

The Dark Matter distribution of the Milky Way

(its uncertainties and consequences on the determination of new physics)

An empirical approach

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Università Federico II, NAPOLI

“Dark Matter searches in the 2020s. At the crossroads of the WIMP”
ICRR, The University of Tokyo, Kashiwa. November 12, 2019

What is the actual distribution of DM in the Milky Way?

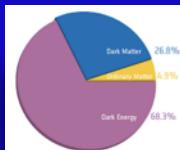
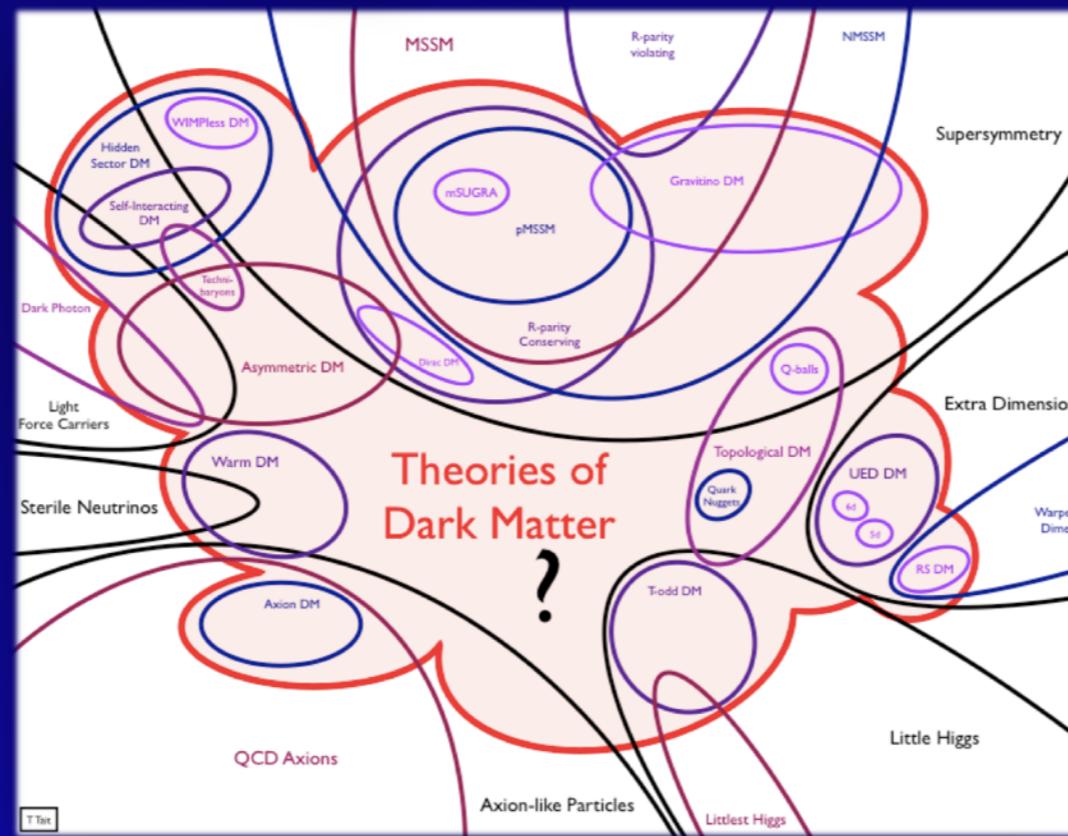
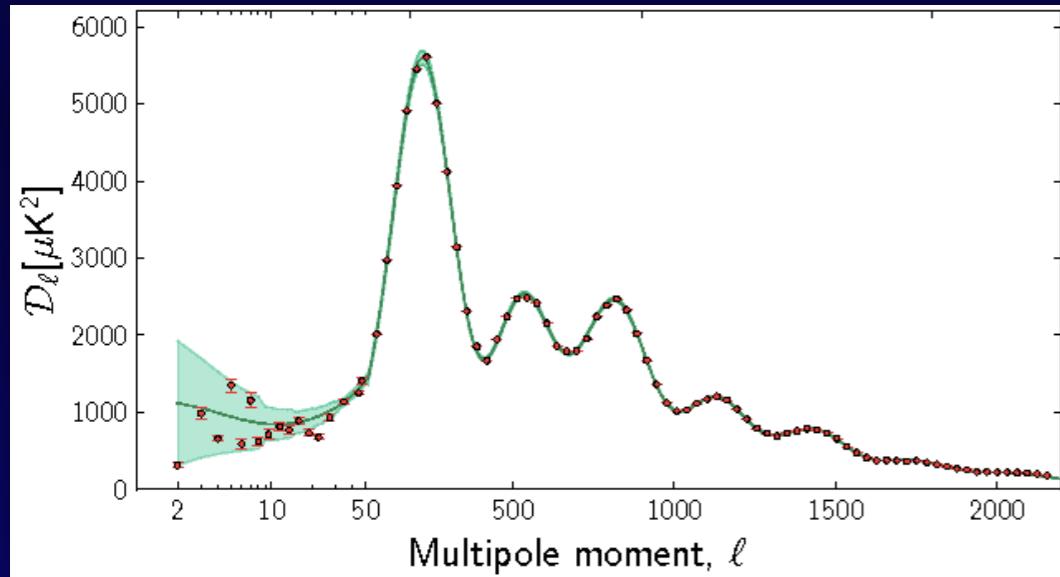


And most notably in the proximity of the Sun?

And the Galactic Center, as requested. Please bear with me until the end.

Dark Matter

Evidence over large range of scales

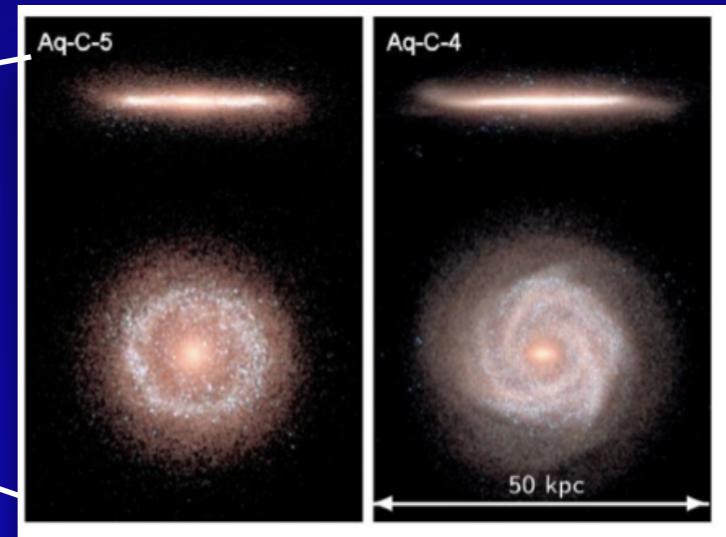
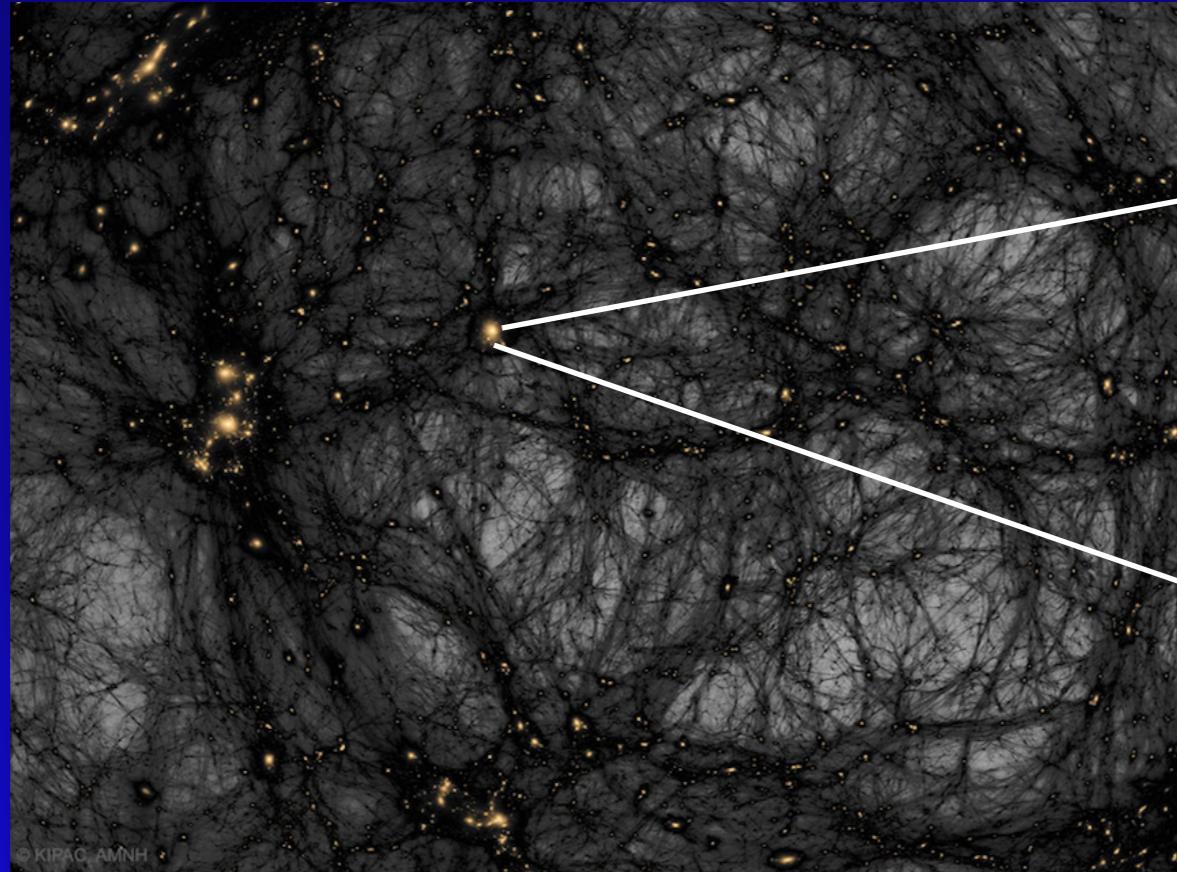
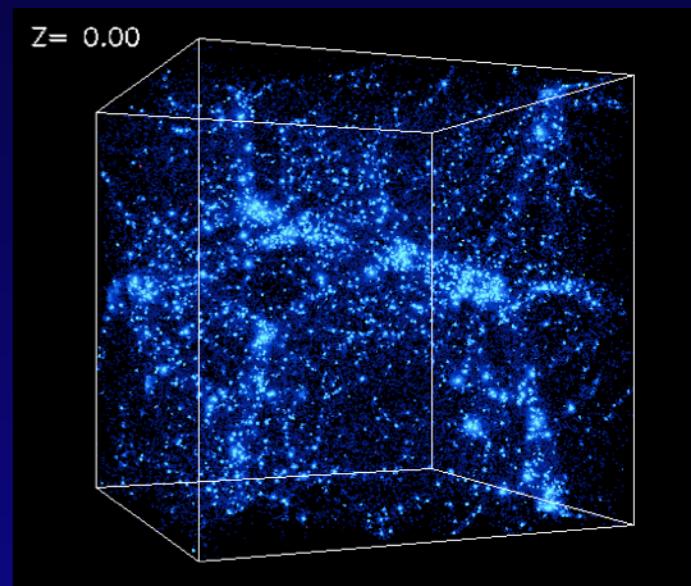
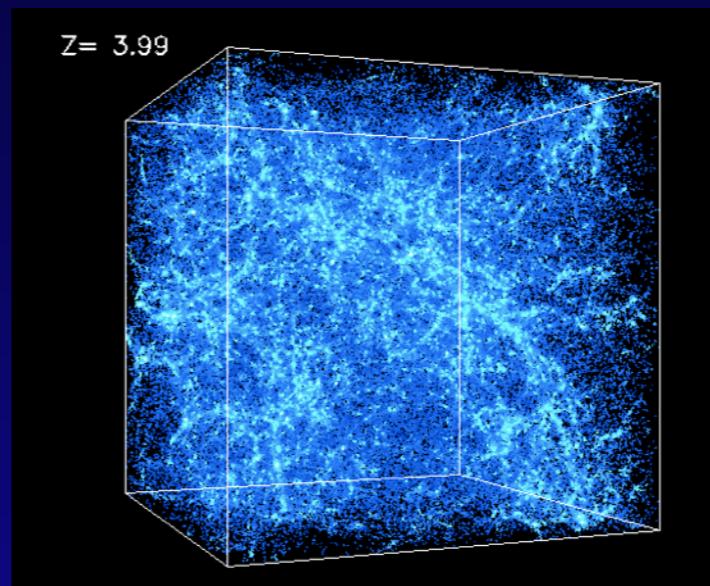
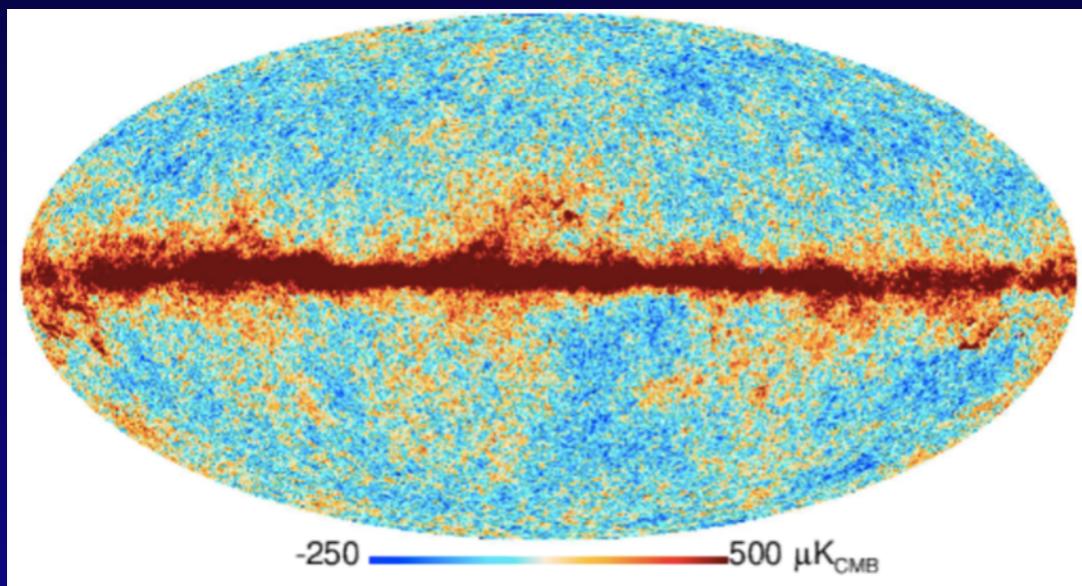


NATURE STILL UNKNOWN

A story of Λ CDM

I: structure formation

age of Universe →



physical size ←

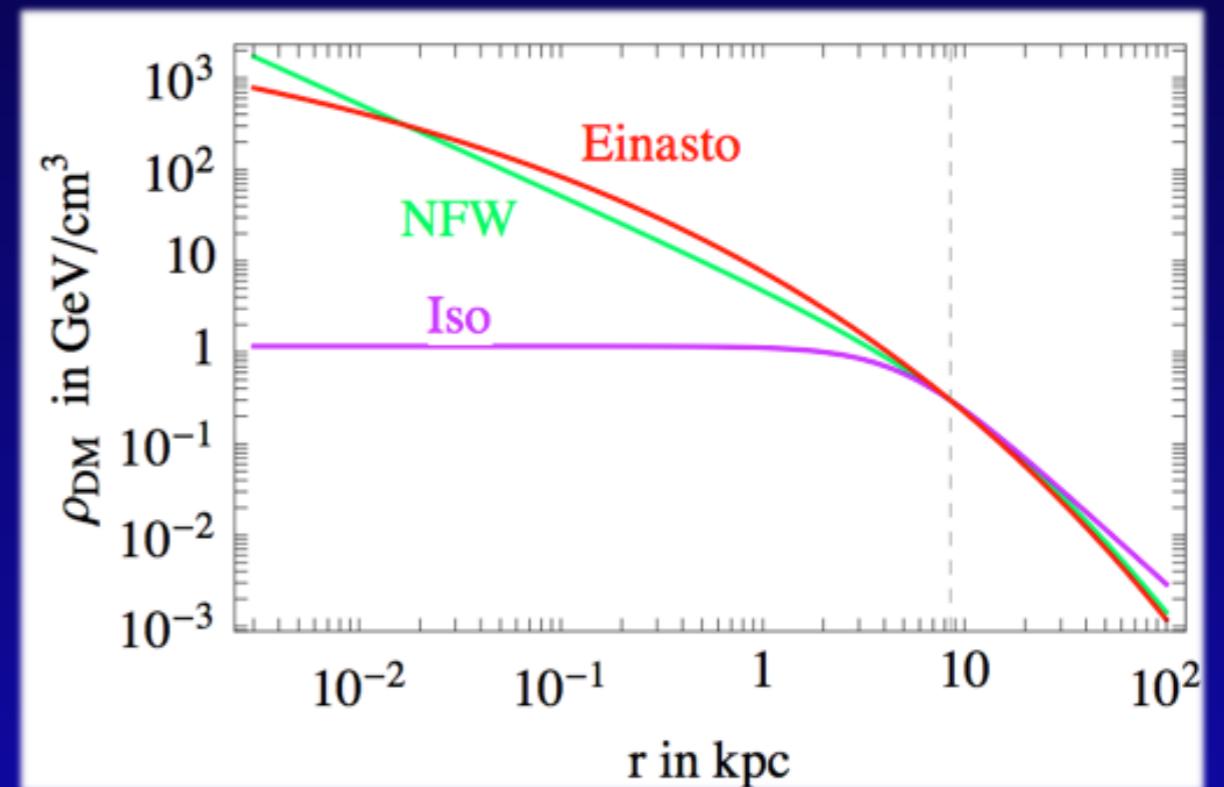
A story of Λ CDM

II. the single halo

A “universal” DM profile?



(not in scale!)

