_E^2 = \frac{4GM_L}{c^2} D_L \left(1 - \frac{D_L}{D_s}\right)$$

$$\text{unresolved images } A(t) = \frac{u^2 + 2}{u\sqrt{u^2 + 4}}$$

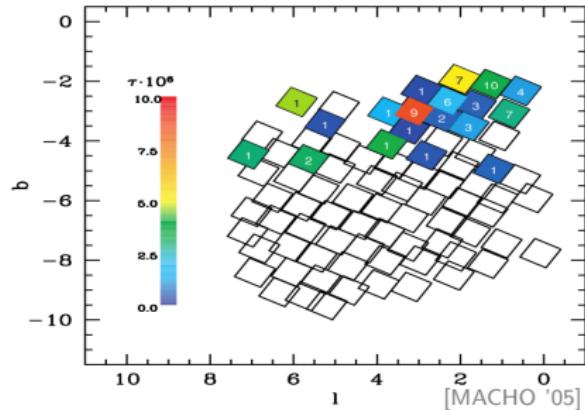
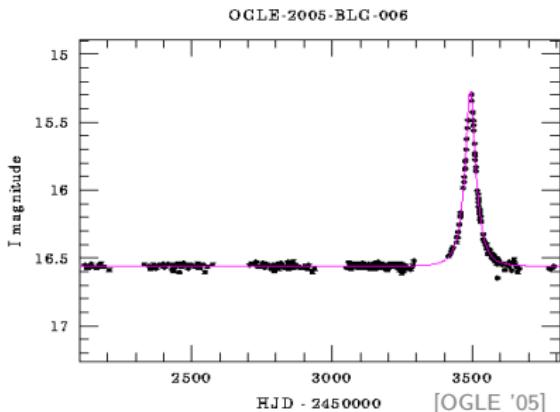
$$M_L \sim [10^{-6}, 10^2] M_\odot : t_E \sim \text{hr} - \text{days}$$

# 1. TOUR OF THE GALAXY: STELLAR BULGE

$$\rho_{\text{bulge}} = \rho_0 f(x, y, z)$$

normalisation  $\rho_0$

Microlensing in our Galaxy was predicted in 1986 and observed for the first time in 1993 by MACHO and EROS.



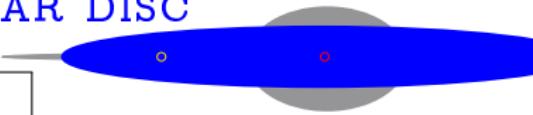
The microlensing optical depth, i.e. the probability for observing a microlensing event,

$$\tau = \int_0^{D_s} dD_I \int dM_I \left( \pi R_E^2 \right) \times \left( \frac{d^2 N_I}{dV dM_I} \right) = \frac{4\pi G}{c^2} \int_0^{D_s} dD_I \rho_I D_I \left( 1 - \frac{D_I}{D_s} \right)$$

is particularly convenient since it depends on  $\rho_I$  only, not on  $M_I$ .

$$\langle \tau \rangle = 2.17^{+0.47}_{-0.38} \times 10^{-6}, (\ell, b) = (1.50^\circ, -2.68^\circ) \quad [\text{MACHO '05}]$$

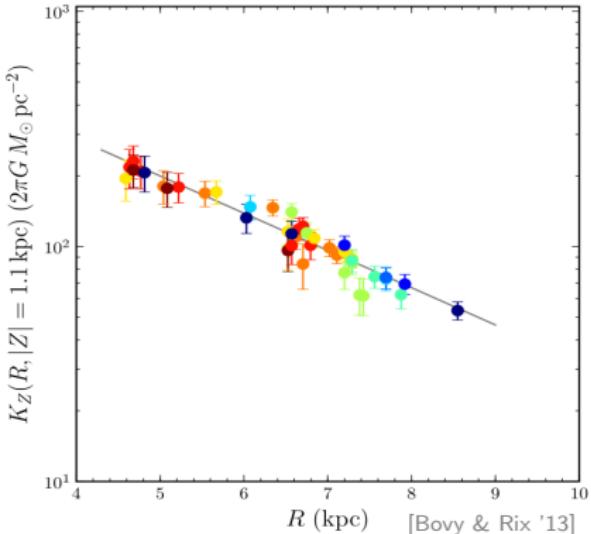
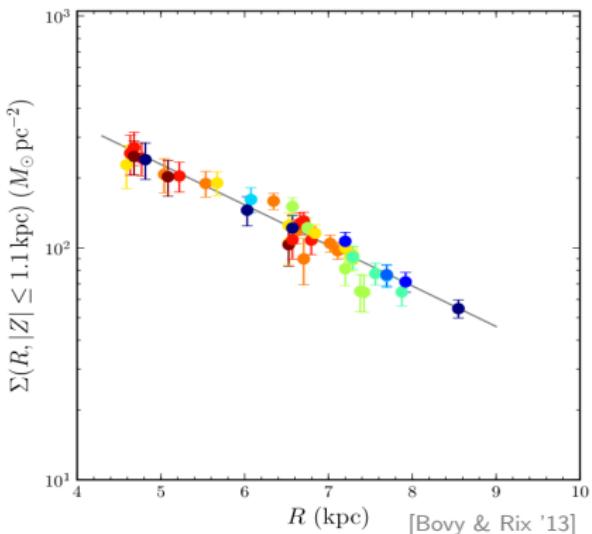
# 1. TOUR OF THE GALAXY: STELLAR DISC



$$\rho_{\text{disc}} = \rho_0 f(x, y, z)$$

normalisation  $\rho_0$

The normalisation of the stellar disc can be pinned down with the kinematics of specific stars.

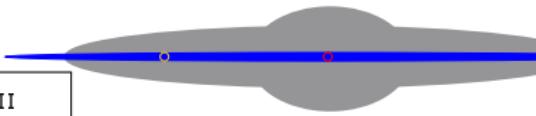


The latest dynamical measurement uses G dwarfs from SEGUE and fixes the stellar local surface density to

$$\Sigma_* = 38 \pm 4 M_\odot / \text{pc}^2 . \quad [\text{Bovy & Rix '13}]$$

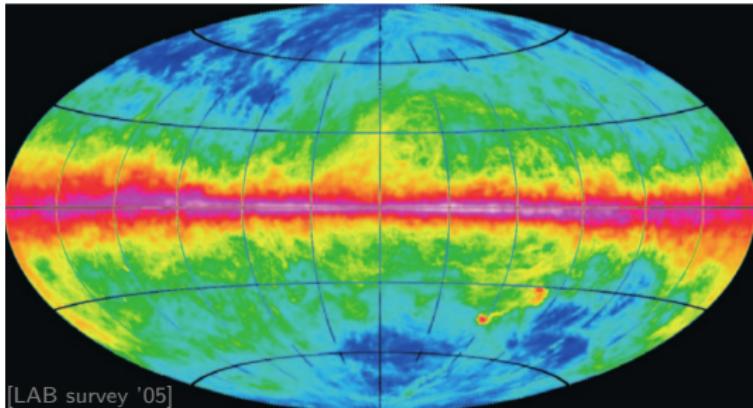
# 1. TOUR OF THE GALAXY: GAS

$$n_{\text{H}} = 2n_{\text{H}_2} + n_{\text{HI}} + n_{\text{HII}}$$

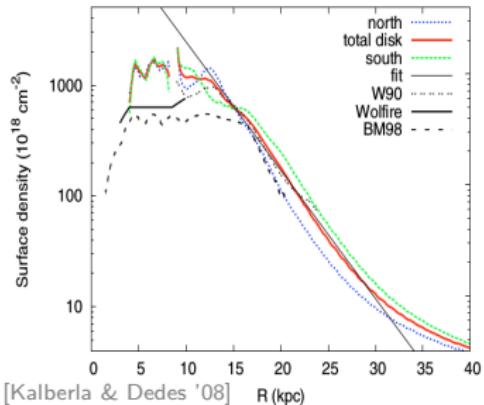


normalisation

The gas content is dominated by H<sub>2</sub> in the inner Galaxy and H I in the outer Galaxy.



[LAB survey '05]



For H<sub>2</sub>, the main normalisation uncertainty arises from the CO-to-H<sub>2</sub> factor,

$$X_{\text{CO}} = 0.25 - 1.0 \times 10^{20} \text{ cm}^{-2} \text{ K}^{-1} \text{ km}^{-1} \text{ s} \quad (r < 2 \text{ kpc})$$

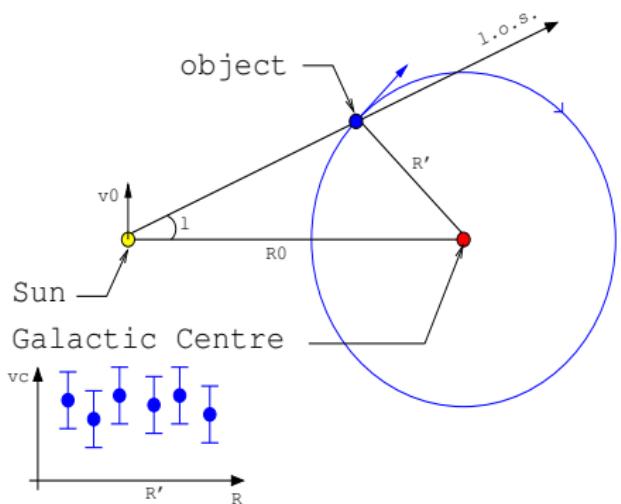
$$X_{\text{CO}} = 0.50 - 3.0 \times 10^{20} \text{ cm}^{-2} \text{ K}^{-1} \text{ km}^{-1} \text{ s} \quad (r > 2 \text{ kpc}) . \quad [\text{Ferrière+ '07, Ackermann '12}]$$

For H I, different surveys disagree by up to a factor  $\sim 2$  in the inner 15 kpc.