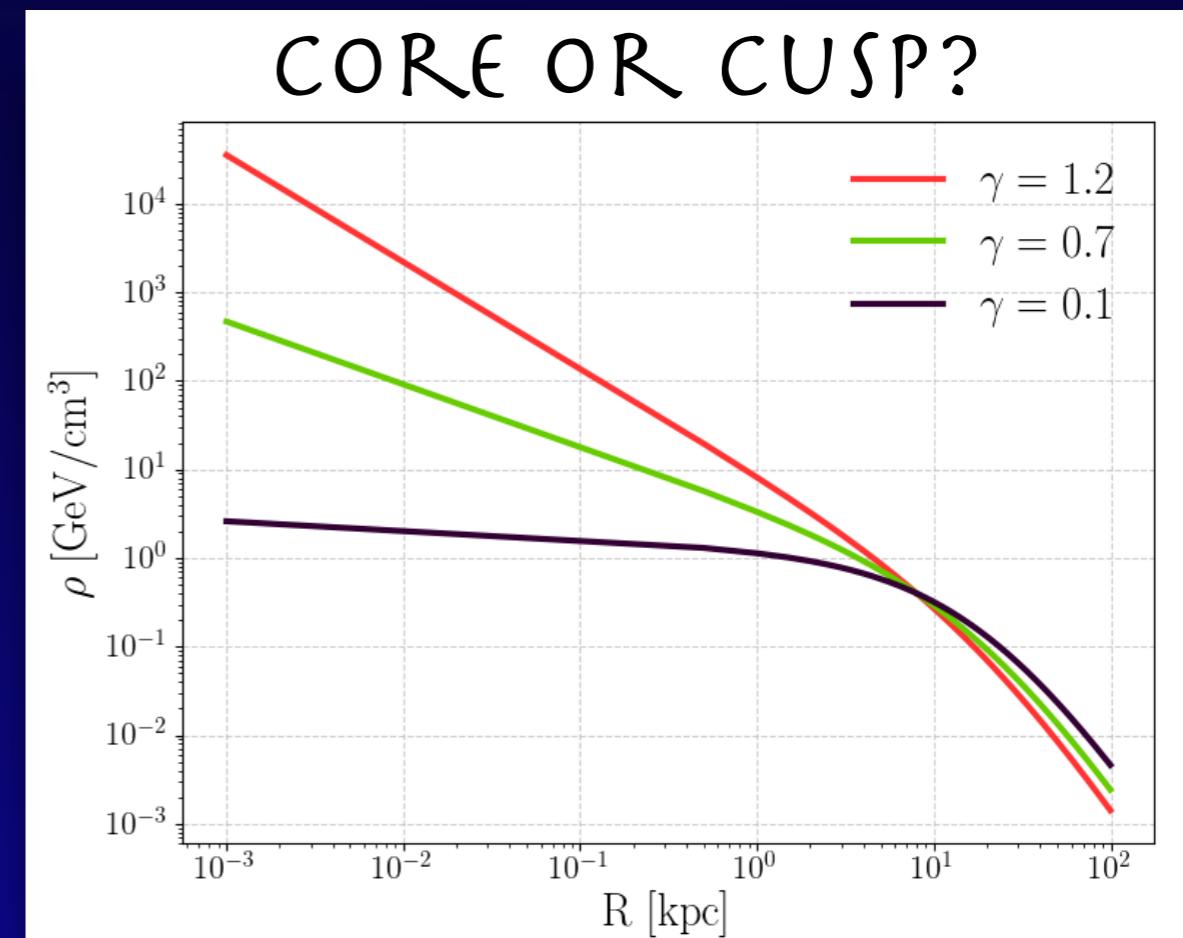
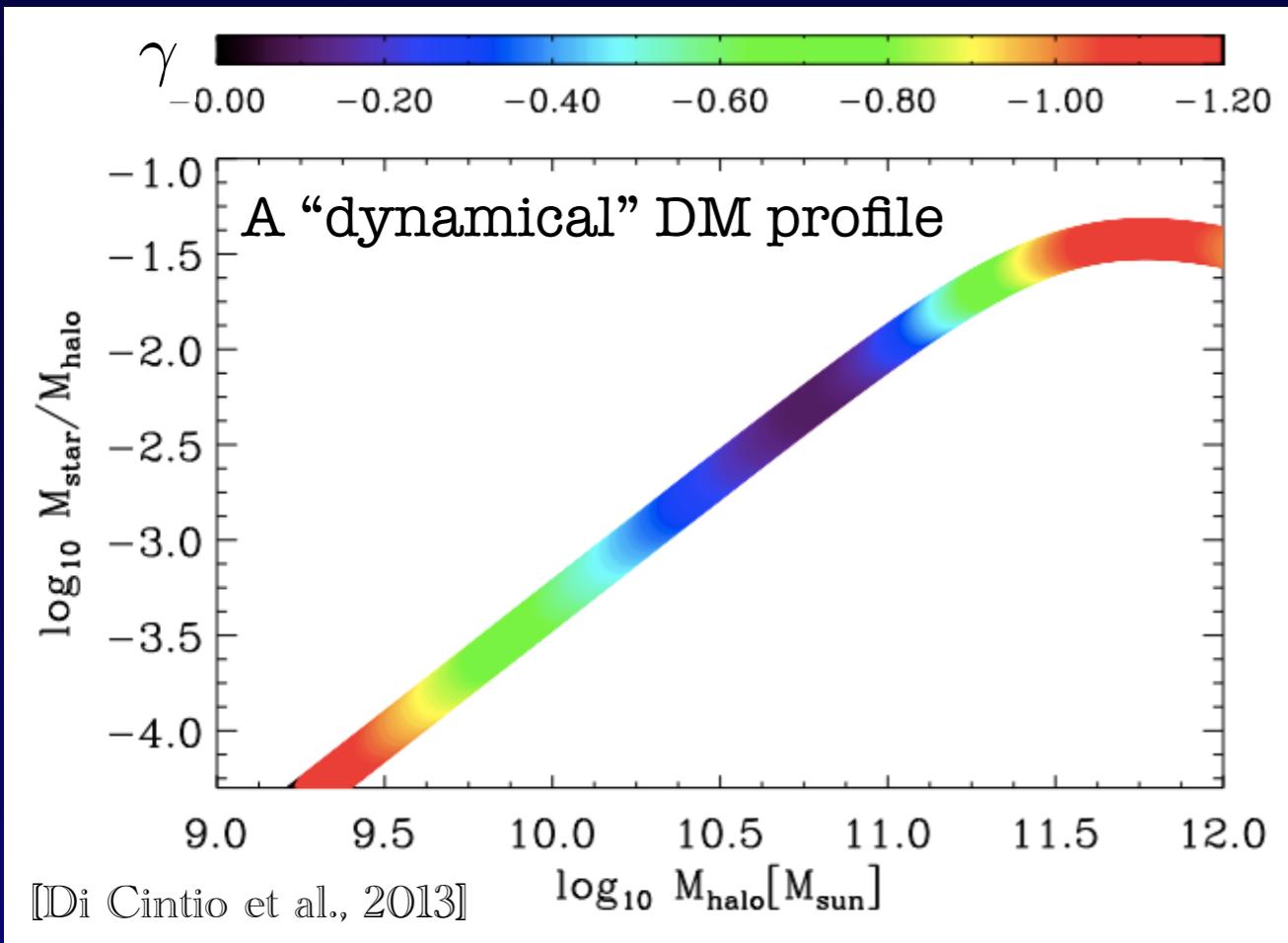


NAVARRO-FRENK-WHITE

$$\rho(R) \propto \frac{R_s}{R} \left(1 + \frac{R}{R_s}\right)^{-2}$$

A story of Λ CDM

III. the dark matter distribution



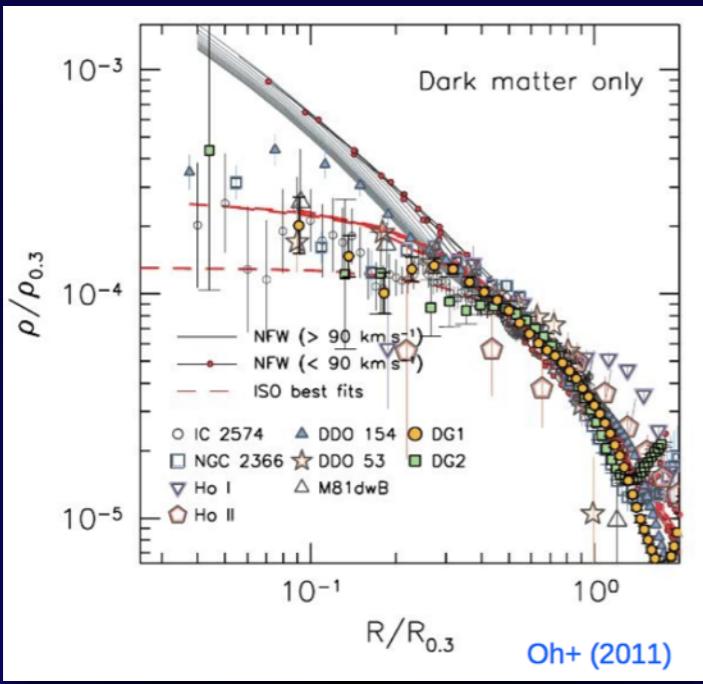
generalized NFW

$$\rho_{DM}(R) \propto \rho_0 \left(\frac{R}{R_s} \right)^{-\gamma} \left(1 + \frac{R}{R_s} \right)^{-3+\gamma}$$

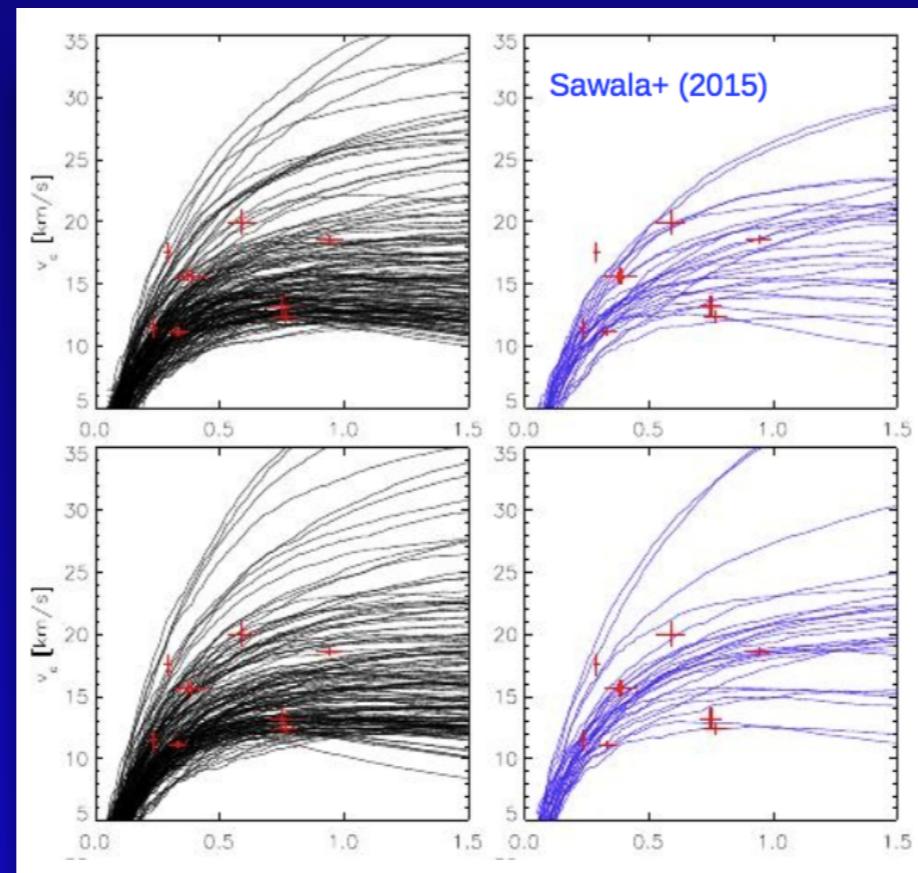
A story of Λ CDM

IV. the small scale problems

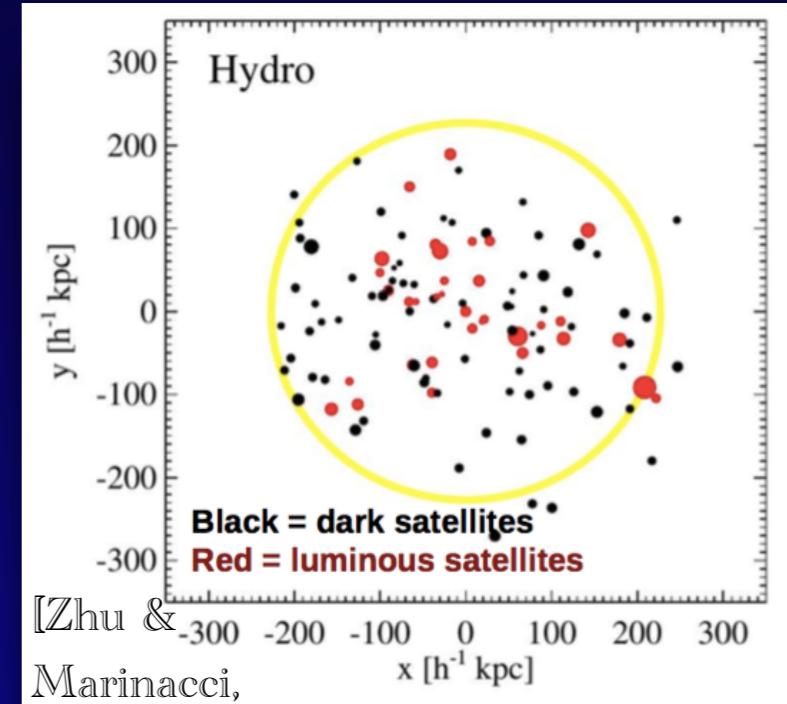
Cusp vs core



Too big to fail



Missing satellite



...or lack thereof

What is the actual distribution of DM in the Milky Way?

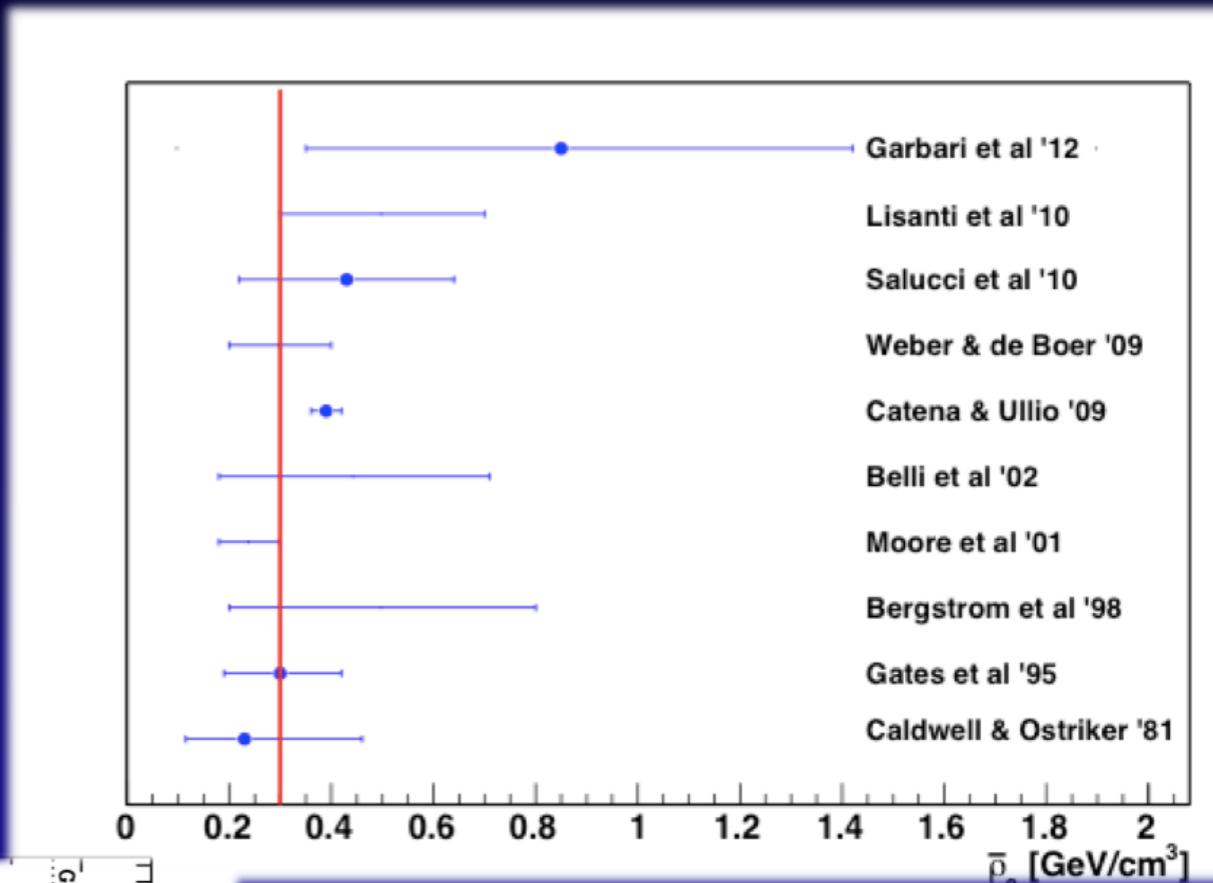
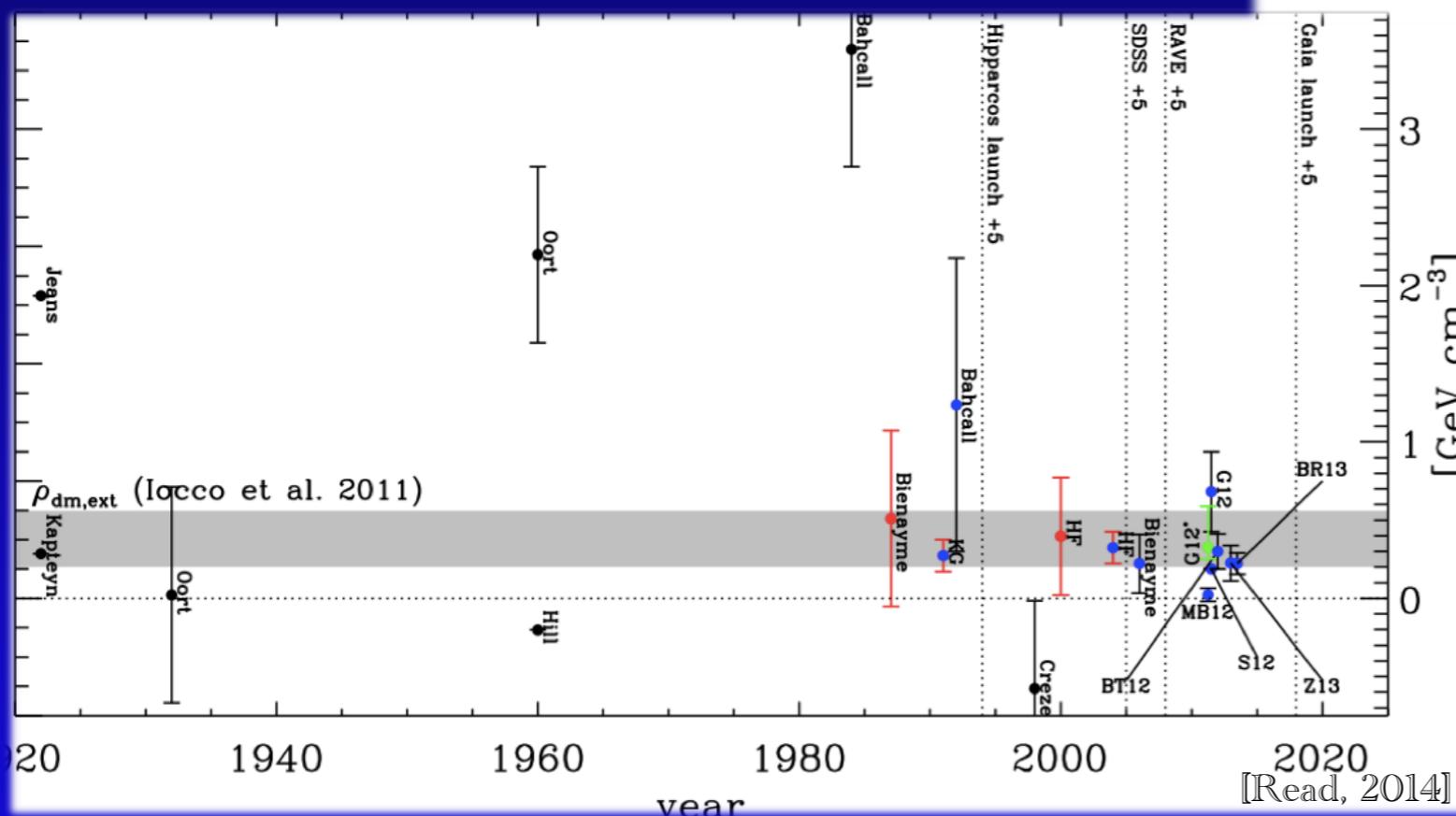


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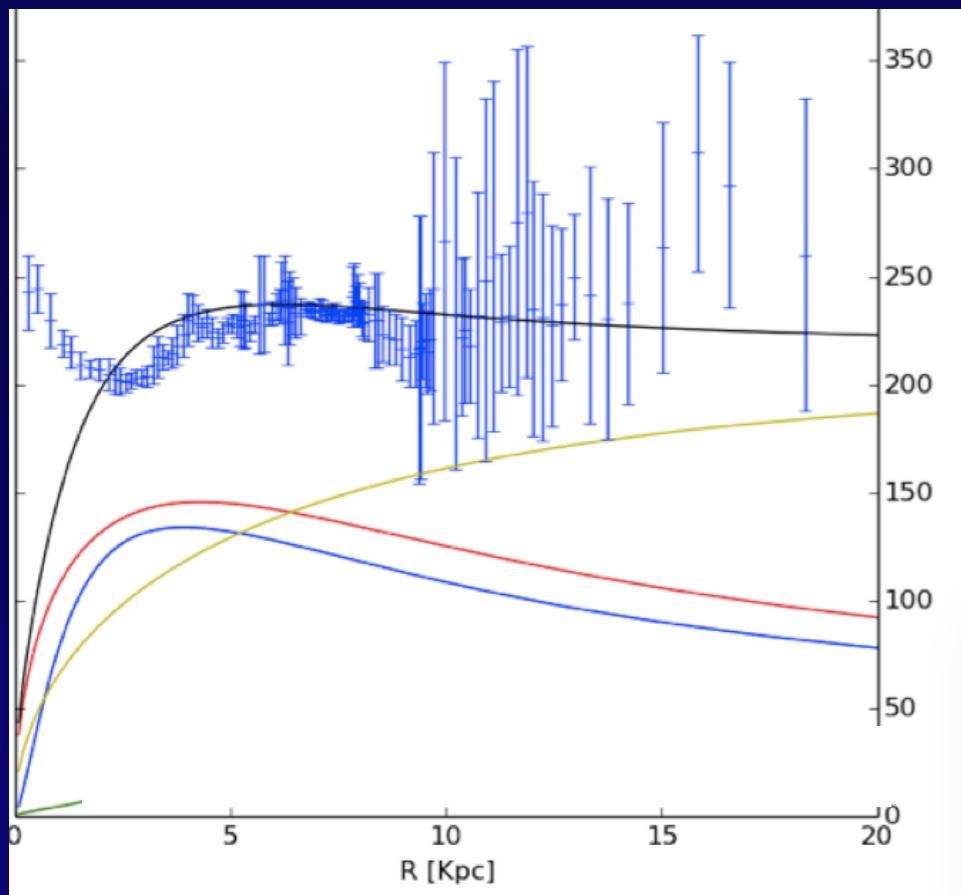
Empirical determination of local DM density

Determinations of
local DM density
are consistent, but noisy



Inferring the whole DM distribution (MW's ‘backbone’)

Fitting a pre-assigned shape
on top of luminous

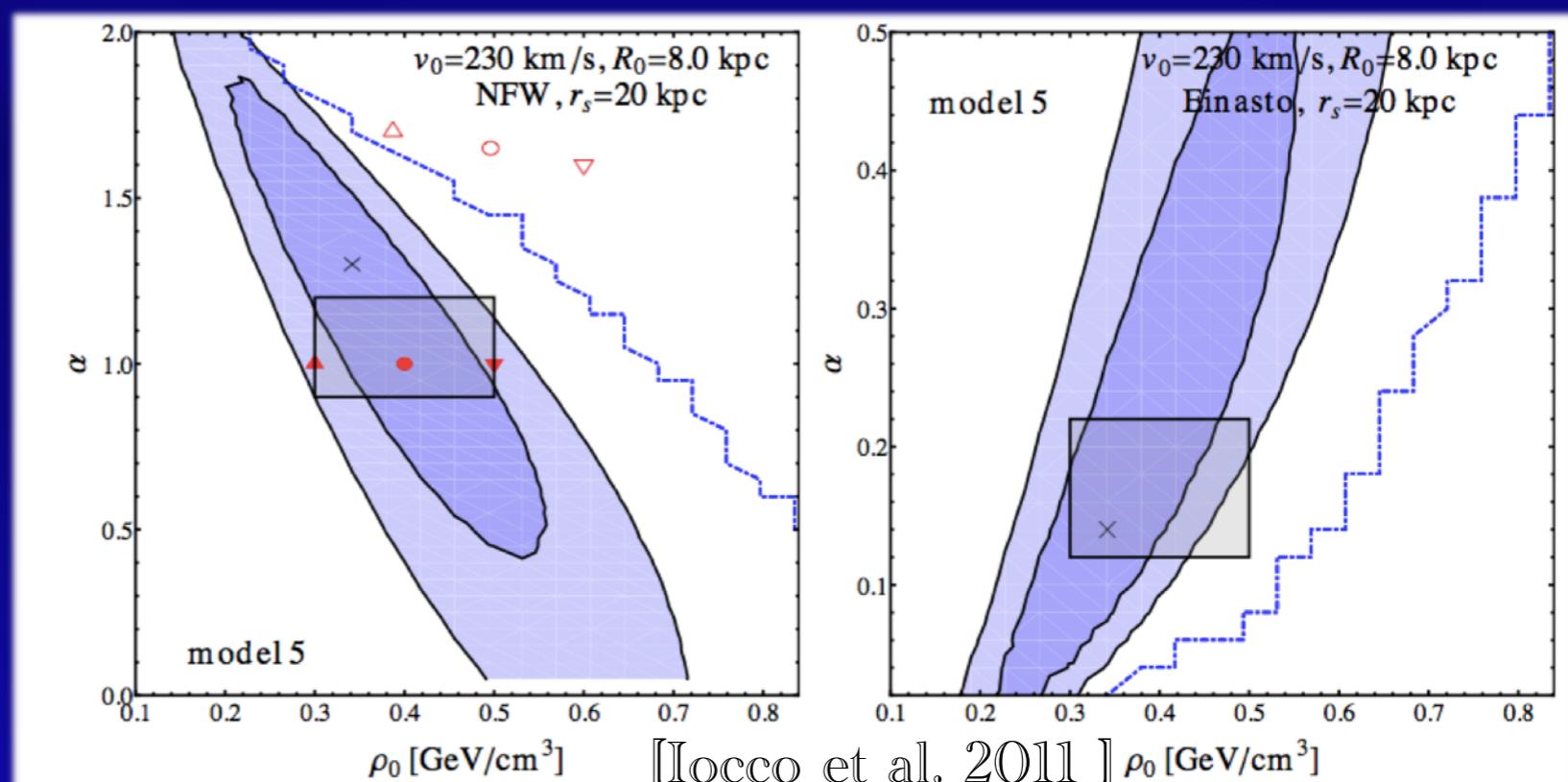


gNFW

$$\rho_{DM}(R) \propto \rho_0 \left(\frac{R}{R_s} \right)^{-\gamma} \left(1 + \frac{R}{R_s} \right)^{-3+\gamma}$$

$$\rho_{DM}(R) \propto \rho_0 \exp \left[-\frac{2}{\gamma} \left(\left(\frac{R}{R_s} \right)^\gamma - 1 \right) \right]$$

Einasto



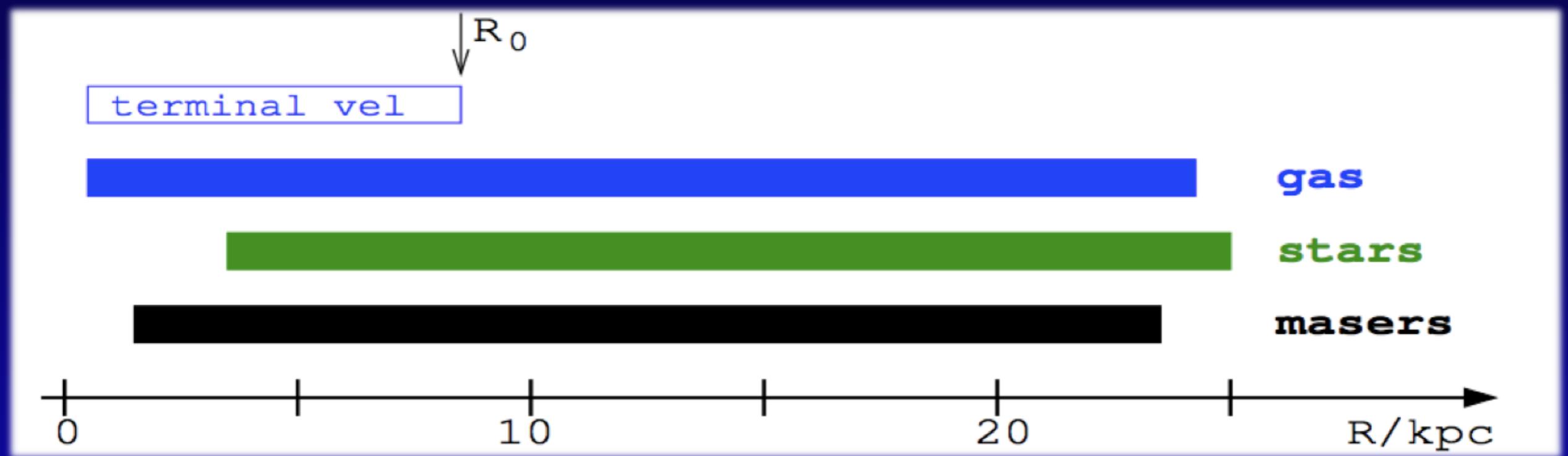
[many authors, e.g.
Iocco et al. 2011]

The case of the Milky Way

Ingredients:

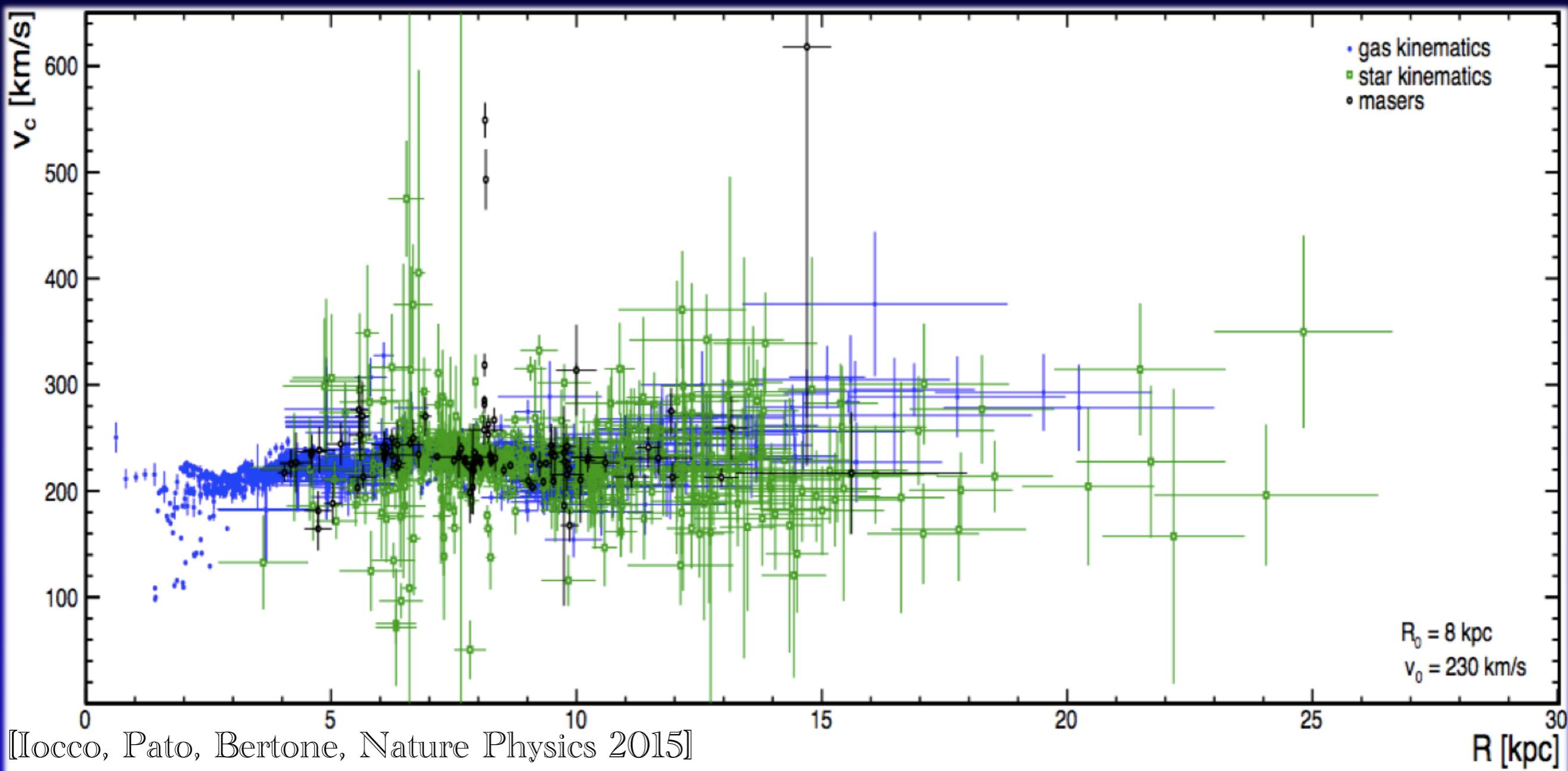
- The observed rotation curve
- The “expected” rotation curve
- Some “grano salis”
- Working hypothesis (later on)

The Milky Way: observed rotation curve the tracers of the gravitational potential



Doppler shift	distance	
1. gas (21cm, H α , CO)	1. terminal velocities (gas)	
2. stars (H, He, O, ...)	2. photo-spectroscopy (stars)	
3. masers (H ₂ O, CH ₃ OH, ...)	3. parallax (masers)	

The Milky Way Rotation Curve as observed



All tracers, optimized for precision between $R=3-20$ kpc

For more details on data treatment (as well as inclusion of different datasets) ...

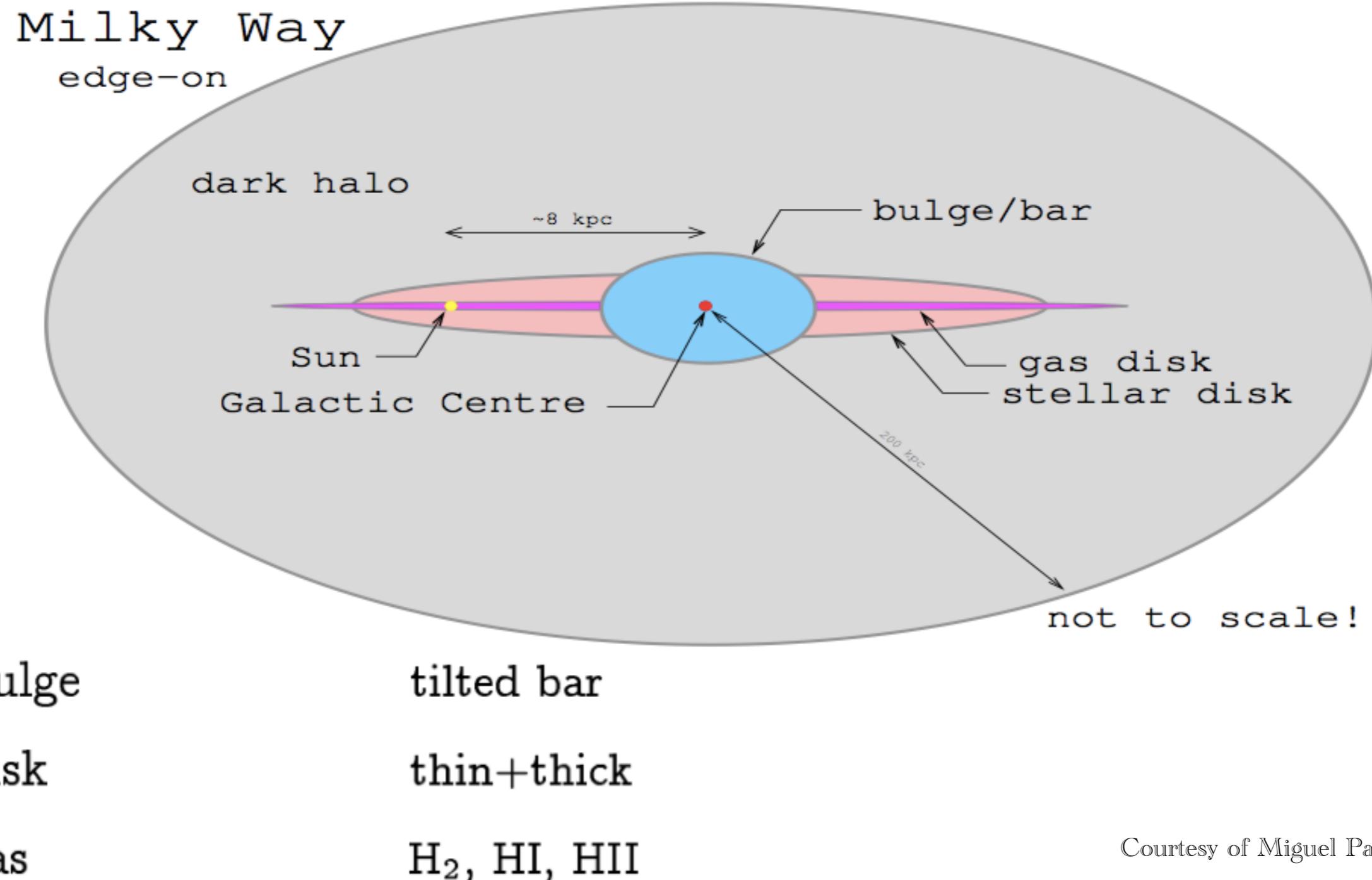
The Milky Way: ‘expected’ rotation curve from visible (baryon) component

$$\Phi_{\text{baryon}} = \Phi_{\text{bulge}} + \Phi_{\text{disk}} + \Phi_{\text{gas}}$$

$$\rho_i(x, y, z) \rightarrow \phi_i(r, \theta, \varphi) \rightarrow v_{c,i}^2(R) = \sum_{\varphi} R \frac{d\phi_i}{dr}(R, \pi/2, \varphi)$$