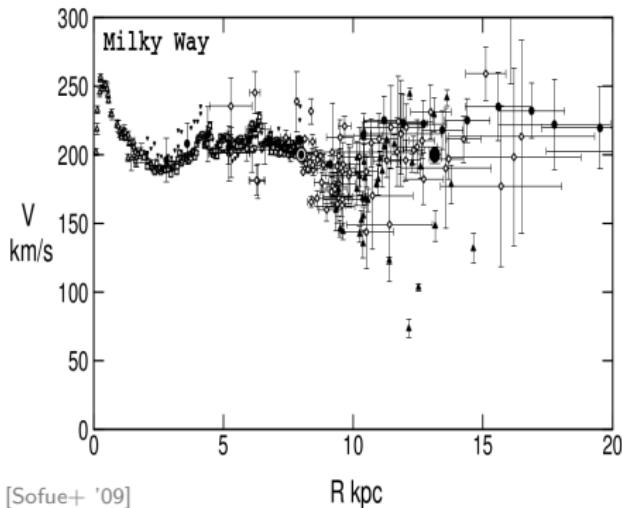
# 1. TOUR OF THE GALAXY: ROTATION CURVE

$$v_c^2 = r \frac{d\phi_{\text{tot}}}{dr} \stackrel{\text{sph.}}{=} \frac{GM_{\text{tot}}(< r)}{r}$$

Rotation curve tracers are young objects or regions that track galactic rotation. In external galaxies the only available tracer is the gas, while in our Galaxy we can use also some stars and star-forming regions. However, the case of our Galaxy is much more challenging due to our position.



$$v_{\text{los}}^{\text{ISR}} = \left( \frac{v_c(R')}{R'/R_0} - v_0 \right) \cos b \sin \ell$$



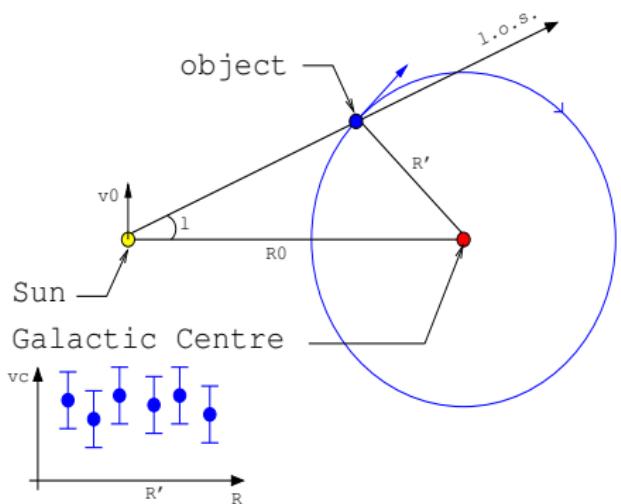
## Doppler shift

1. gas (21cm, H $\alpha$ , CO)
2. stars (H, He, O, ...)
3. masers (H<sub>2</sub>O, CH<sub>3</sub>OH, ...)

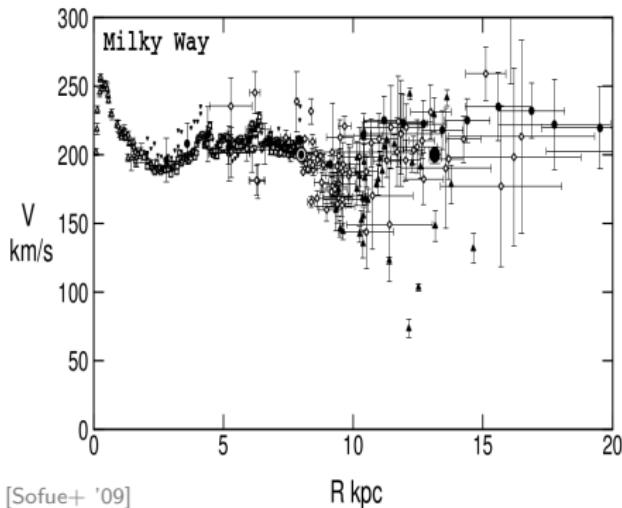
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distance

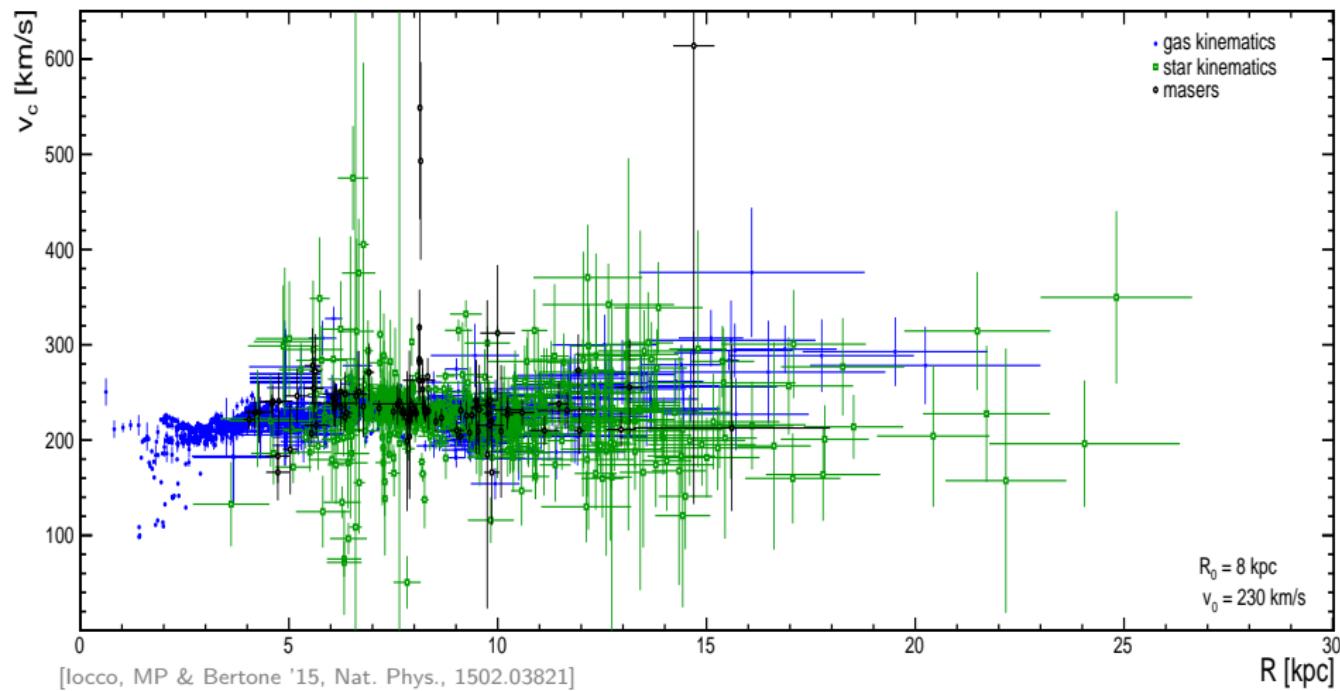
1. terminal velocities (gas)
2. photo-spectroscopy (stars)
3. parallax (masers)

# 1. TOUR OF THE GALAXY: ROTATION CURVE

optimised to  $R = 3 - 20$  kpc

2780 individual measurements

2174/506/100 from gas/stars/masers



# 1. TOUR OF THE GALAXY: ROTATION CURVE

gas

Object type	R [kpc]	quadrants	# objects
HI terminal velocities			
Fich+ '89	2.1 – 8.0	1,4	149
Malhotra '95	2.1 – 7.5	1,4	110
McClure-Griffiths & Dickey '07	2.8 – 7.6	4	701
HI thickness method			
Honma & Sofue '97	6.8 – 20.2	–	13
CO terminal velocities			
Burton & Gordon '78	1.4 – 7.9	1	284
Clemens '85	1.9 – 8.0	1	143
Knapp+ '85	0.6 – 7.8	1	37
Luna+ '06	2.0 – 8.0	4	272
HII regions			
Blitz '79	8.7 – 11.0	2,3	3
Fich+ '89	9.4 – 12.5	3	5
Turbide & Moffat '93	11.8 – 14.7	3	5
Brand & Blitz '93	5.2 – 16.5	1,2,3,4	148
Hou+ '09	3.5 – 15.5	1,2,3,4	274
giant molecular clouds			
Hou+ '09	6.0 – 13.7	1,2,3,4	30
open clusters			
Frinchaboy & Majewski '08	4.6 – 10.7	1,2,3,4	60
planetary nebulae			
Durand+ '98	3.6 – 12.6	1,2,3,4	79
stars			
classical cepheids			
Pont+ '94	5.1 – 14.4	1,2,3,4	245
Pont+ '97	10.2 – 18.5	2,3,4	32
carbon stars			
Demers & Battinelli '07	9.3 – 22.2	1,2,3	55
Battinelli+ '13	12.1 – 24.8	1,2	35
masers			
Reid+ '14	4.0 – 15.6	1,2,3,4	80
Honma+ '12	7.7 – 9.9	1,2,3,4	11
Stepanishchev & Bobylev '11	8.3	3	1
Xu+ '13	7.9	4	1
Bobylev & Bajkova '13	4.7 – 9.4	1,2,4	7