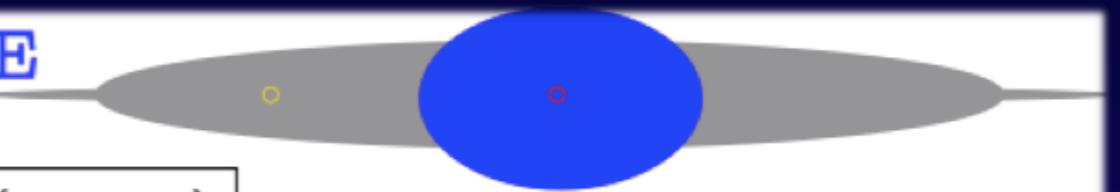
Constructing the curve expected from observed mass profiles

The Milky Way: expected rotation curve the baryonic components



The luminous Milky Way: observations of morphology

2. BARYONS: STELLAR BULGE



$$\rho_{\text{bulge}} = \rho_0 f(x, y, z)$$

morphology $f(x, y, z)$

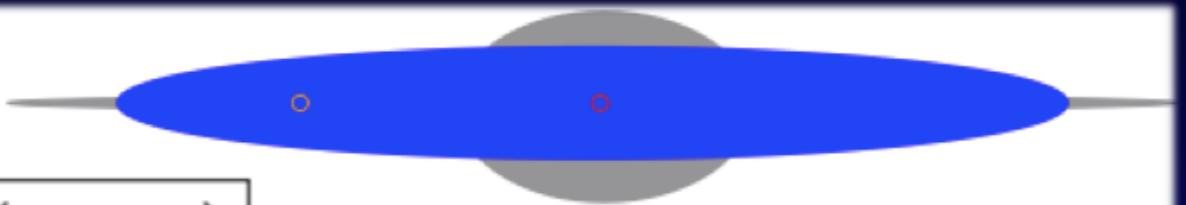
Stanek+ '97 (E2)	e^{-r}	0.9:0.4:0.3	24°	optical
Stanek+ '97 (G2)	$e^{-r_s^2/2}$	1.2:0.6:0.4	25°	optical
Zhao '96	$e^{-r_s^2/2} + r_a^{-1.85} e^{-r_a}$	1.5:0.6:0.4	20°	infrared
Bissantz & Gerhard '02	$e^{-r_s^2}/(1+r)^{1.8}$	2.8:0.9:1.1	20°	infrared
Lopez-Corredoira+ '07	Ferrer potential	7.8:1.2:0.2	43°	infrared/optical
Vanhollebeke+ '09	$e^{-r_s^2}/(1+r)^{1.8}$	2.6:1.8:0.8	15°	infrared/optical
Robin+ '12	$\operatorname{sech}^2(-r_s) + e^{-r_s}$	1.5:0.5:0.4	13°	infrared

normalisation ρ_0 and its statistical uncertainties

microlensing optical depth: $\langle \tau \rangle = 2.17^{+0.47}_{-0.38} \times 10^{-6}$, $(\ell, b) = (1.50^\circ, -2.68^\circ)$
(MACHO '05)

The luminous Milky Way: observations of morphology

2. BARYONS: STELLAR DISK



$$\rho_{\text{disk}} = \rho_0 f(x, y, z)$$

morphology $f(x, y, z)$

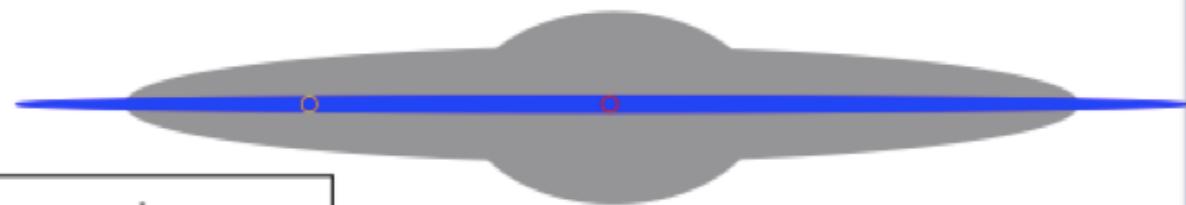
Han & Gould '03	$e^{-R} \operatorname{sech}^2(z)$ $e^{-R- z }$	2.8:0.27 2.8:0.44	thin thick	optical
Calchi-Novati & Mancini '11	$e^{-R- z }$ $e^{-R- z }$	2.8:0.25 4.1:0.75	thin thick	optical
deJong+ '10	$e^{-R- z }$ $e^{-R- z }$ $(R^2 + z^2)^{-2.75/2}$	2.8:0.25 4.1:0.75 1.0:0.88	thin thick halo	optical
Jurić+ '08	$e^{-R- z }$ $e^{-R- z }$ $(R^2 + z^2)^{-2.77/2}$	2.2:0.25 3.3:0.74 1.0:0.64	thin thick halo	optical
Bovy & Rix '13	$e^{-R- z }$	2.2:0.40	single	optical

normalization and its statistical uncertainties

local surface density: $\Sigma_* = 38 \pm 4 M_\odot/\text{pc}^2$ [Bovy & Rix '13]

The luminous Milky Way: observations of morphology

2. BARYONS: GAS



$$n_{\text{H}} = 2n_{\text{H}_2} + n_{\text{HI}} + n_{\text{HII}}$$

morphology

Ferrière '12	$r < 0.01 \text{ kpc}$	$M_{\text{gas}} \sim 7 \times 10^5 \text{ M}_{\odot}$		CO, 21cm, H α , ...
Ferrière+ '07	$r = 0.01 - 2 \text{ kpc}$	CMZ, holed disk CMZ, holed disk warm, hot, very hot	H ₂ H I H II	CO 21cm disp. meas.
Ferrière '98	$r = 3 - 20 \text{ kpc}$	molecular ring cold, warm warm, hot	H ₂ H I H II	CO 21cm disp. meas., H α
Moskalenko+ '02	$r = 3 - 20 \text{ kpc}$	molecular ring	H ₂ H I H II	CO 21cm disp. meas.

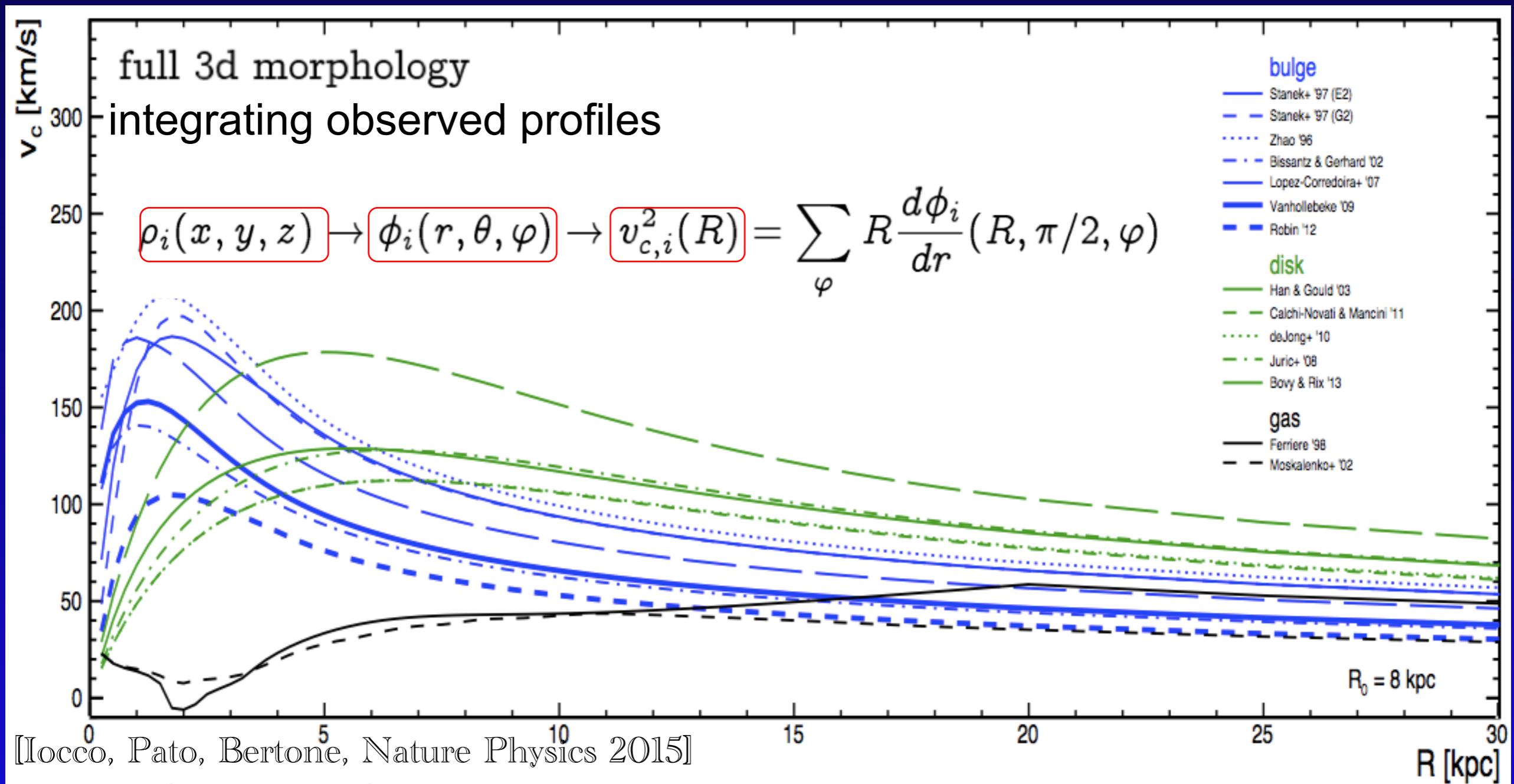
uncertainties

CO-to-H₂ factor: $X_{\text{CO}} = 0.25 - 1.0 \times 10^{20} \text{ cm}^{-2} \text{ K}^{-1} \text{ km}^{-1} \text{ s}$ for $r < 2 \text{ kpc}$
 $X_{\text{CO}} = 0.50 - 3.0 \times 10^{20} \text{ cm}^{-2} \text{ K}^{-1} \text{ km}^{-1} \text{ s}$ for $r > 2 \text{ kpc}$

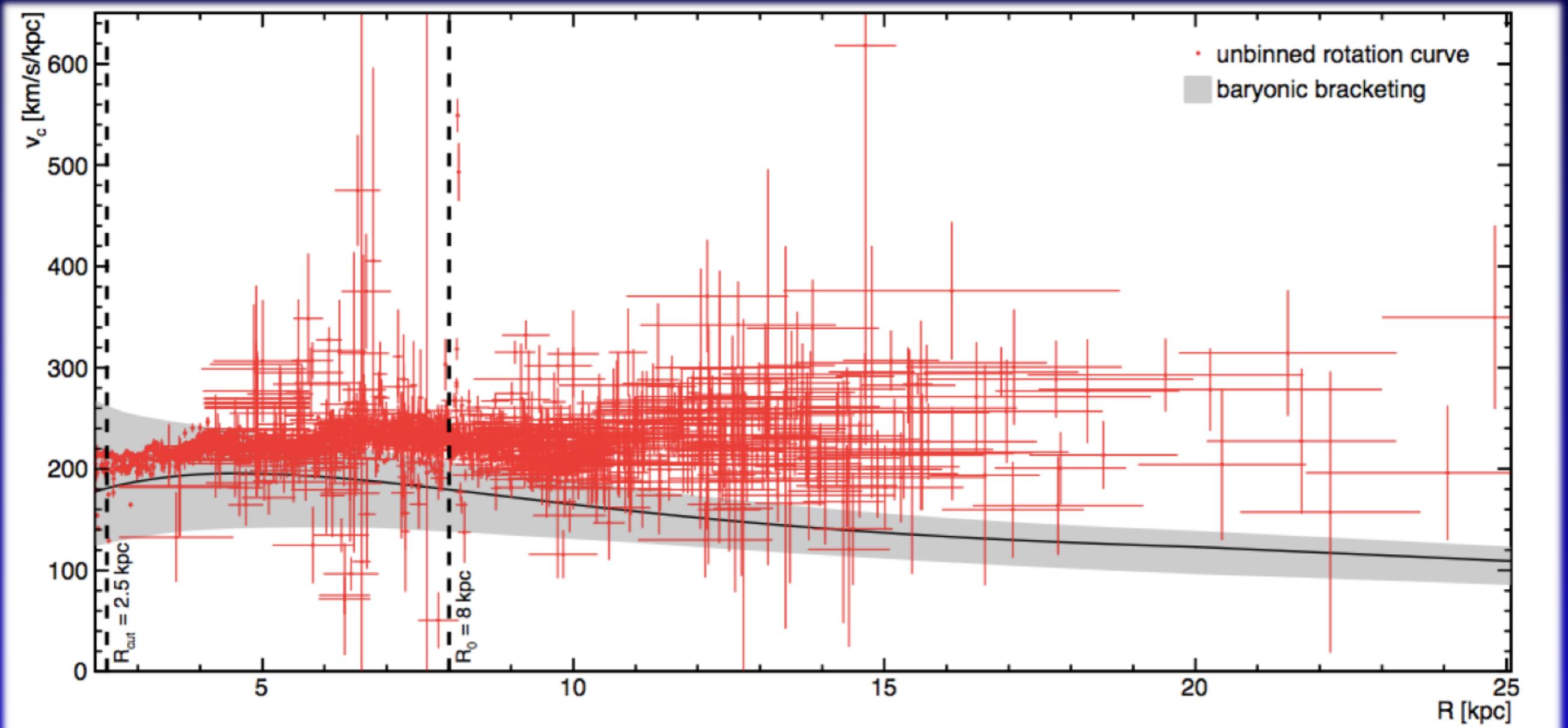
[Ferrière+ '07, Ackermann '12]

The luminous Milky Way: expected rotation curve

$$\phi_i(r, \theta, \varphi) = -4\pi G \sum_{l,m} \frac{Y_{lm}(\theta, \varphi)}{2l+1} \left[\frac{1}{r^{l+1}} \int_0^r \rho_{i,lm}(a) a^{l+2} da + r^l \int_r^\infty \rho_{i,lm}(a) a^{1-l} da \right]$$

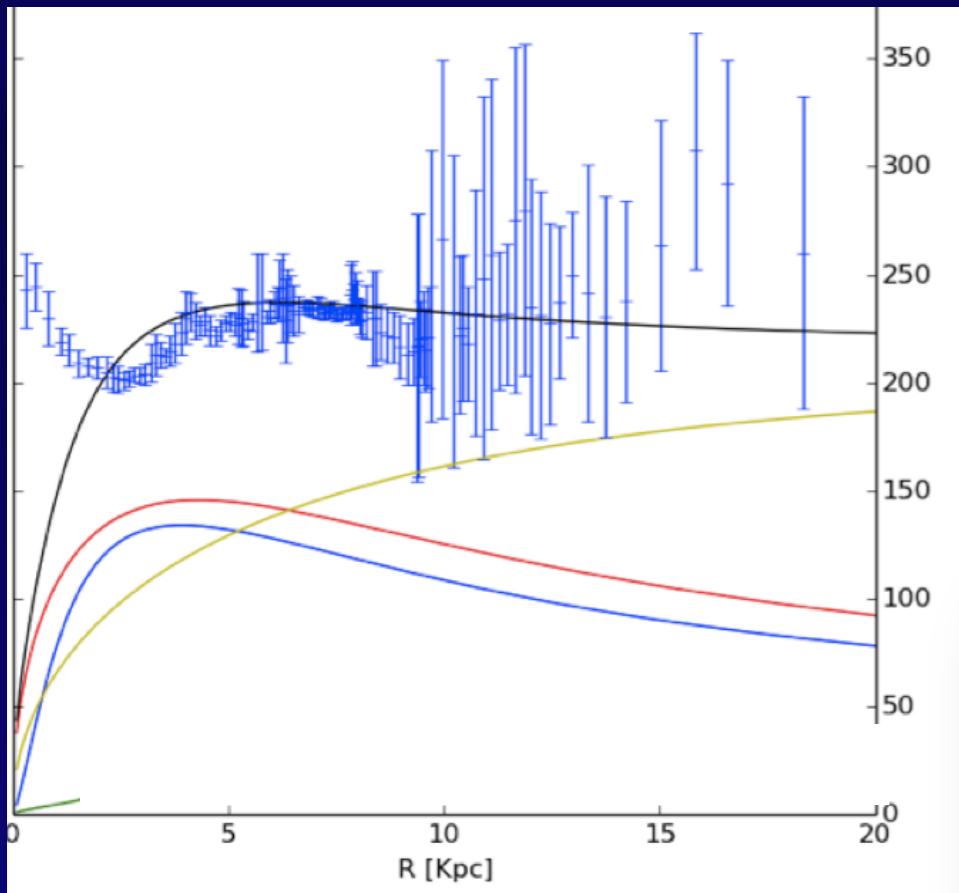


The Milky Way: testing expectations (with no additional assumptions)