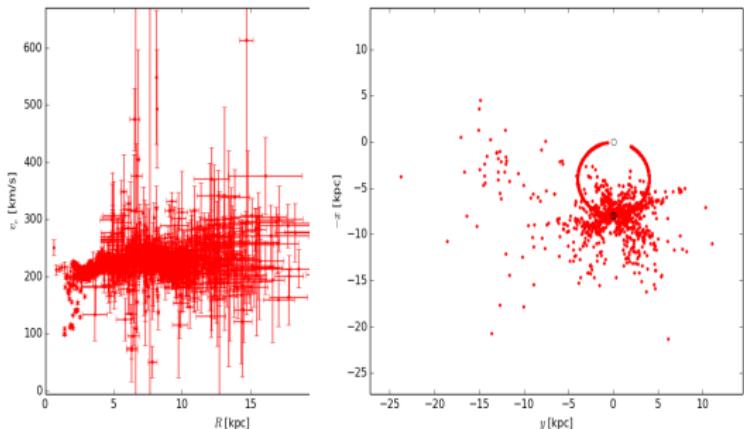
stars

masers

# 1. GALKIN

coming soon: galkin, public code in python

```
#####
# galkin, version 1.2, by Miguel Pato and Fabio Iocco
# Last update: MP 30 Jun 2015.
#####
# A tool to handle the available data on the rotation
#####
### read input ###
launching window...
```



enter input parameters

galactic parameters					
R0 [kpc]=	8.0	V0 [km/s]=	230.0	syst [km/s]=	0.0
Usun [km/s]=	11.10	Vsun [km/s]=	12.24	Wsun [km/s]=	07.25

data to use

- HI terminal velocities
  - Fich+ 89 (Table 2)
  - Malhotra 95
  - McClure-Griffiths & Dickey 07
- HI thickness
  - Honma & Sofue 97
- CO terminal velocities
  - Burton & Gordon 78
  - Clemens 85
  - Knapp+ 85
  - Luna+ 06
- HII regions
  - Blitz 79
  - Fich+ 89 (Table 1)
  - Turbide & Moffat 93
  - Brand & Blitz 93
  - Hou+ 09 (Table A1)
- giant molecular clouds
  - Hou+ 09 (Table A2)
- open clusters
  - Frinchaboy & Majewski 08
- planetary nebulae
  - Durand+ 98
- classical cepheids
  - Pont+ 94
  - Pont+ 97
- carbon stars
  - Demers & Battinelli 07
  - Battinelli+ 12
- masers
  - Reid+ 14
  - Honma+ 12
  - Stepanishchev & Bobylev 11
  - Xu+ 13
  - Bobylev & Bajkova 13

OK

user-friendly interface

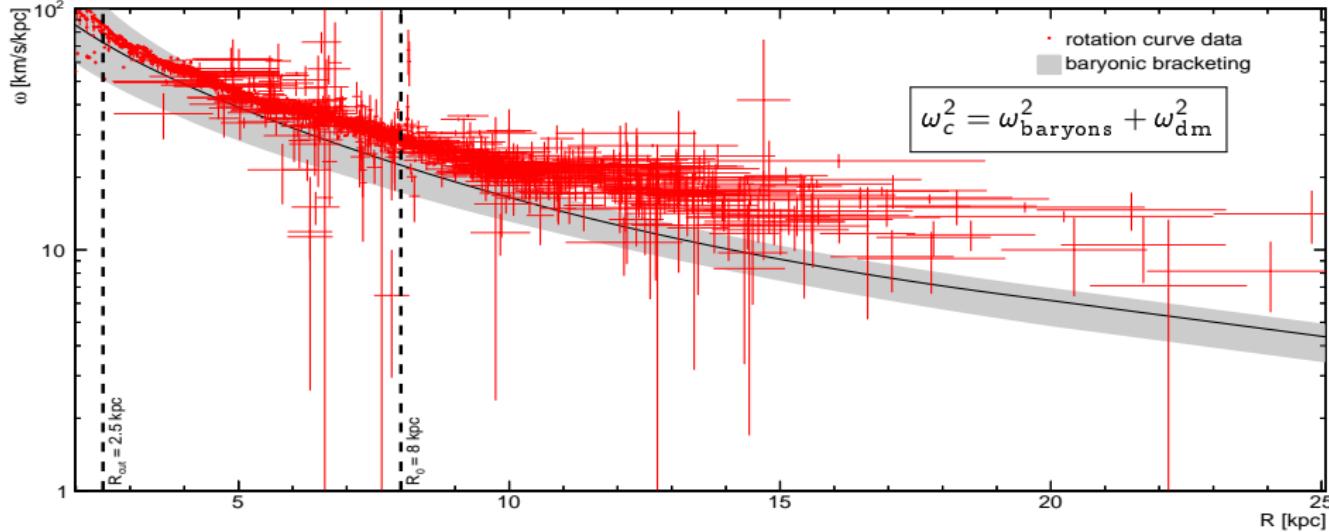
data & parameter selection

output rotation curve

output positional data

# 1. EVIDENCE FOR DARK MATTER

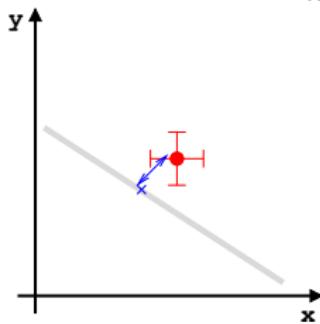
$$\phi_{\text{tot}} = \phi_{\text{bulge}} + \phi_{\text{disc}} + \phi_{\text{gas}} + \phi_{\text{dm}}$$



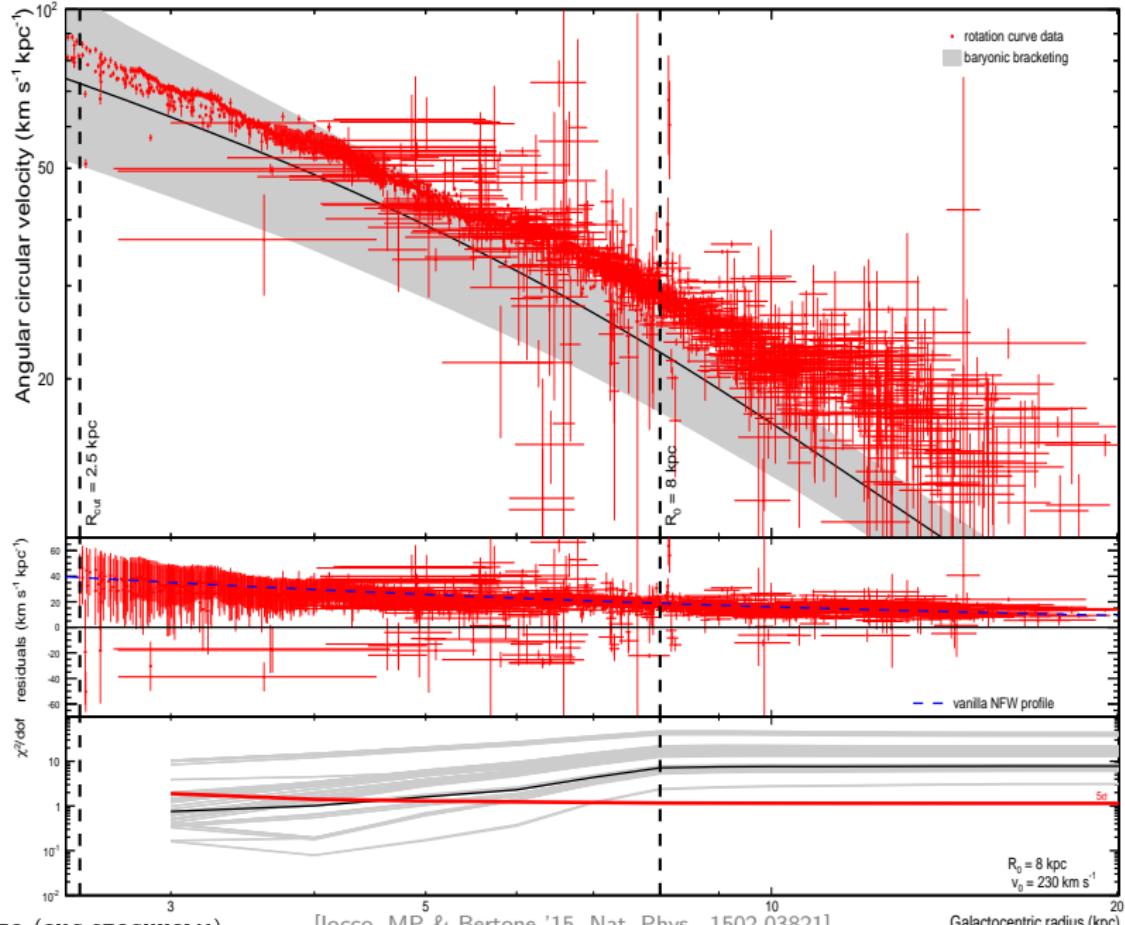
How bad is a baryon-only fit?

$$x = R/R_0 \quad y = \omega/\omega_0 - 1$$

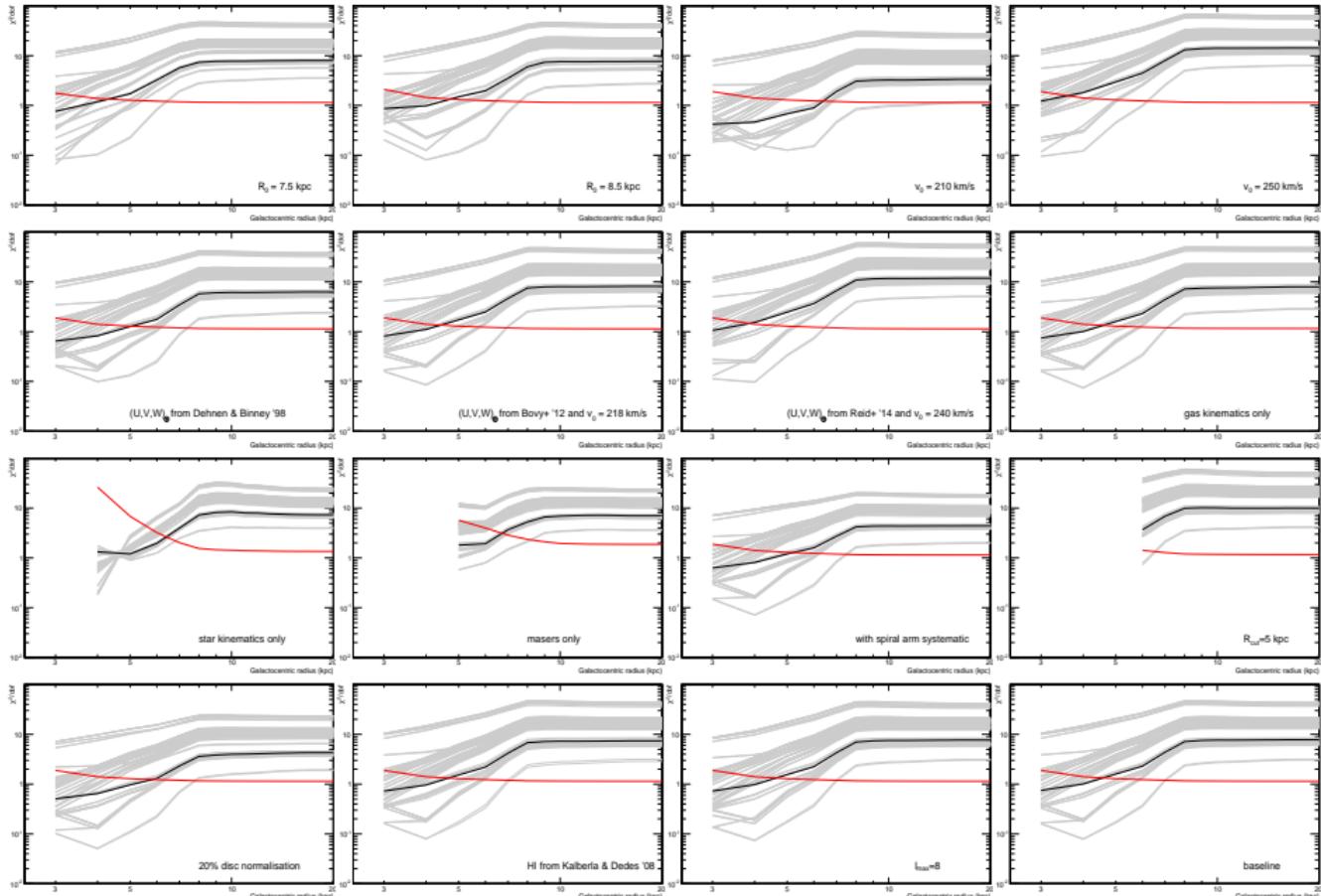
$$\chi^2 = \sum_{i=1}^N d_i^2 \equiv \sum_{i=1}^N \left[ \frac{(y_i - y_{\text{b},i})^2}{\sigma_{y,i}^2} + \frac{(x_i - x_{\text{b},i})^2}{\sigma_{x,i}^2} \right]$$