Inferring the DM density structure

Fitting a pre-assigned shape
on top of luminous

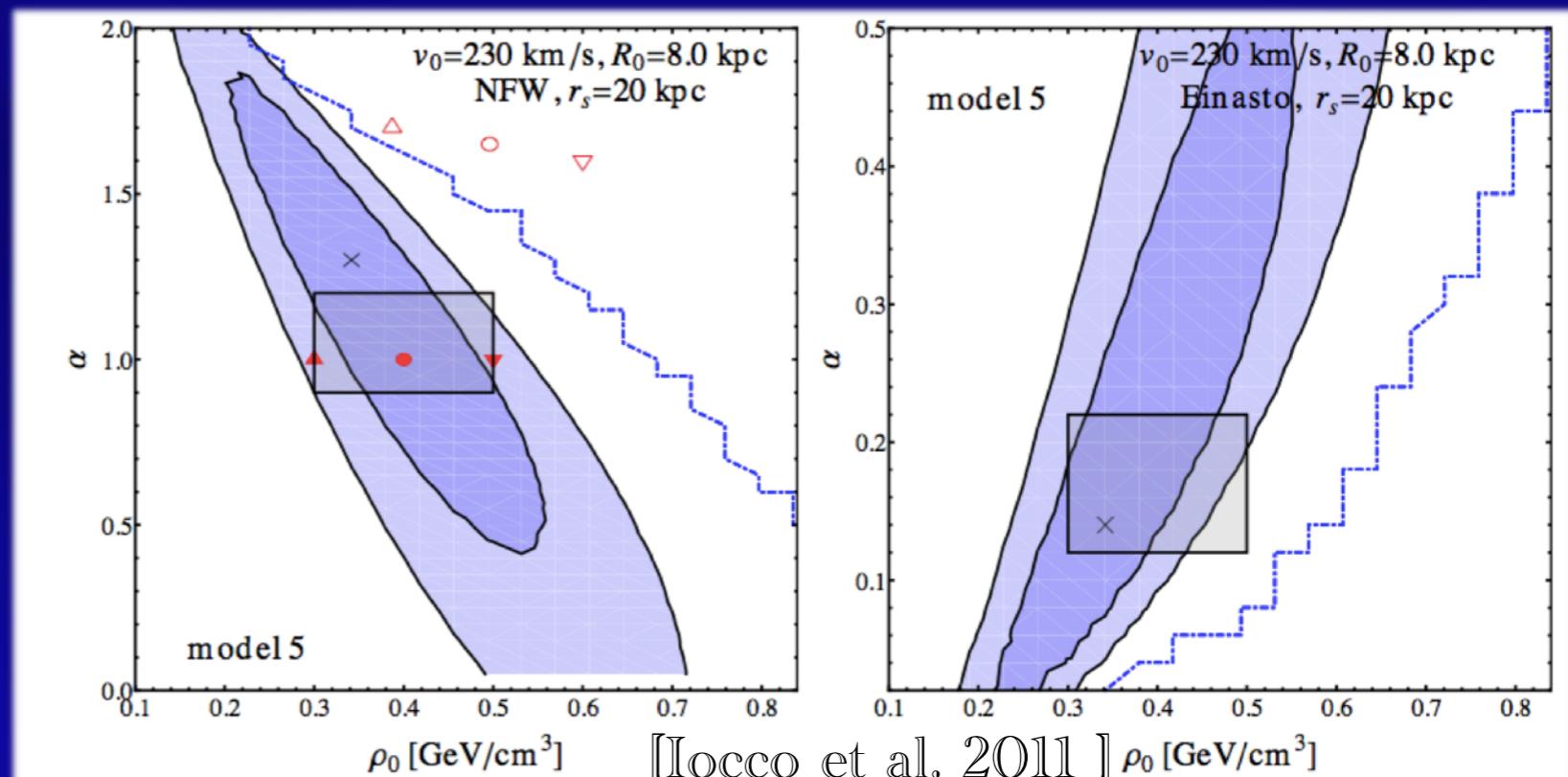


gNFW

$$\rho_{DM}(R) \propto \rho_0 \left(\frac{R}{R_s} \right)^{-\gamma} \left(1 + \frac{R}{R_s} \right)^{-3+\gamma}$$

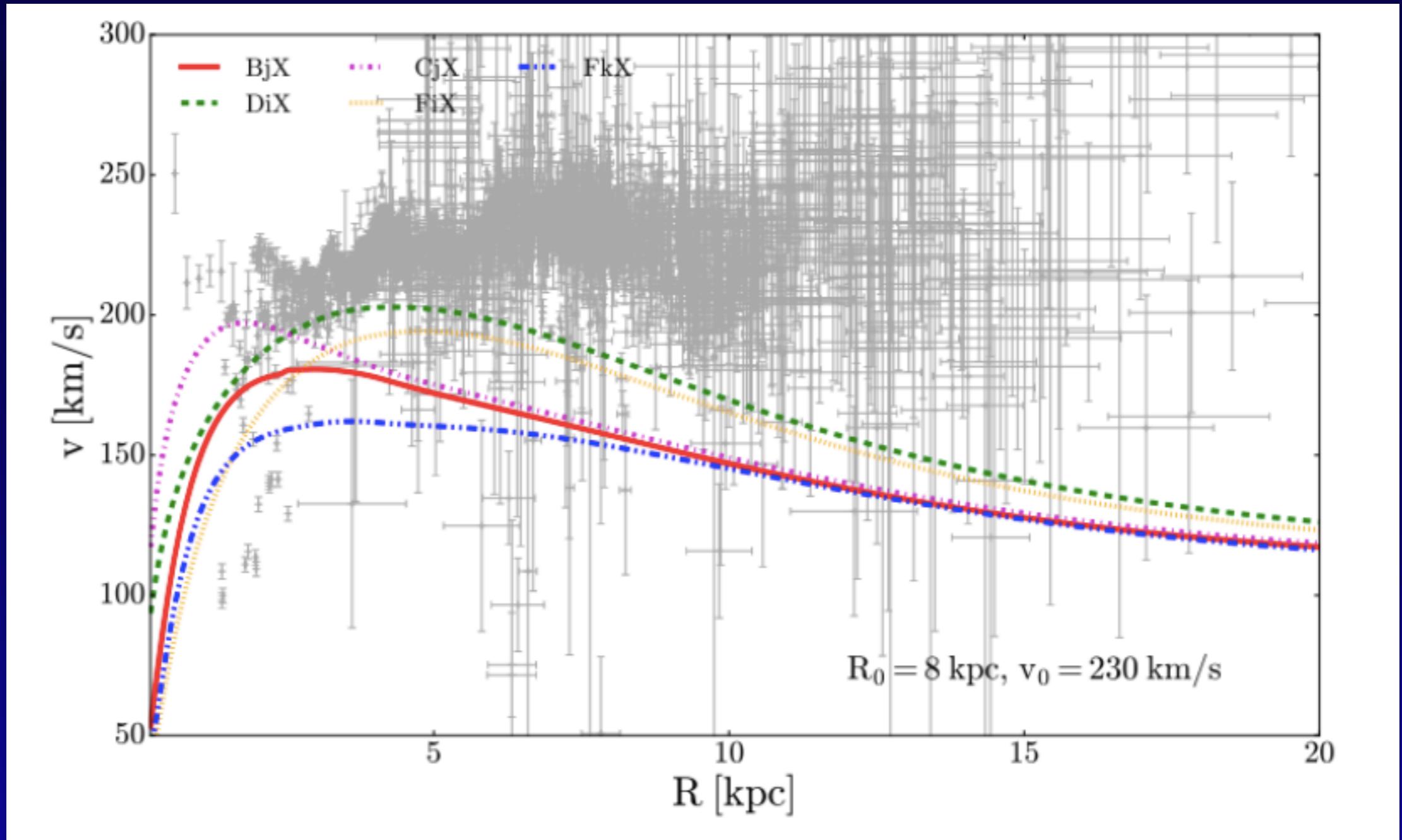
$$\rho_{DM}(R) \propto \rho_0 \exp \left[-\frac{2}{\gamma} \left(\left(\frac{R}{R_s} \right)^\gamma - 1 \right) \right]$$

Einasto

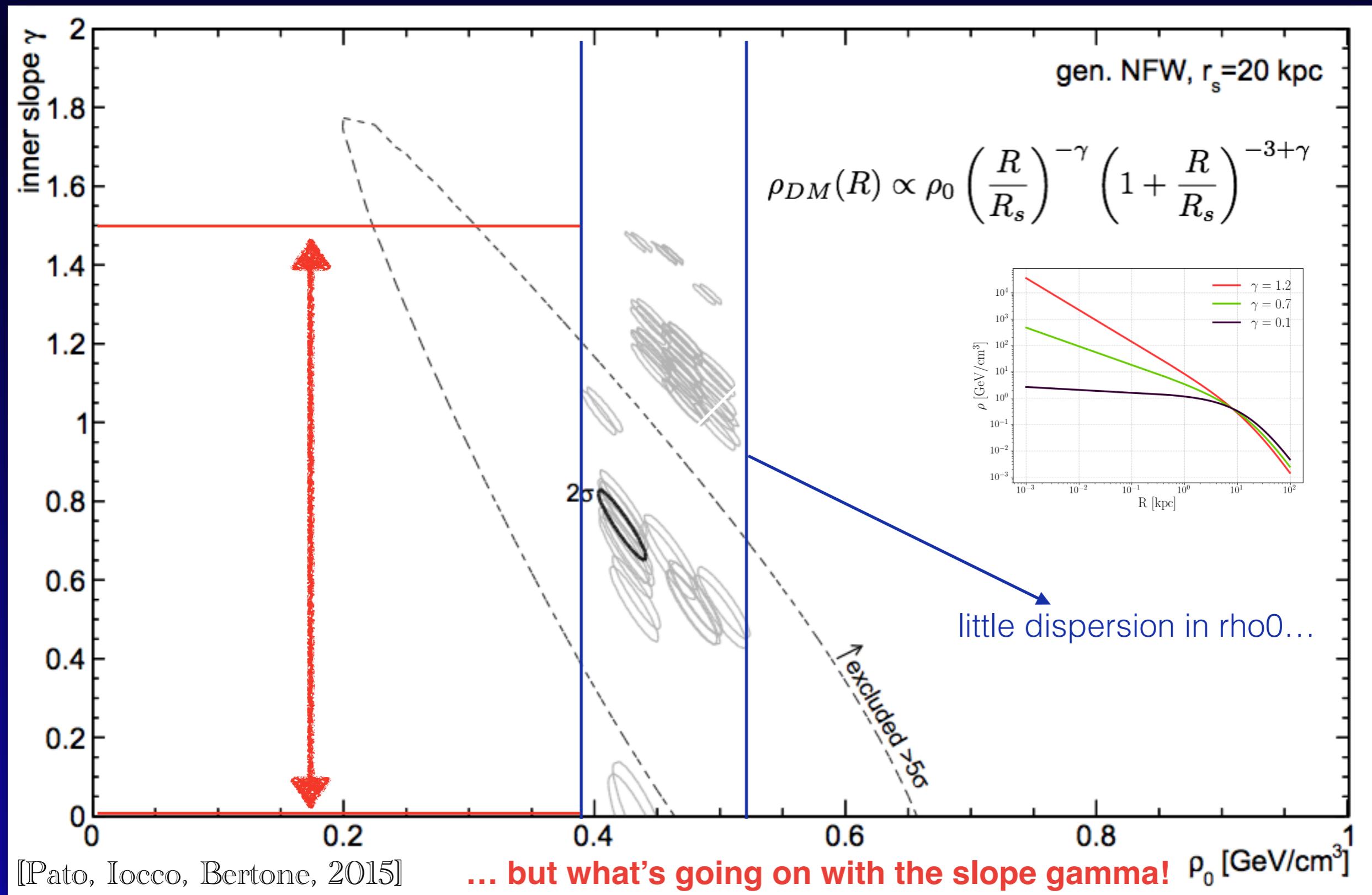


[many authors, e.g.
Iocco et al. 2011]

Systematic uncertainties (luminous component)

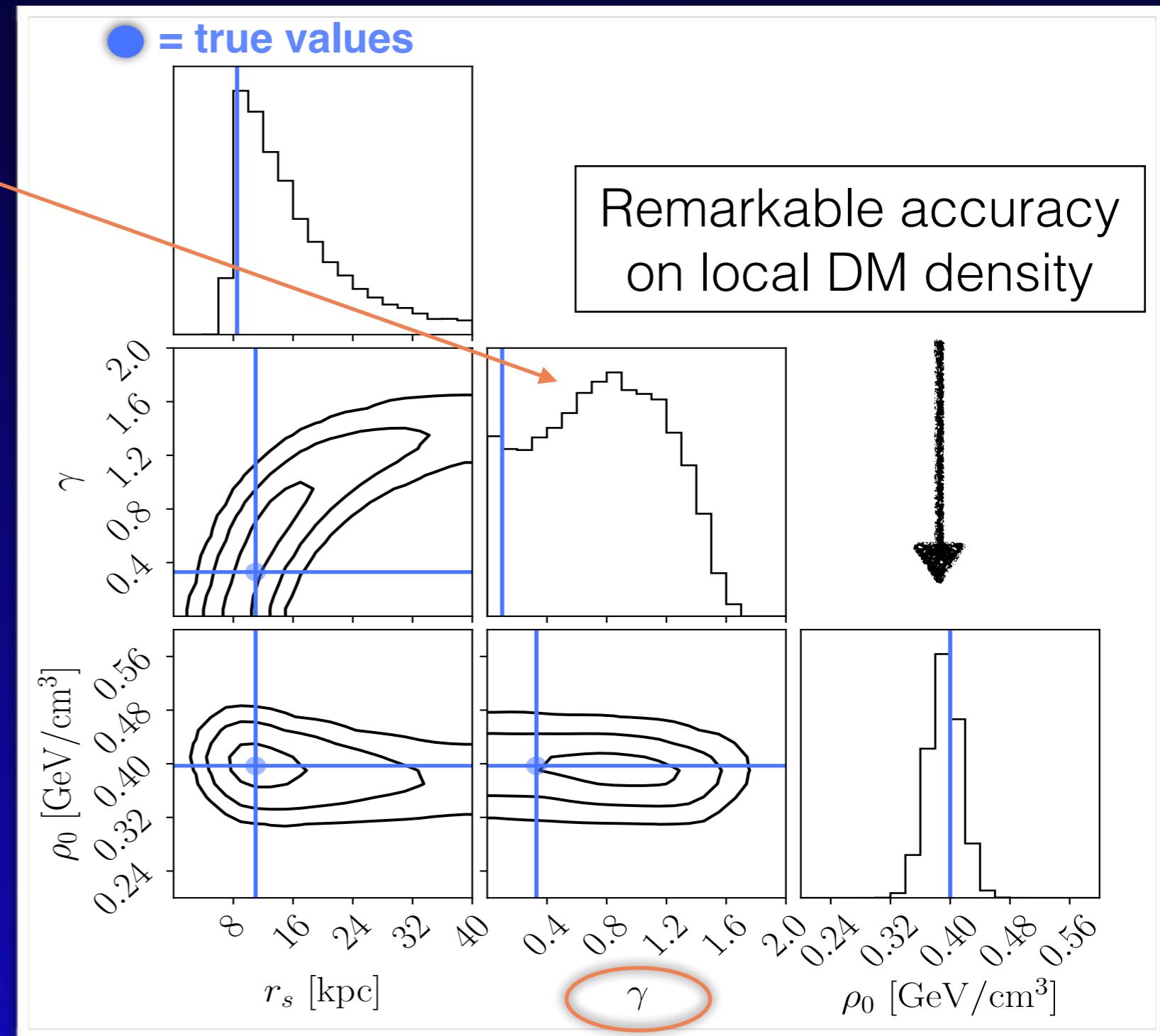
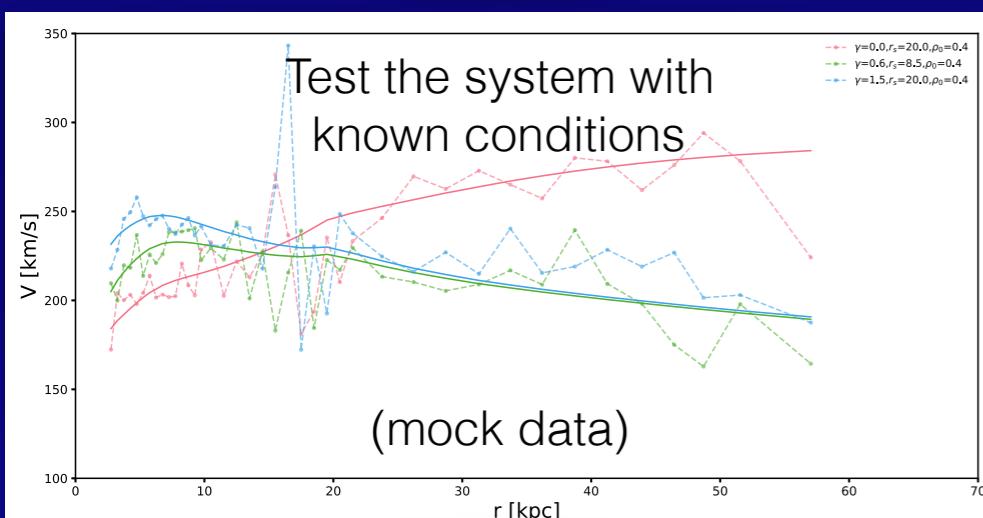
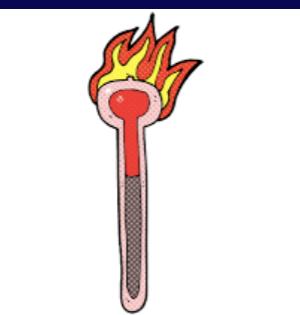


Extracting the DM density structure



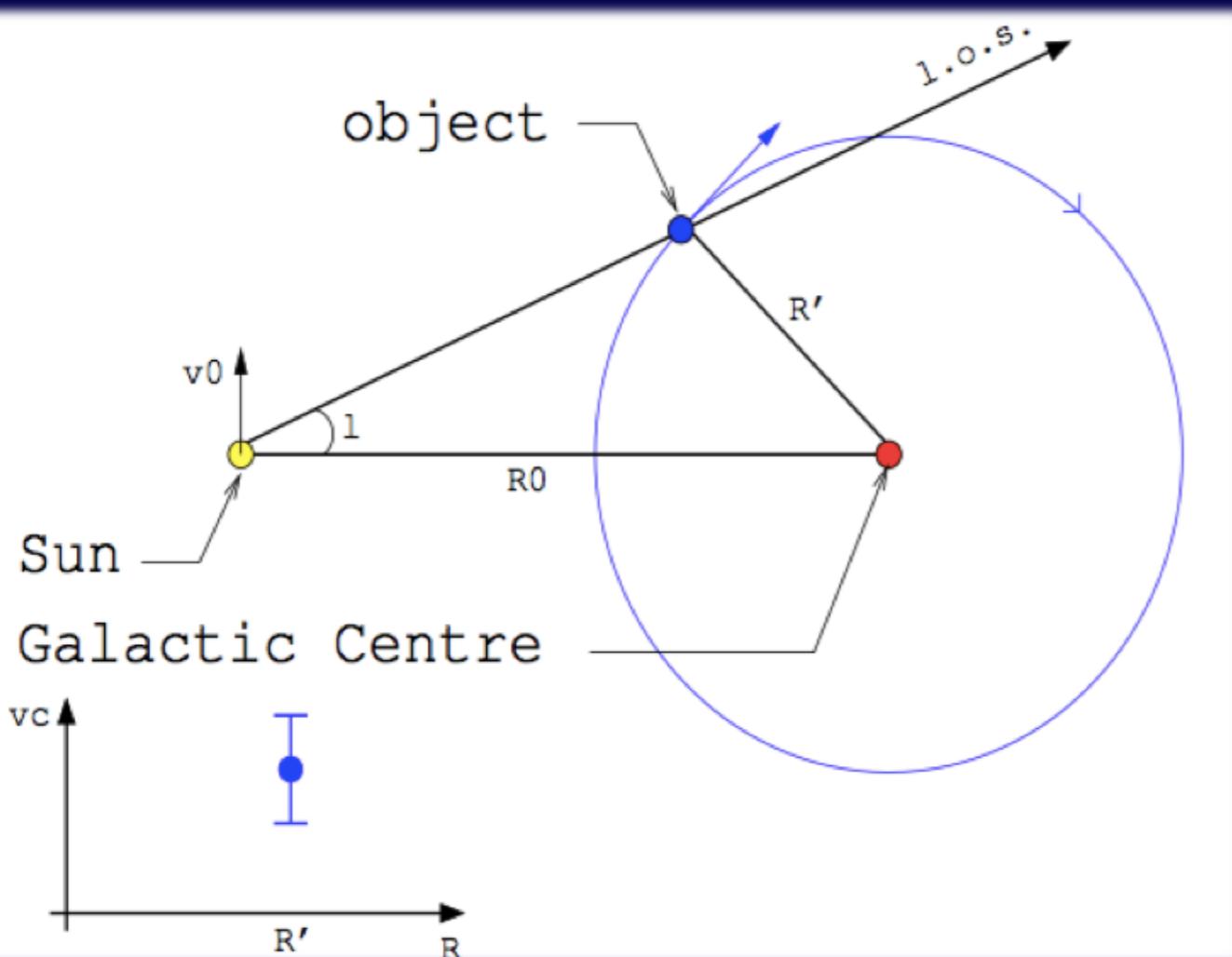
What to do of our measurement?