# 1. EVIDENCE FOR DARK MATTER



# 1. EVIDENCE FOR DARK MATTER



# 1. TOUR OF THE GALAXY

$$\phi_{\text{tot}} = \phi_{\text{bulge}} + \phi_{\text{disc}} + \phi_{\text{gas}} + \phi_{\text{dm}}$$

**dynamics**

traces total potential

$R \sim 0.1 - 30 \text{ kpc}$

rotation curve tracers

$R \sim 8 - 60 \text{ kpc}$

star population tracers

$R \sim 100 - 300 \text{ kpc}$

satellite kinematics

$R \sim 300+ \text{kpc}$

timing in Local Group

**"photometry"** traces individual baryonic components

bulge star counts, luminosity, microlensing

disc star counts, luminosity, stellar dynamics

gas emission lines, dispersion measure

# 1. TOUR OF THE GALAXY: STAR POPULATION

In a galaxy star encounters are rare and stars feel on average the smooth gravitational potential. We can therefore treat a set of stars as a collisionless gas and apply the collisionless Boltzmann equation, whose first momentum gives the **Jeans equations**:

$$-\rho_s \frac{\partial \phi_{\text{tot}}}{\partial x_j} = \frac{\partial(\rho_s \bar{v}_j)}{\partial t} + \sum_i \frac{\partial(\rho_s \bar{v}_i \bar{v}_j)}{\partial x_i} , \quad j = 1, 2, 3 \text{ (cartesian)} .$$

$\rho_s$ : star density

$v_j$ : velocity of stars

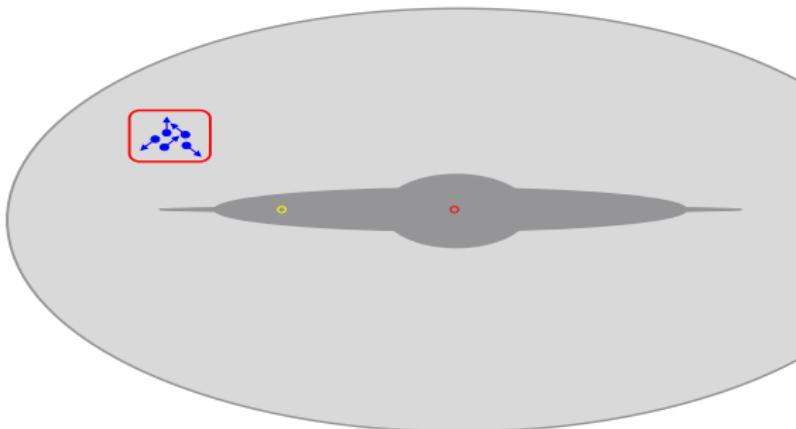
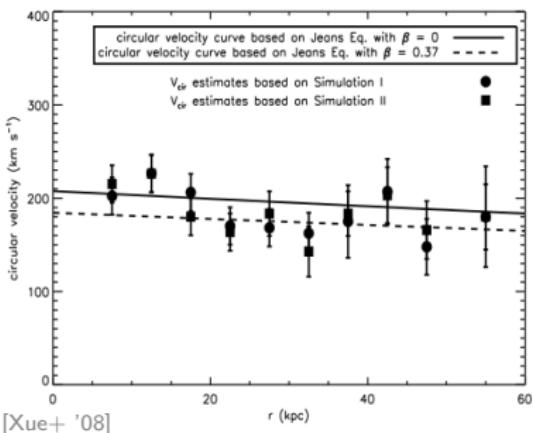
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[Sakamoto+ '03, Dehnen+ '06, Xue+ '08, Bhattacharjee+ '14, Kafle+ '14]

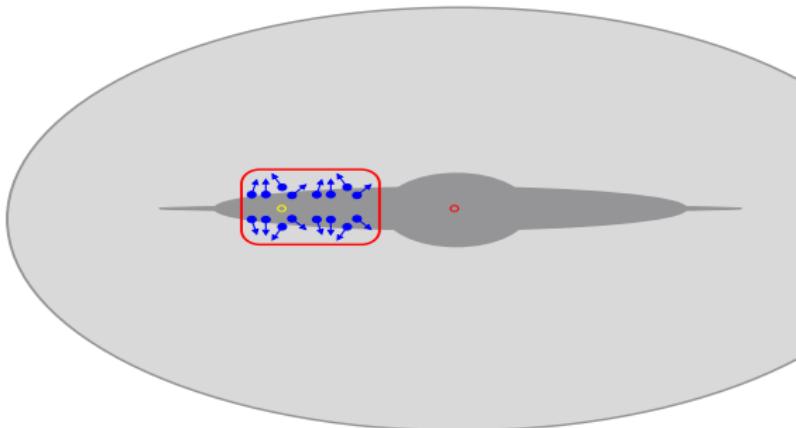
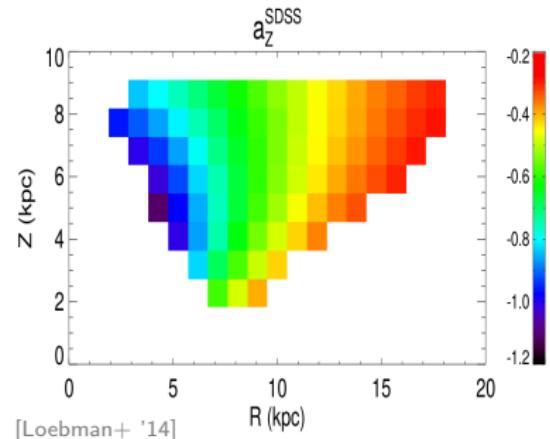
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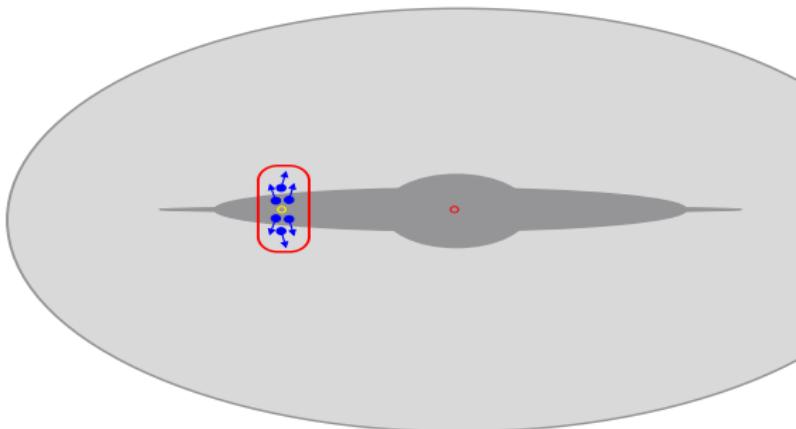
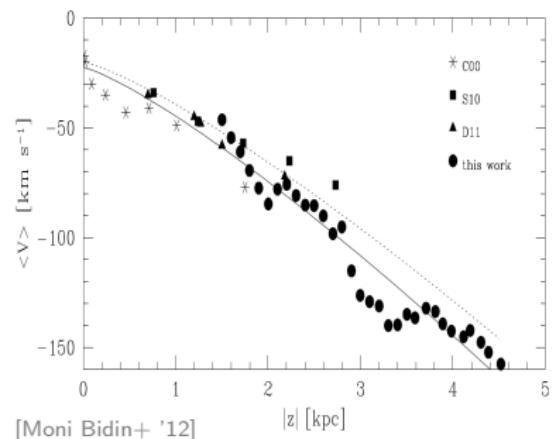
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[Kuijken & Gilmore '91, Holmberg & Flynn '04, Moni Bidin+ '12, Bovy & Tremaine '12, Moni Bidin+ '14]

## 2. DARK MATTER CONTENT

$$\phi_{\text{tot}} = \phi_{\text{bulge}} + \phi_{\text{disc}} + \phi_{\text{gas}} + \phi_{\text{dm}}$$

**dynamics**

traces total potential

- |                                |                         |
|--------------------------------|-------------------------|
| $R \sim 0.1 - 30 \text{ kpc}$  | rotation curve tracers  |
| $R \sim 8 - 60 \text{ kpc}$    | star population tracers |
| $R \sim 100 - 300 \text{ kpc}$ | satellite kinematics    |
| $R \sim 300+ \text{ kpc}$      | timing in Local Group   |