(Our instrument is very precise. Is it accurate?)



The Milky Way: observed rotation curve

Neglecting some quite remarkable uncertainties (for now)



$$v_{\text{LSR}}^{\text{l.o.s.}} = \left(\frac{v_c(R')}{R'/R_0} - v_0 \right) \cos b \sin \ell$$

observing tracers from our own position,
transforming into GC-centric reference frame

Uncertainties on (R_0, v_0)
ultimately affects our
determination of
 (ρ_0, γ)

Direct and indirect searches of WIMP DM *complementary to colliders*

Direct detection:

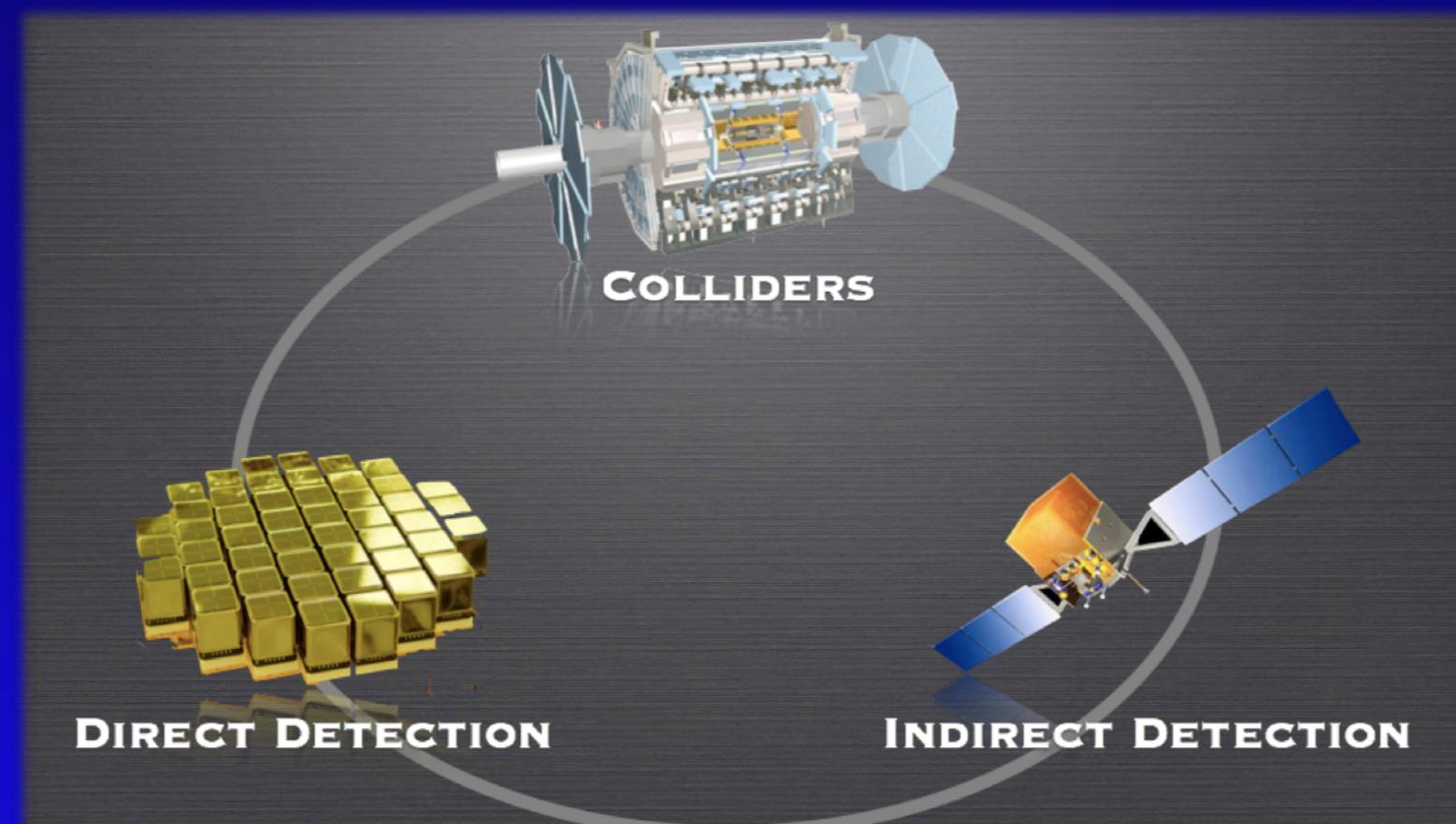
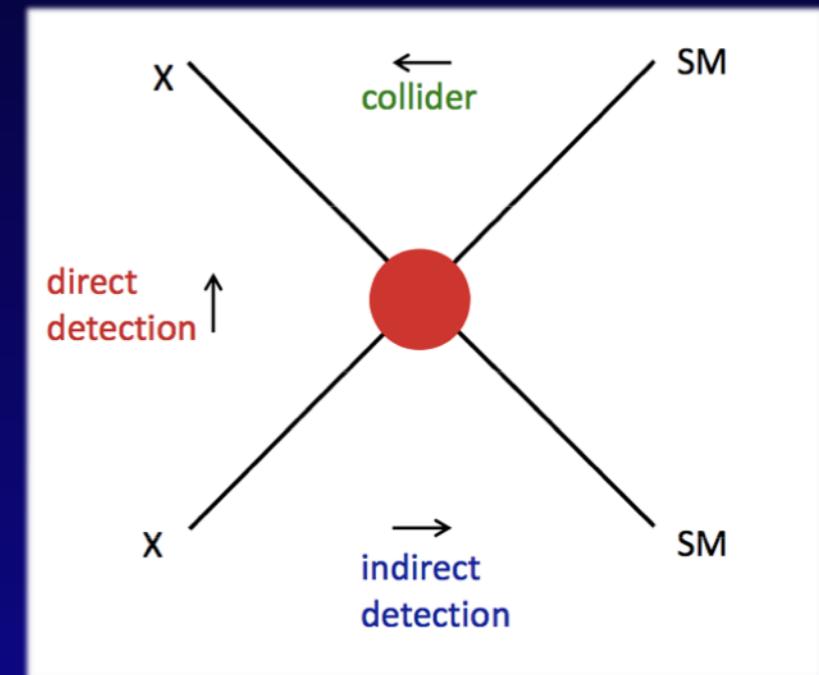
DM scattering against nuclei, recoil

Indirect detection:

Annihilation in astrophysical envir.

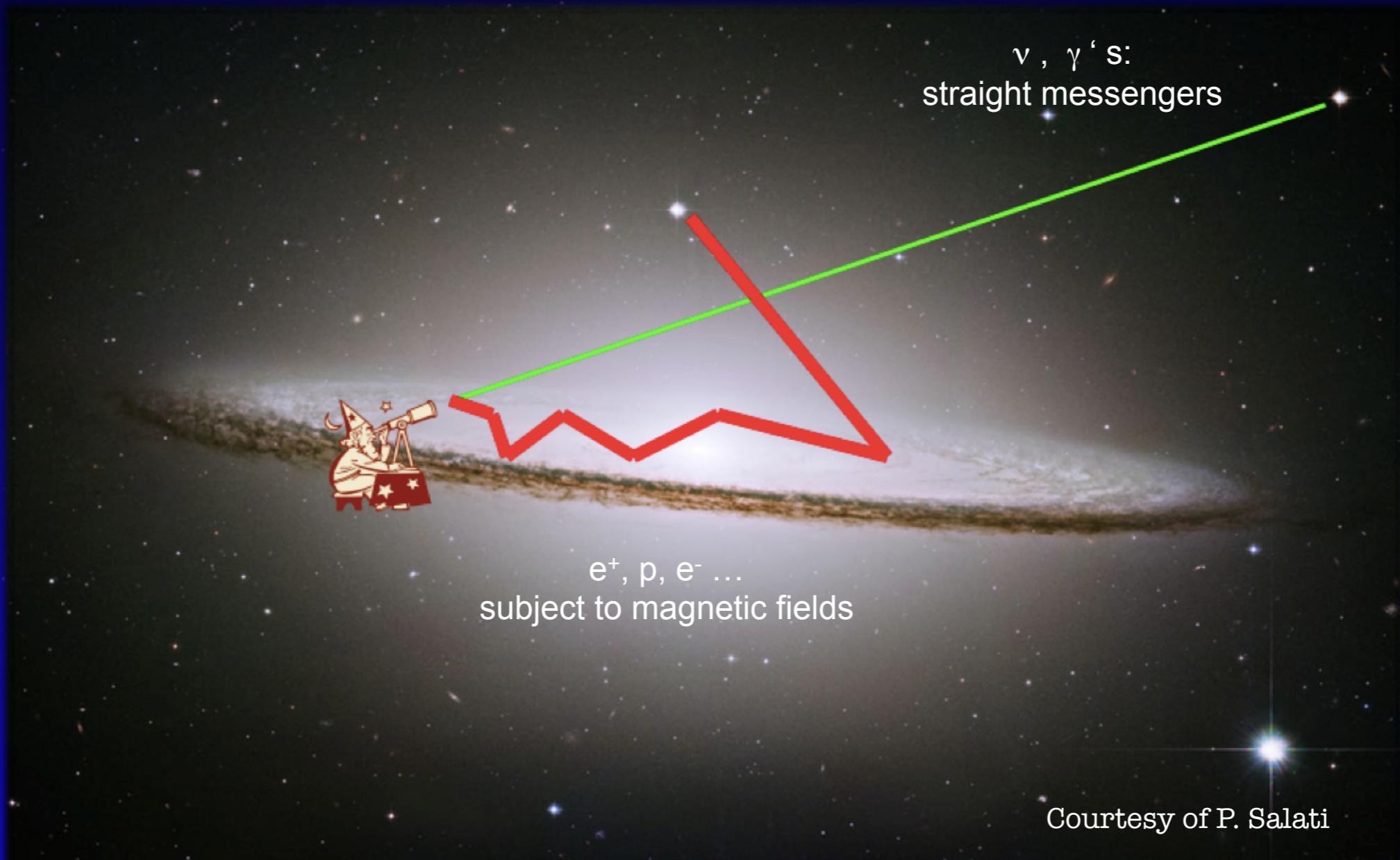
Observation of SM products of annih.

Production at LHC



Indirect Detection: principles and dependencies

$\chi + \chi \rightarrow q\bar{q}, W^+W^-, \dots \rightarrow \gamma, \bar{p}, \bar{D}, e^+ & \nu's$



Courtesy of P. Salati

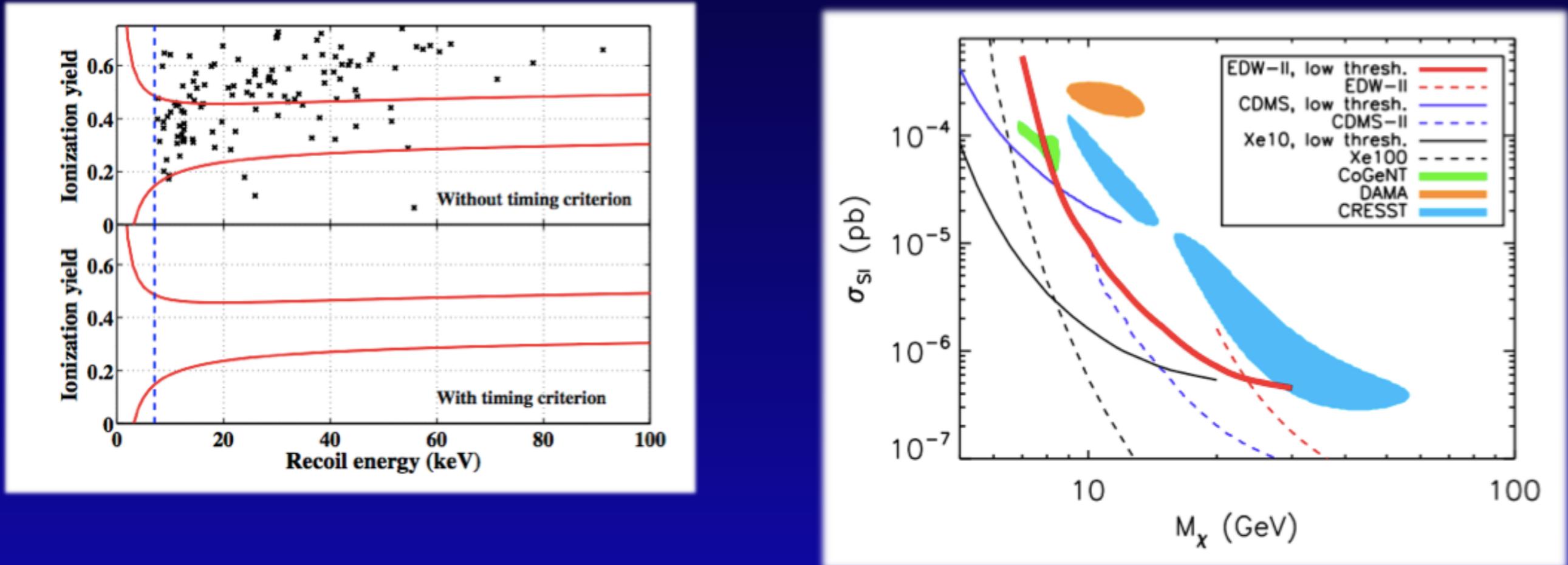
$$F_i \propto \frac{1}{4\pi d^2} B_i \frac{\langle \sigma v \rangle}{m_\chi} \int \rho^2(r) dV$$

Direct Detection: principles and dependencies (to go...)

from this



to this



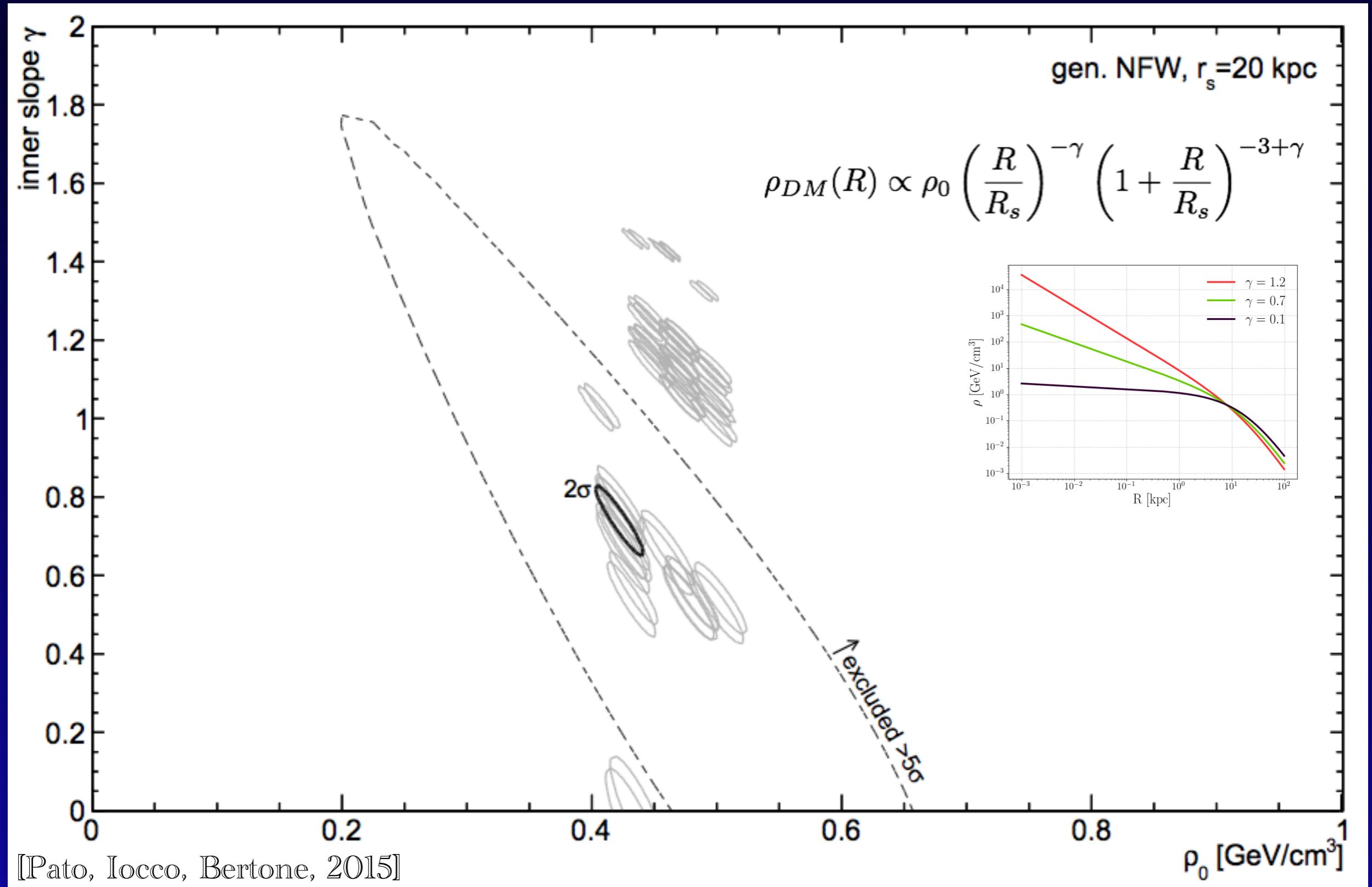
you need this

$$\frac{dR}{dE} \propto \frac{1}{\mu^2} \frac{\sigma_\chi}{m_\chi} \rho_0 \eta(v, t)$$