**"photometry"** traces individual baryonic components

- |       |   |
|-------|---|
| bulge | star counts, luminosity, microlensing     |
| disc  | star counts, luminosity, stellar dynamics |
| gas   | emission lines, dispersion measure        |

## 2. LOCAL METHODS

In a galaxy star encounters are rare and stars feel on average the smooth gravitational potential. We can therefore treat a set of stars as a collisionless gas and apply the collisionless Boltzmann equation, whose first momentum gives the **Jeans equations**:

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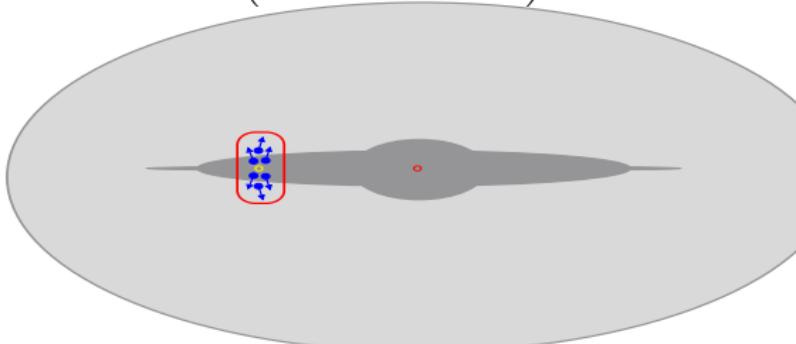
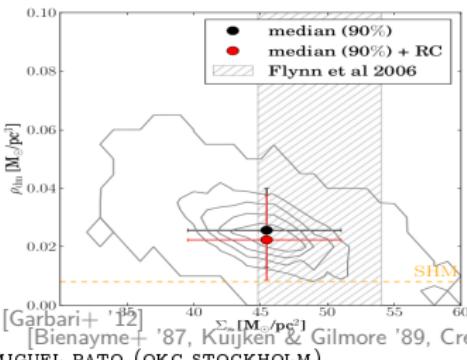
We can couple this to the **Poisson equation**:  $4\pi G \rho_{\text{tot}} = \nabla^2 \phi_{\text{tot}}$ .

$$\phi_{\text{tot}}(R, z) \quad \partial/\partial t \rightarrow 0 \quad -F_R = \partial \phi_{\text{tot}} / \partial R \quad -F_z = \partial \phi_{\text{tot}} / \partial z$$

$$-4\pi G \rho_{\text{tot}} = \frac{1}{R} \frac{\partial}{\partial R} (RF_R) + \frac{\partial F_z}{\partial z}$$

$$F_R = \frac{1}{\rho_s} \left( \frac{\partial(\rho_s \bar{v}_R^2)}{\partial R} + \frac{\partial(\rho_s \bar{v}_R \bar{v}_z)}{\partial z} \right) + \frac{\bar{v}_R^2 - \bar{v}_\phi^2}{R}$$

$$F_z = \frac{1}{\rho_s} \left( \frac{\partial(\rho_s \bar{v}_R \bar{v}_z)}{\partial R} + \frac{\partial(\rho_s \bar{v}_z^2)}{\partial z} \right) + \frac{\bar{v}_R \bar{v}_z}{R}$$



[Bienayme+ '87, Kuijken & Gilmore '89, Creze+ '98, Holmberg & Flynn '00, Garbari+ '11 '12, Smith+ '12, Zhang+ '13]  
MIGUEL PATO (OKC STOCKHOLM)

## 2. LOCAL METHODS

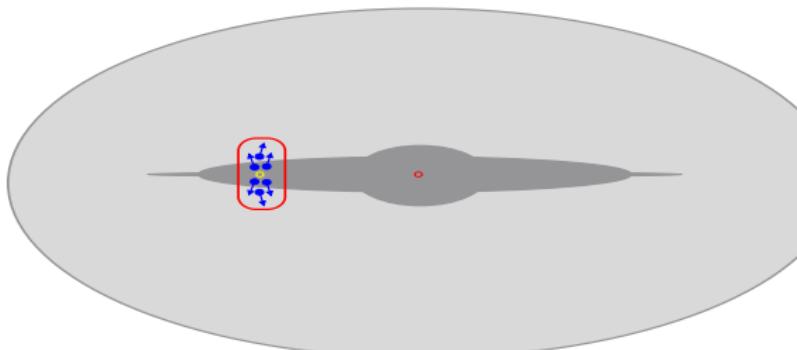
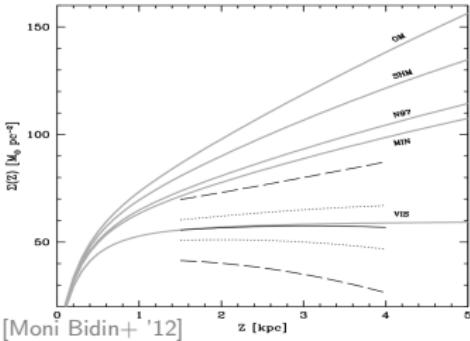
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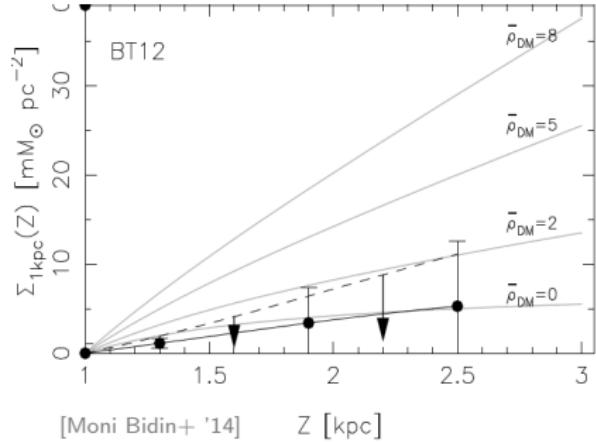
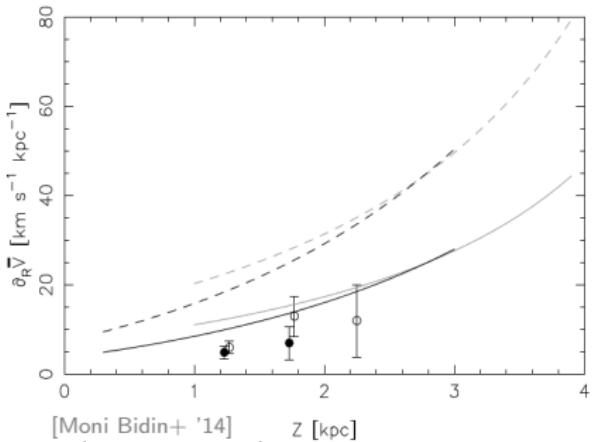
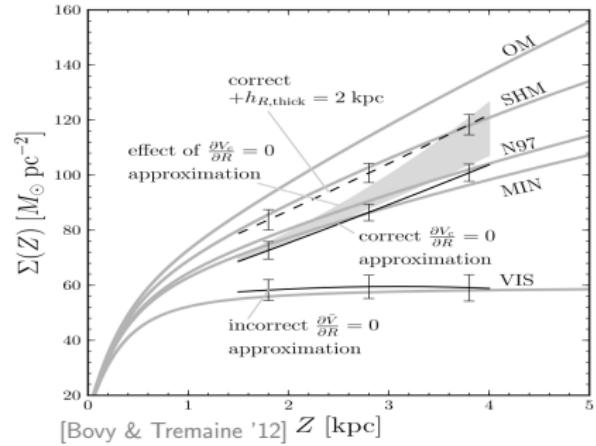
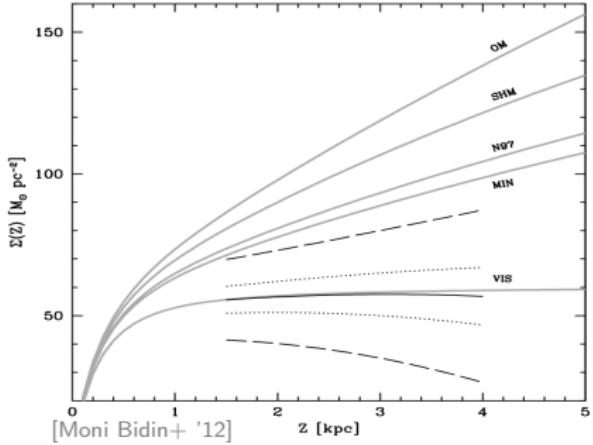
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$$-4\pi G \rho_{\text{tot}} = \frac{1}{R} \frac{\partial}{\partial R} (RF_R) + \frac{\partial F_z}{\partial z}$$
$$-4\pi G \Sigma_{\text{tot}}(z) = \int_{-z}^z dz \frac{1}{R} \frac{\partial}{\partial R} (RF_R) + F_z(z) - F_z(-z)$$



[Moni Bidin+ '12, Bovy & Tremaine '12, Moni Bidin+ '14]

## 2. LOCAL METHODS



## 2. LOCAL METHODS

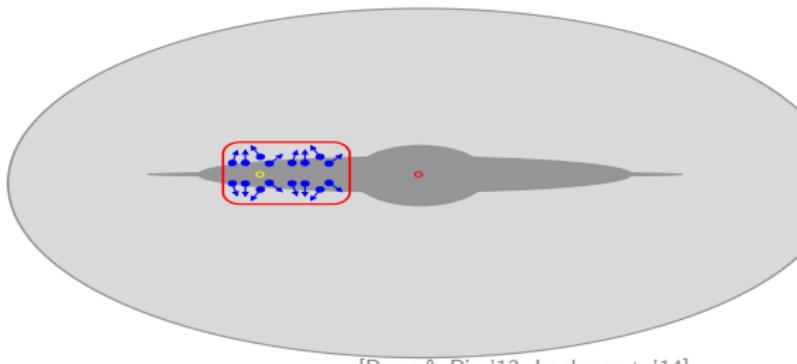
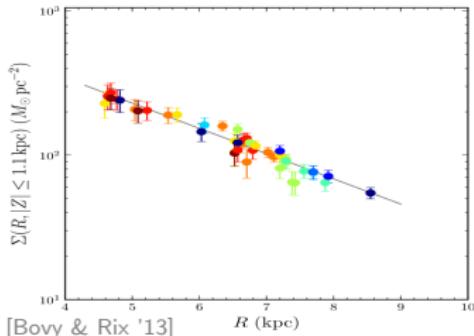
In a galaxy star encounters are rare and stars feel on average the smooth gravitational potential. We can therefore treat a set of stars as a collisionless gas and apply the collisionless Boltzmann equation, whose first momentum gives the **Jeans equations**:

$$-\rho_s \frac{\partial \phi_{\text{tot}}}{\partial x_j} = \frac{\partial(\rho_s \bar{v}_j)}{\partial t} + \sum_i \frac{\partial(\rho_s \bar{v}_i v_j)}{\partial x_i} , \quad j = 1, 2, 3 \text{ (cartesian)} .$$

We can couple this to the **Poisson equation**:  $4\pi G \rho_{\text{tot}} = \nabla^2 \phi_{\text{tot}}$ .