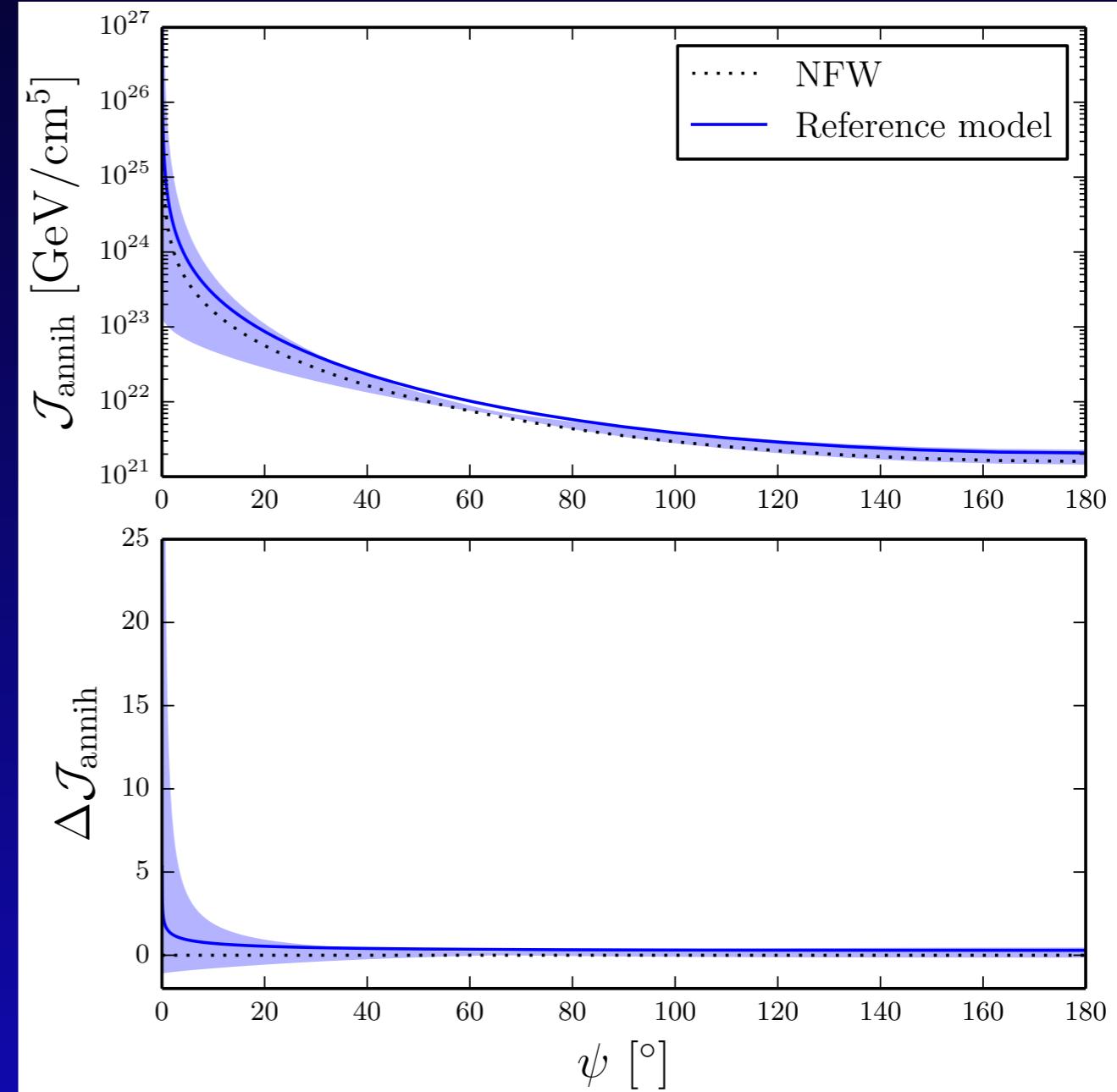
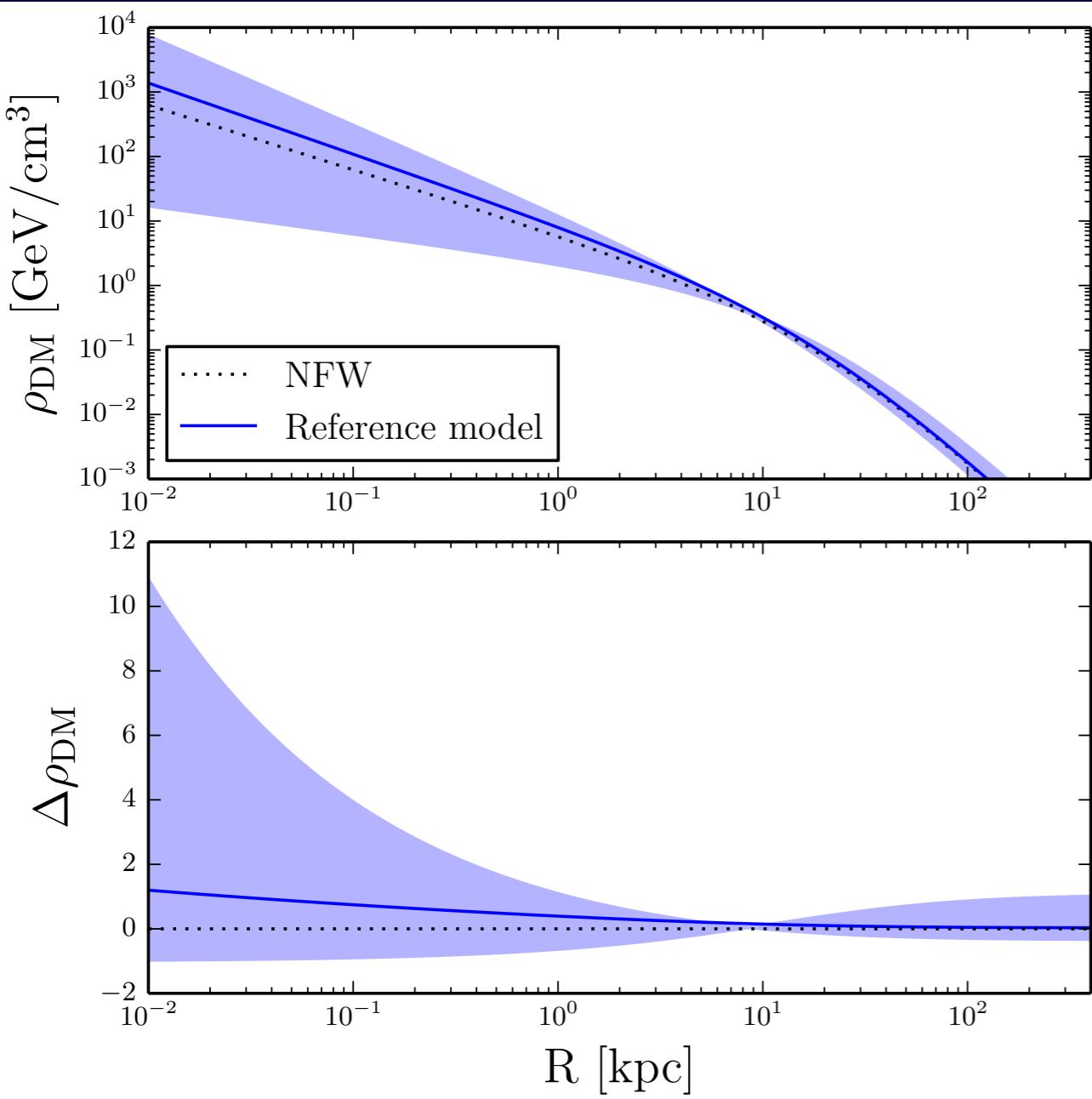
SEE TALK BY
M. YAMASHITA

SEE TALK BY
G. GELMINI

Extracting the DM density structure

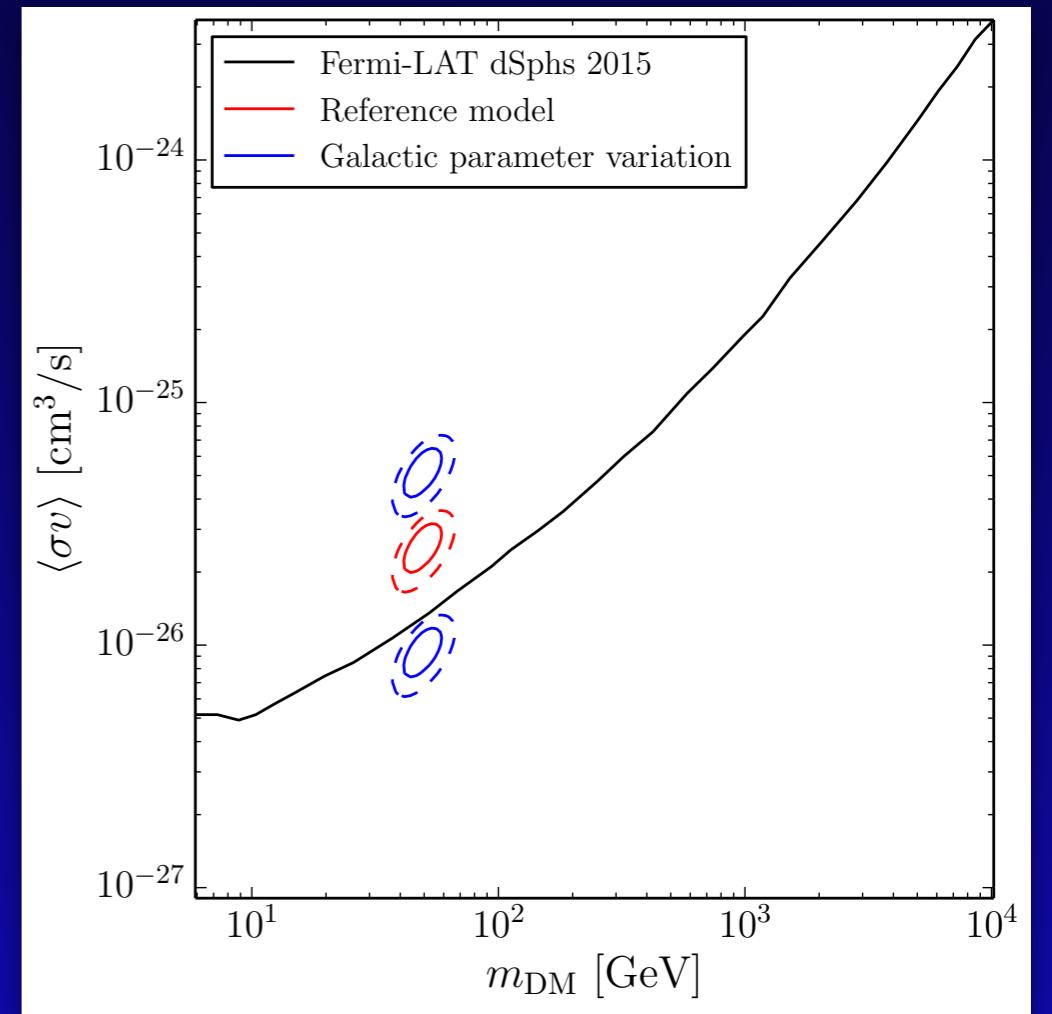
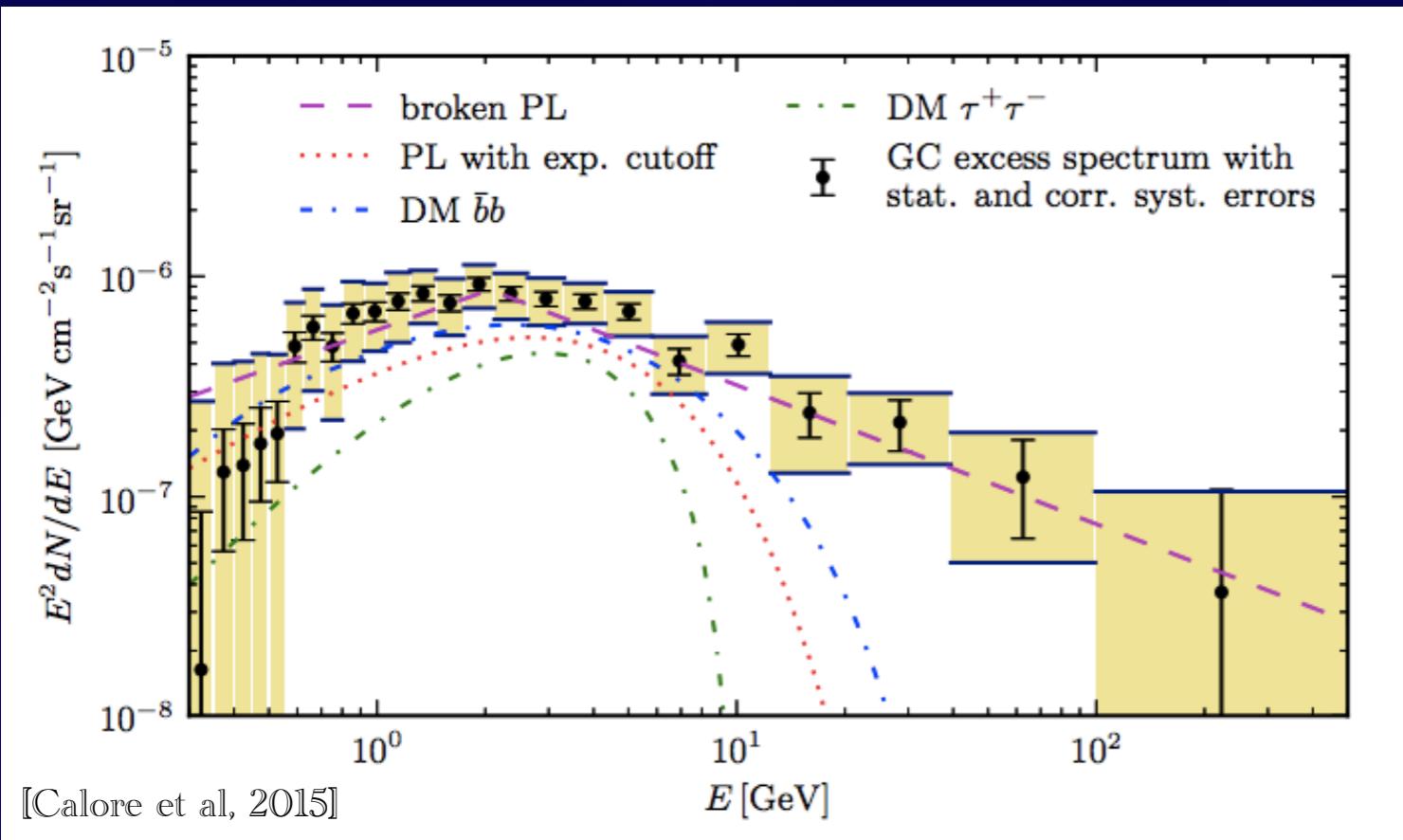


But do Galactic uncertainties affect PP, for real?