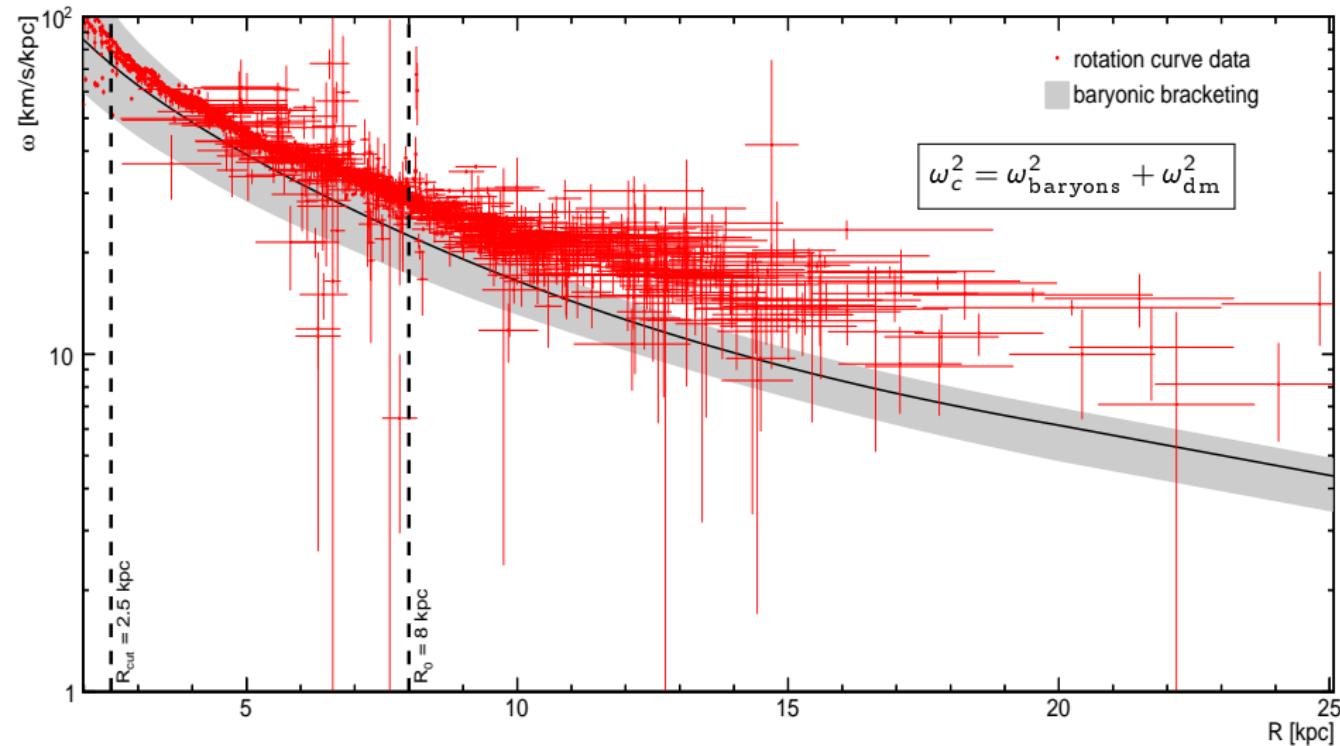
$$\phi_{\text{tot}}(R, z) \quad \partial/\partial t \rightarrow 0 \quad -F_R = \partial \phi_{\text{tot}} / \partial R \quad -F_z = \partial \phi_{\text{tot}} / \partial z$$

$$\begin{aligned} -4\pi G \rho_{\text{tot}} &= \frac{1}{R} \frac{\partial}{\partial R} (RF_R) + \frac{\partial F_z}{\partial z} \\ -4\pi G \Sigma_{\text{tot}}(z) &= \int_{-z}^z dz \frac{1}{R} \frac{\partial}{\partial R} (RF_R) + F_z(z) - F_z(-z) \end{aligned}$$



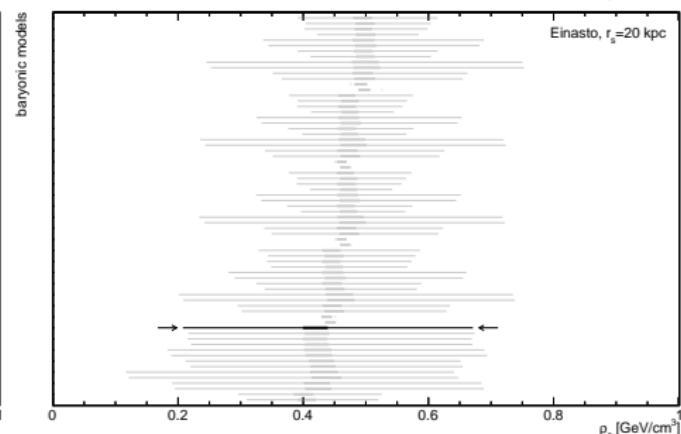
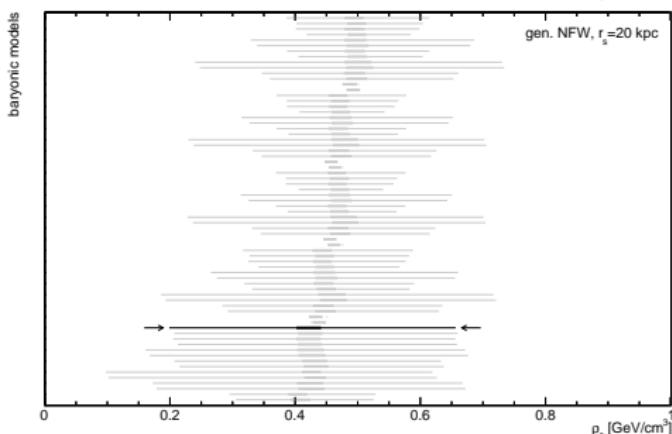
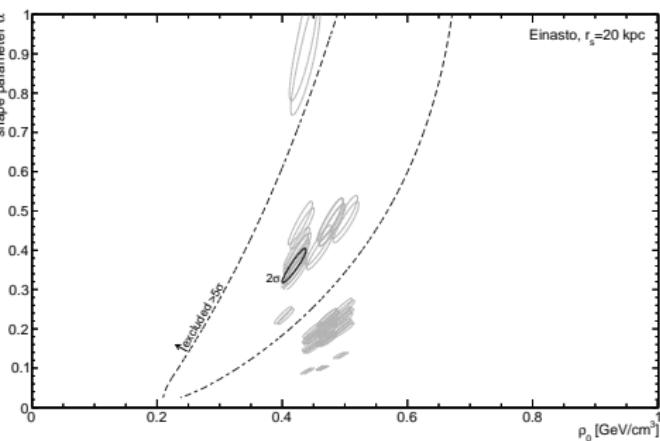
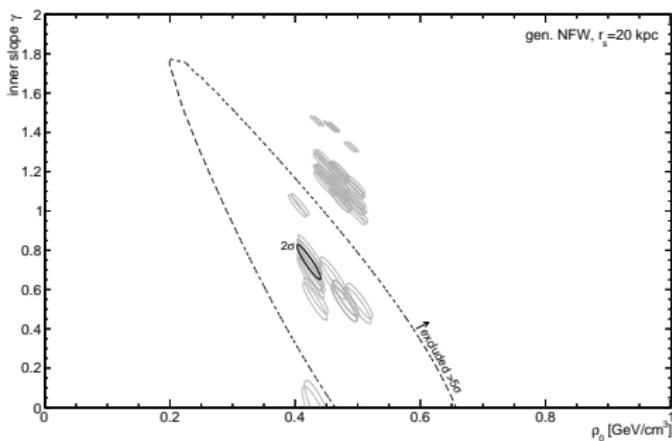
## 2. GLOBAL METHODS

$$\phi_{\text{tot}} = \phi_{\text{bulge}} + \phi_{\text{disc}} + \phi_{\text{gas}} + \phi_{\text{dm}}$$



## 2. GLOBAL METHODS

$$\rho_{\text{dm}} \propto (r/r_s)^{-\gamma} (1+r/r_s)^{-3+\gamma}, \exp(-2((r/r_s)^\alpha - 1)/\alpha)$$

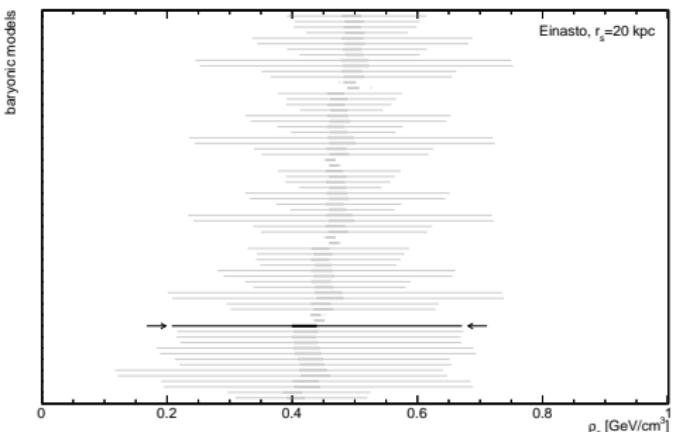
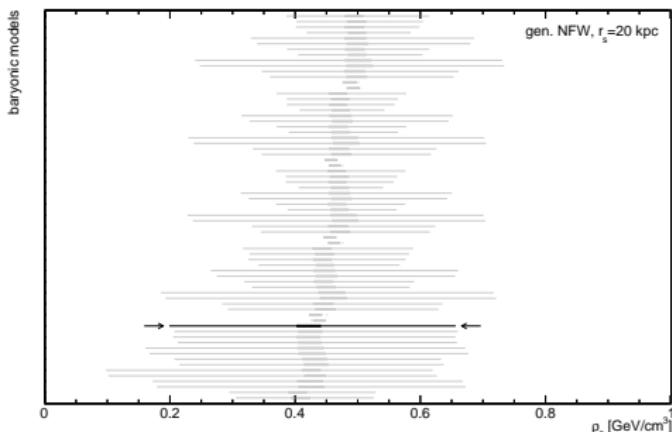


[MP, Iocco & Bertone '15, 1504.06324]

## 2. GLOBAL METHODS

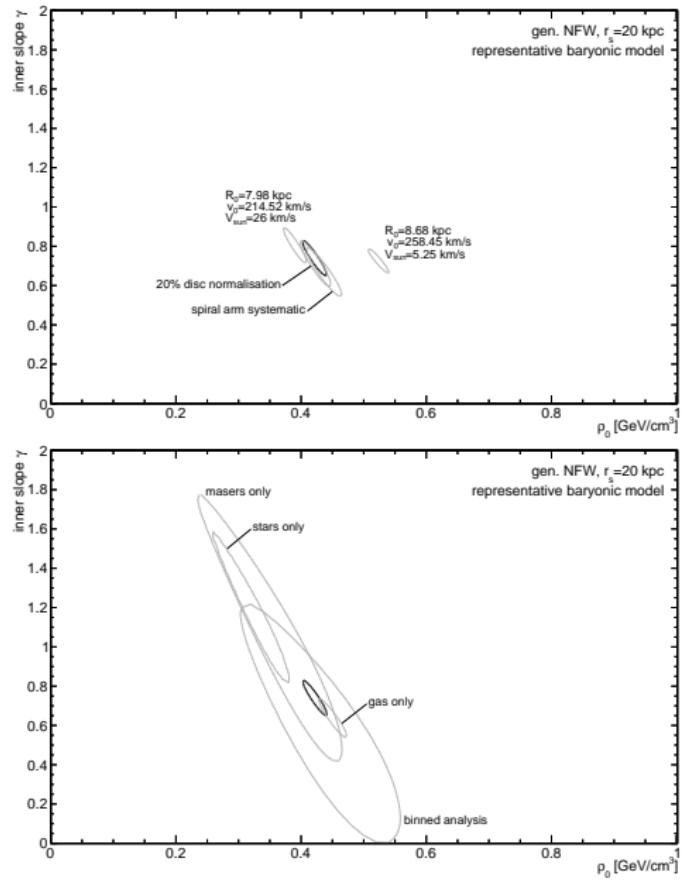
$$\rho_{\text{dm}} \propto (r/r_s)^{-\gamma} (1+r/r_s)^{-3+\gamma}, \exp(-2((r/r_s)^\alpha - 1)/\alpha)$$

NFW:  $\rho_0 = 0.420^{+0.021}_{-0.018} (2\sigma) \pm 0.025 \text{ GeV/cm}^3$   
Einasto:  $\rho_0 = 0.420^{+0.019}_{-0.021} (2\sigma) \pm 0.026 \text{ GeV/cm}^3$



[MP, Iocco & Bertone '15, 1504.06324]

## 2. GLOBAL METHODS

$$\rho_{\text{dm}} \propto (r/r_s)^{-\gamma} (1 + r/r_s)^{-3+\gamma}$$


[MP, Iocco & Bertone '15, 1504.06324]

## 2. MODIFIED NEWTONIAN DYNAMICS

wait, what about MoND?

$$\mu \left( \frac{a}{a_0} \right) a = a_N$$

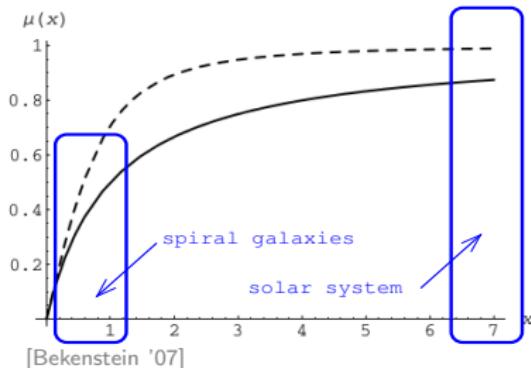
$$a_0 \simeq 10^{-10} \text{ m/s}^2$$

[Milgrom x3 '83]

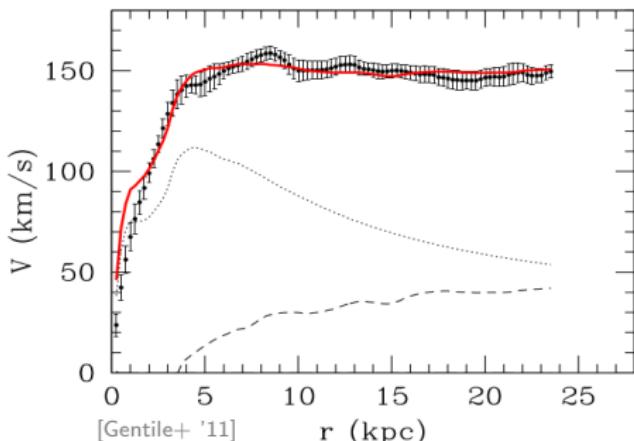
$$\lim_{x \ll 1} \mu(x) = x$$

$$\lim_{x \gg 1} \mu(x) = 1$$

$$\mu_{\text{std}}(x) = \frac{x}{\sqrt{1+x^2}} \quad , \quad \mu_{\text{sim}}(x) = \frac{x}{1+x}$$



NGC 3198



## 2. MODIFIED NEWTONIAN DYNAMICS

wait, what about MoND?

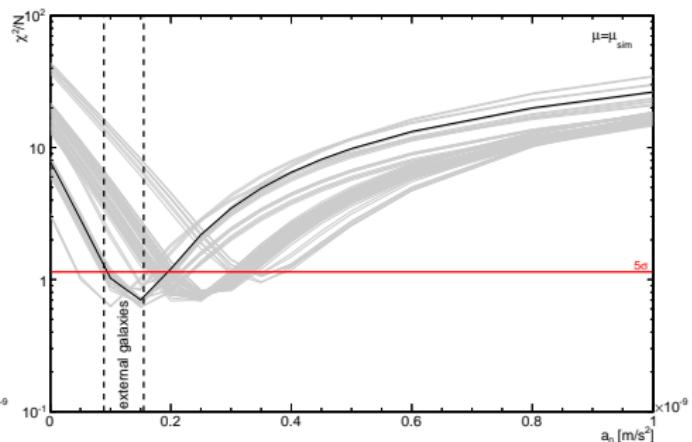
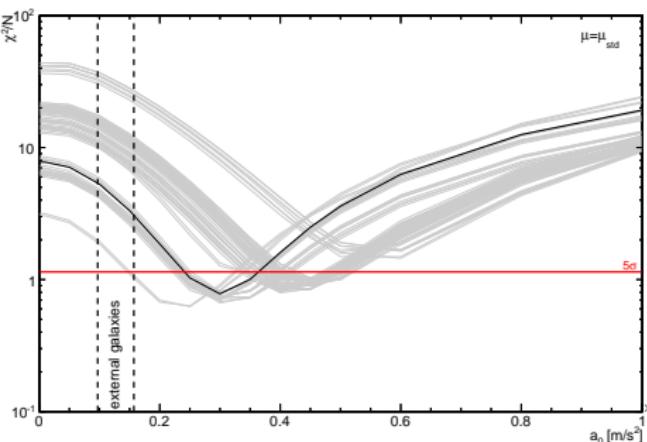
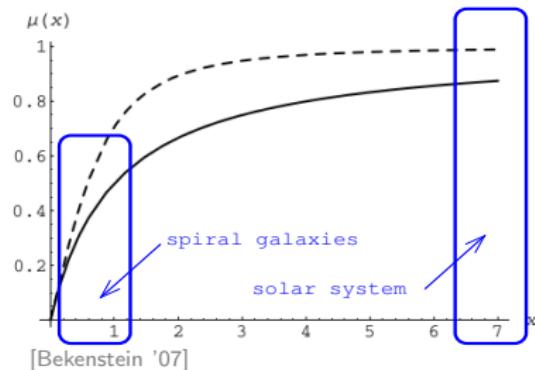
$$\mu \left( \frac{a}{a_0} \right) a = a_N$$

$$a_0 \simeq 10^{-10} \text{ m/s}^2$$

[Milgrom x3 '83]

$$a \rightarrow R\omega_c^2 \quad a_N = R\omega_b^2$$

$$\mu_{\text{std}}(x) = \frac{x}{\sqrt{1+x^2}} \quad , \quad \mu_{\text{sim}}(x) = \frac{x}{1+x}$$



[Iocco, MP & Bertone '15, 1505.05181]

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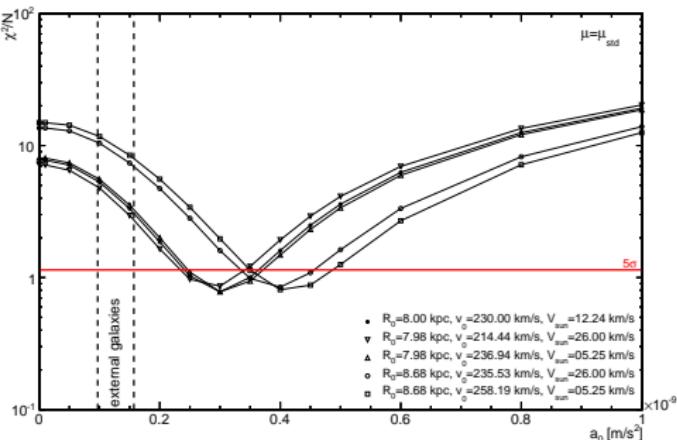
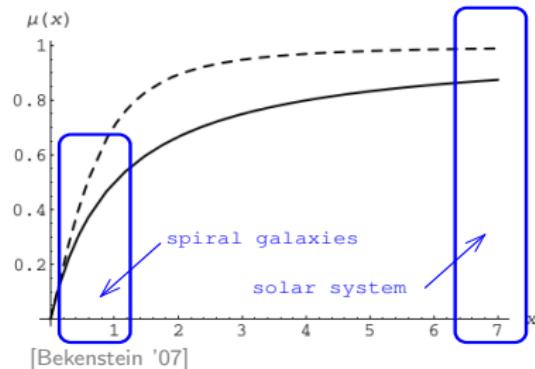
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[Milgrom x3 '83]

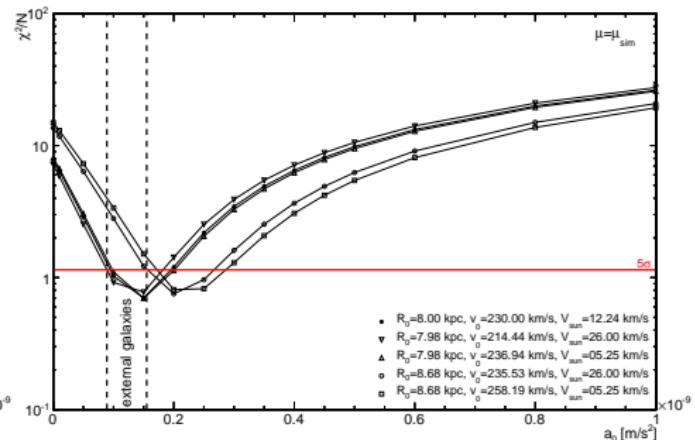
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[Iocco, MP & Bertone '15, 1505.05181]



## 2. MODIFIED NEWTONIAN DYNAMICS

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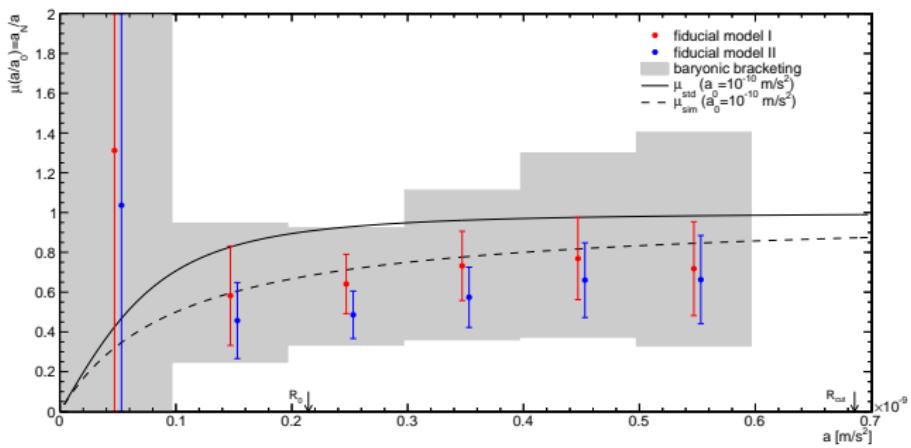
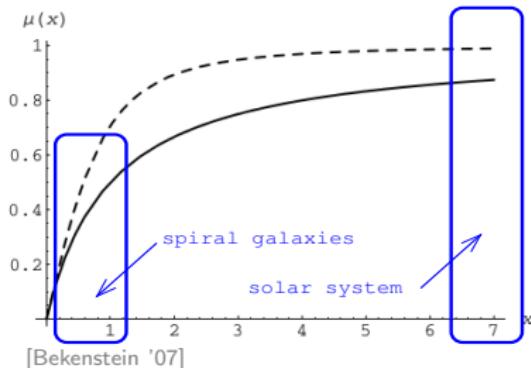
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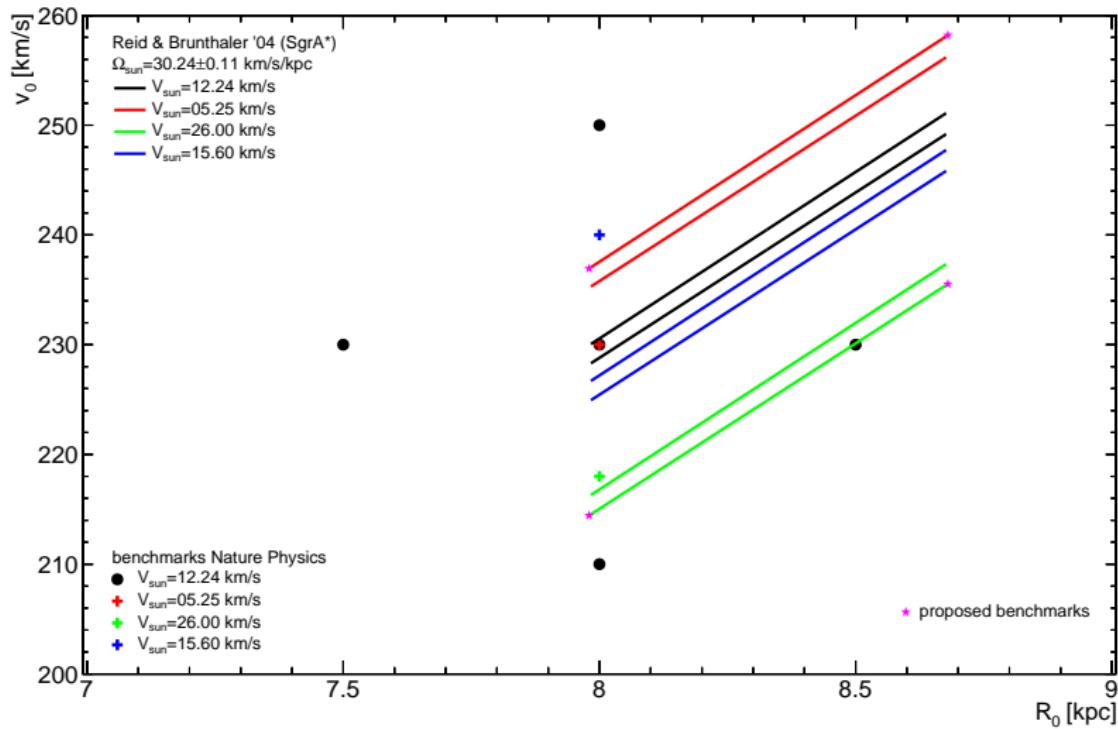
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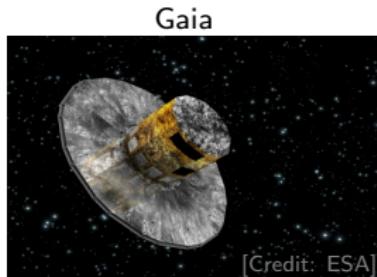
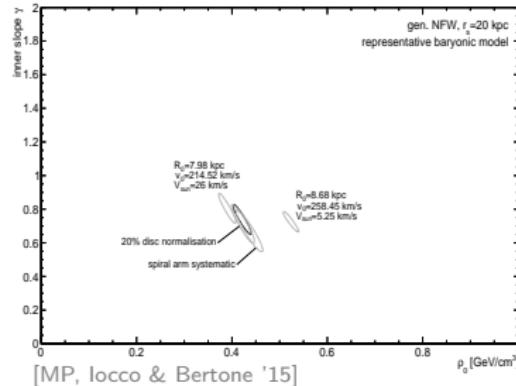
[Iocco, MP & Bertone '15, 1505.05181]

## 2. GALACTIC PARAMETERS



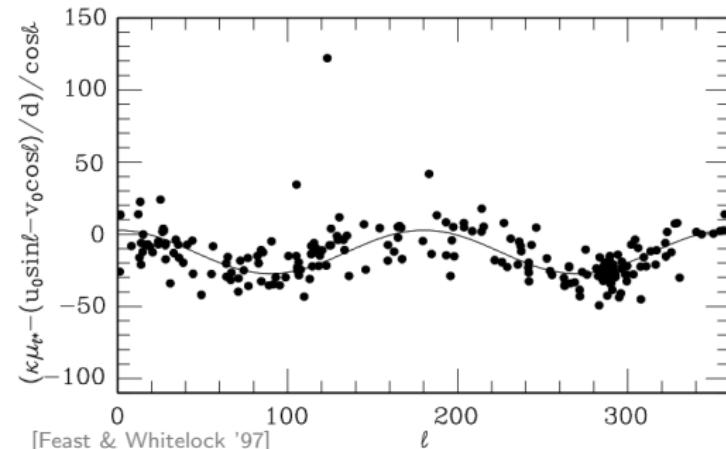
[Iocco, MP & Bertone '15, 1505.05181]

### 3. FUTURE DIRECTIONS?



#### fact sheet

2013-2018  
 $\lambda = 320 - 1000$  nm  
 $10^9$  stars  $G < 20$  mag  
 parallax  $\pm 10 \mu\text{as}$   
 proper motion  $\pm 10 \mu\text{as}/\text{yr}$   
 radial velocity  $\pm 1 \text{ km/s}$



#### Oort constants:

$$A = \frac{1}{2} \left( \frac{v_0}{R_0} - v'_0 \right) \quad B = -\frac{1}{2} \left( \frac{v_0}{R_0} + v'_0 \right)$$

#### Hipparcos:

$$A = +14.82 \pm 0.84 \text{ km/s/kpc}$$

$$B = -12.37 \pm 0.64 \text{ km/s/kpc}$$

Gaia will improve proper motions, radial velocities and parallaxes by a factor 10-200 wrt Hipparcos.