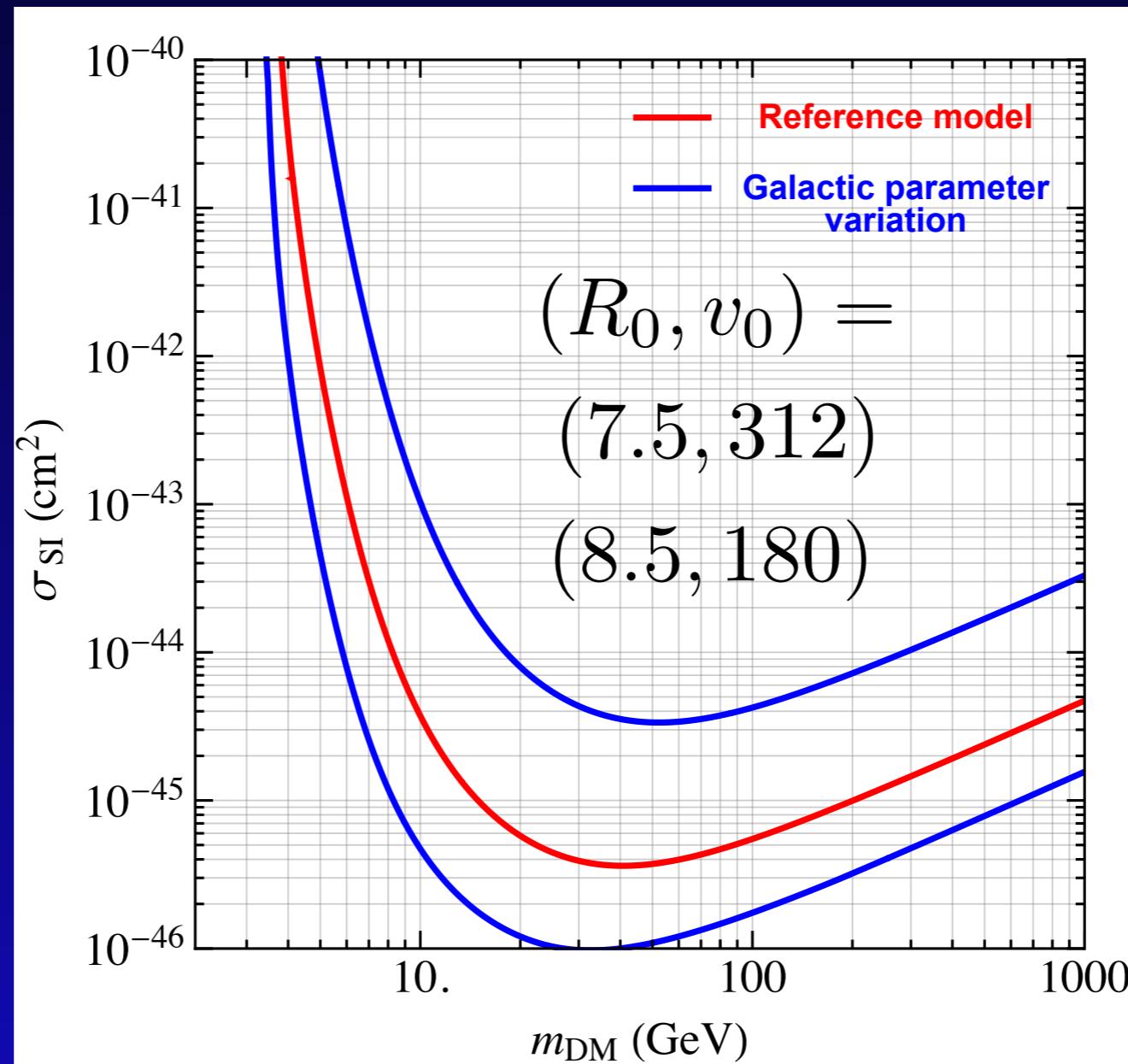


$$J_{\text{annih}} \propto \int_{\text{los}} \rho^2(r) dV$$

It is well known that uncertainties affect inDirect
(some more, some less) and its interpretation



It is well known that uncertainties affect Direct Detection



Current LUX limits, but varying astrophysical uncertainties

The effect of astrophysical uncertainties on the determination of new physics

Uncertainties accounted for:

Calore analysis:

observed GC signal
(only stat. on gamma flux)

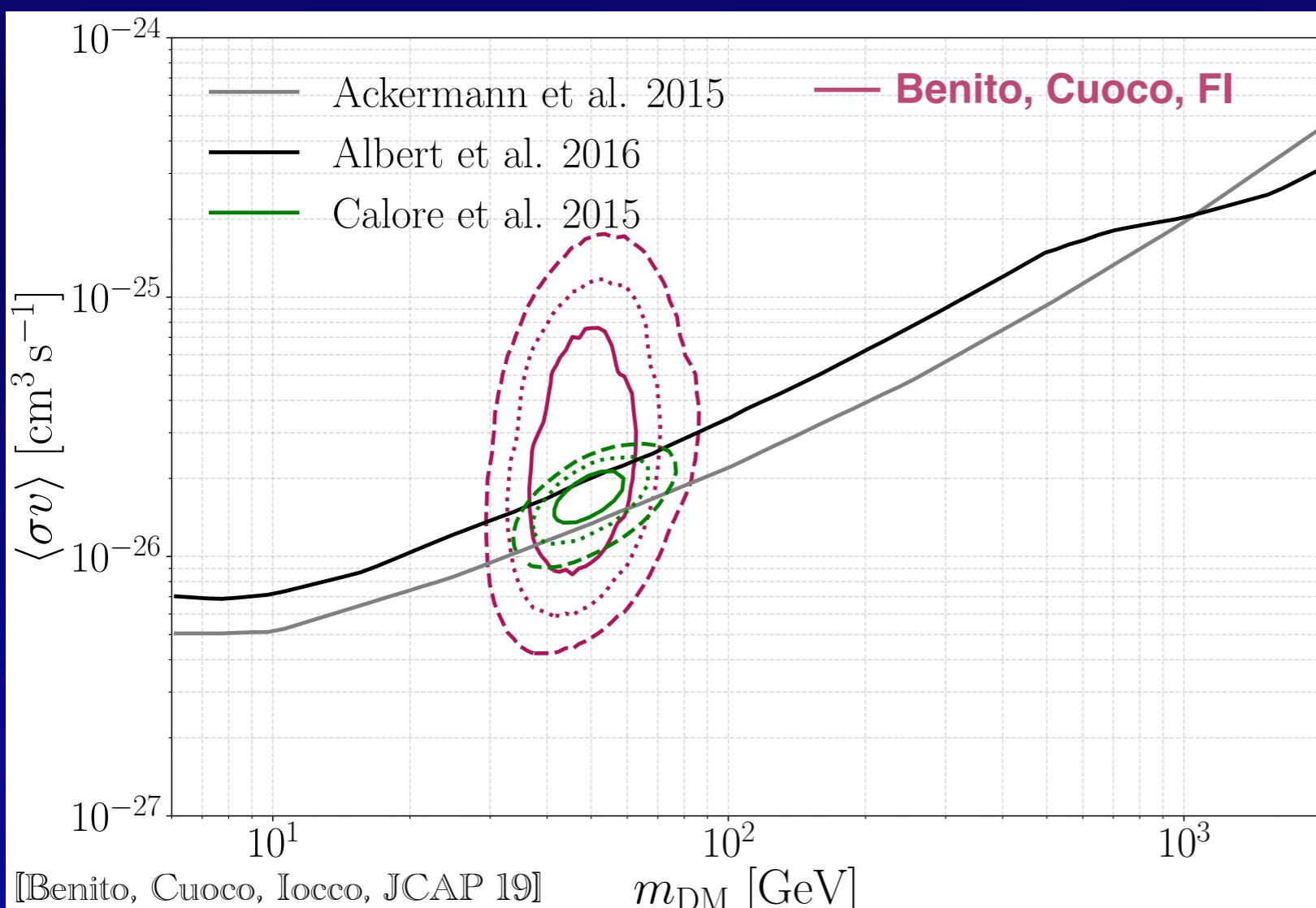
This analysis:

observed GC signal
+
DM density profile
(Gal. Param. + Morphologies + stat)

Ready-to-use likelihood publicly available @

[https://github.com/mariabenitocst/
UncertaintiesDMinTheMW](https://github.com/mariabenitocst/UncertaintiesDMinTheMW)

with Gaia-era
(R0,v0) determination,
update in progress



Let's quantify this effect in a specific case:
Singlet Scalar DM

$$V = \mu_H^2 |H|^2 + \lambda_H |H|^4 + \mu_S^2 S^2 + \lambda_S S^4 + \lambda_{HS} |H|^2 S^2$$

$$v_H = 246 \text{ GeV} \quad \langle S \rangle = 0$$

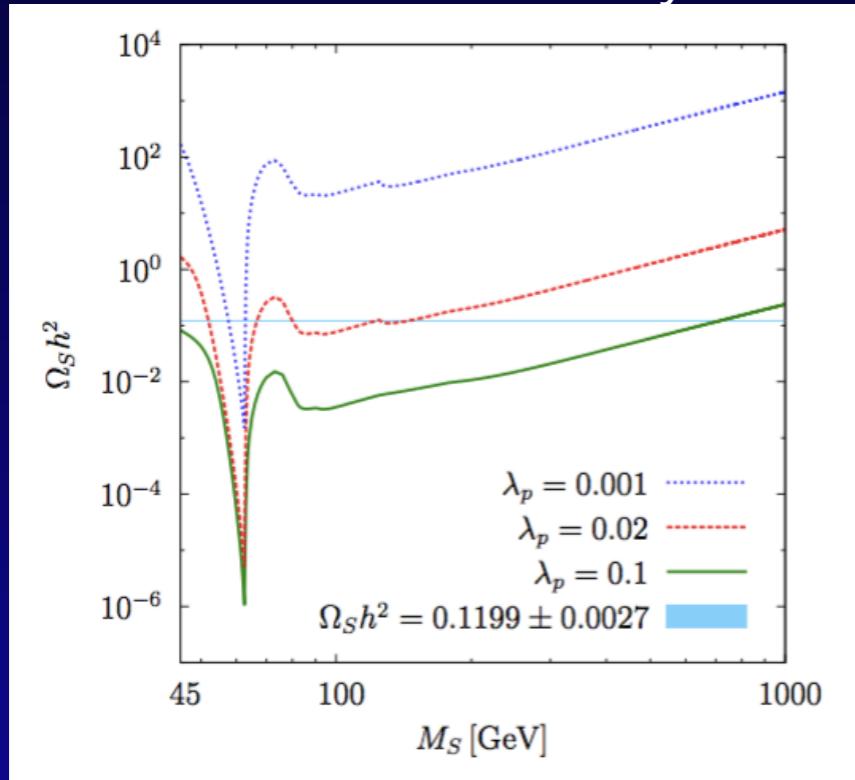
$$m_S^2 = 2 \mu_S^2 + \lambda_{HS} v_H^2$$

“WIMP phenomenology” entirely dictated by the
Higgs coupling and physical DM mass.

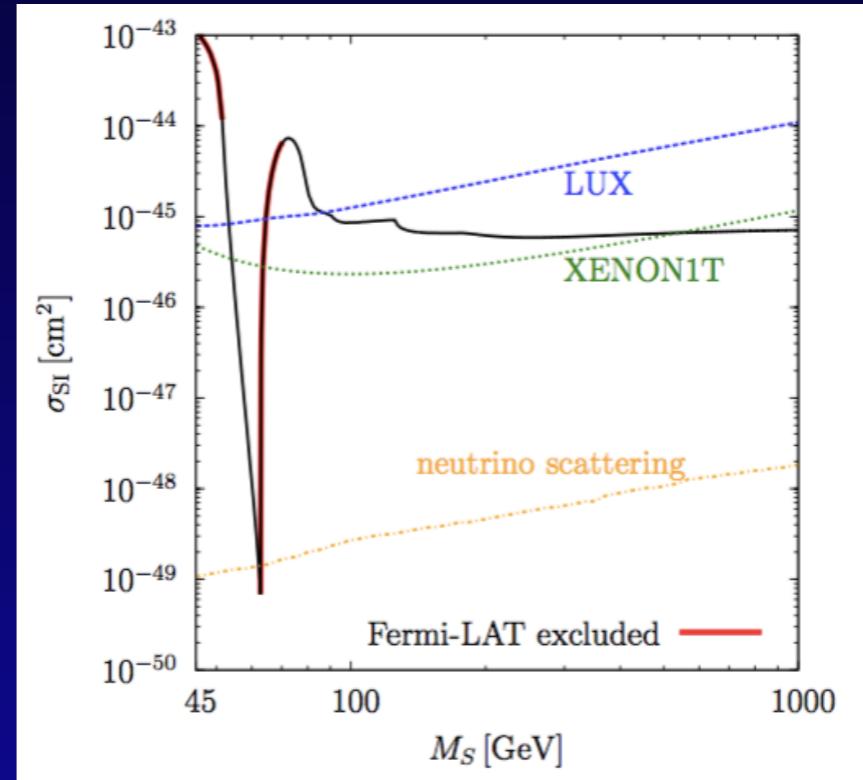
Singlet Scalar DM

Constraints and interplay of experiments

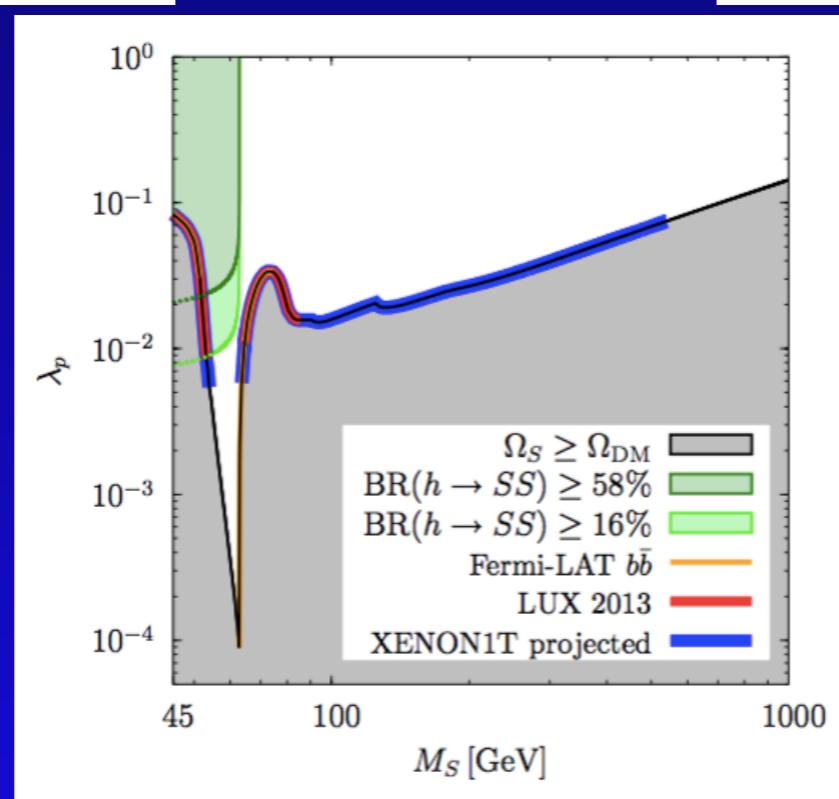
Relic density



Direct detection



Combined

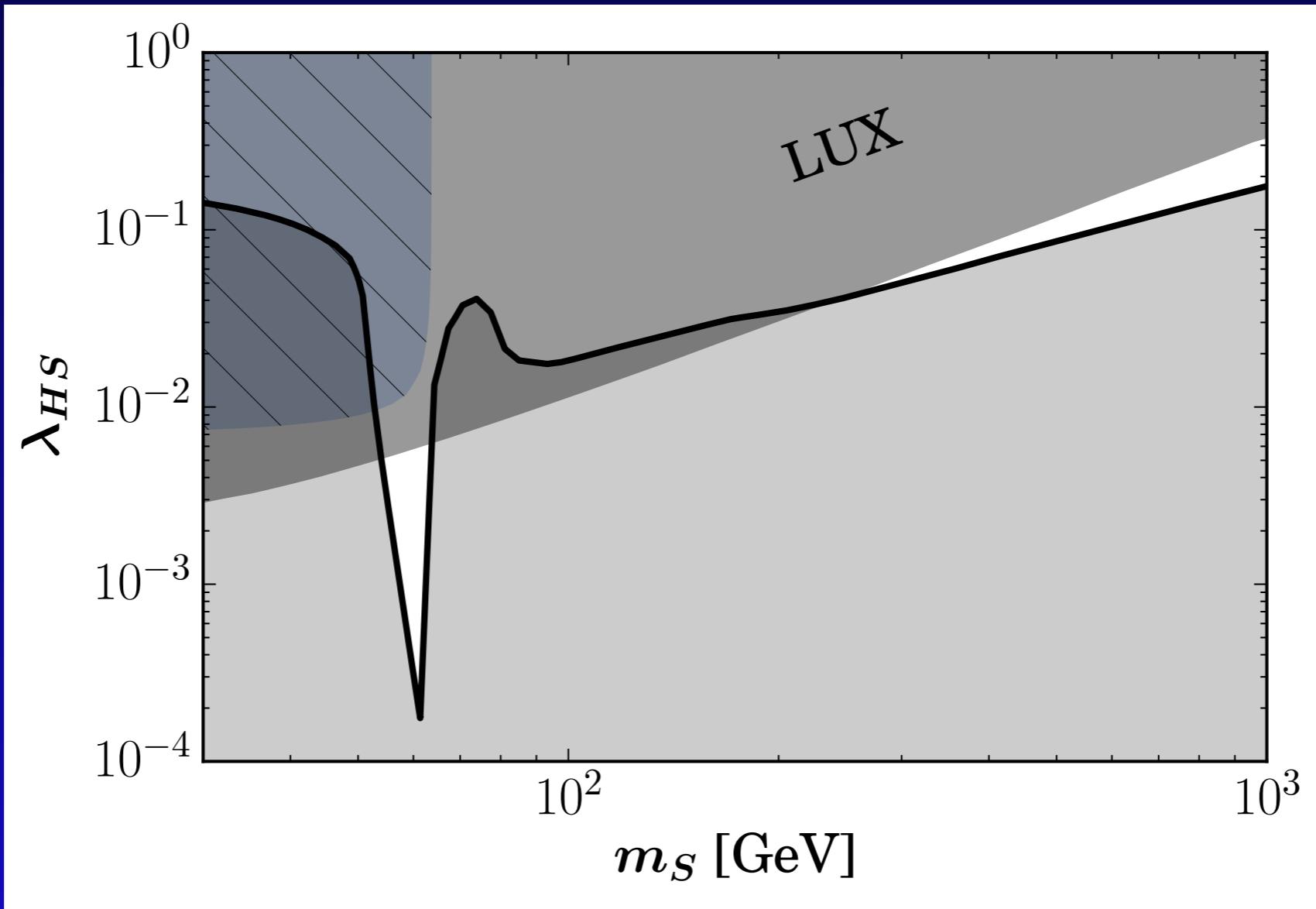


[Duerr et al, 2015]

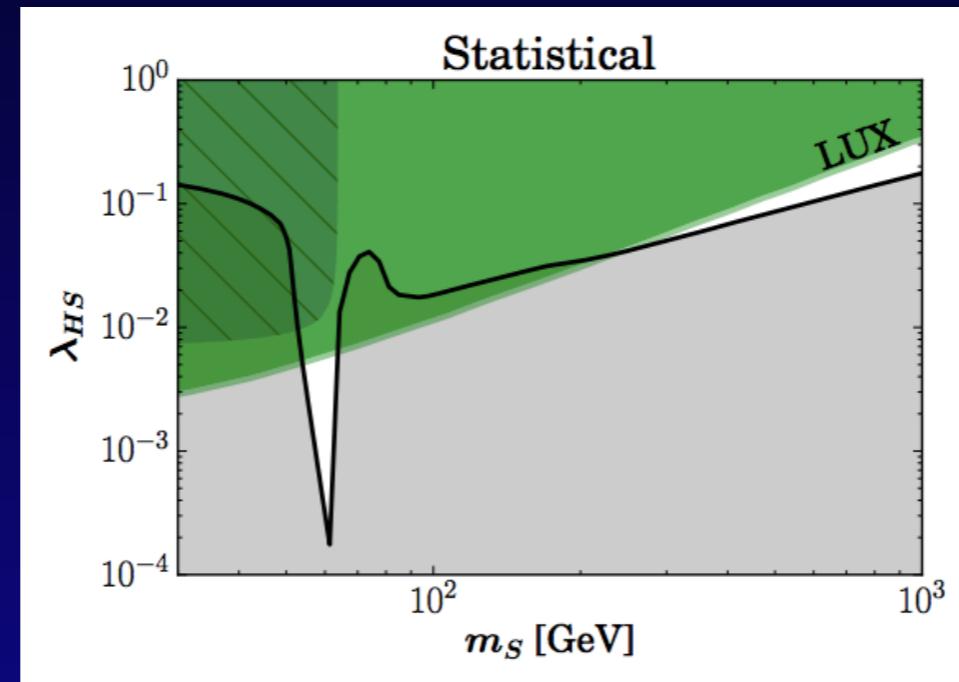
Singlet Scalar DM

Constraints and interplay of experiments

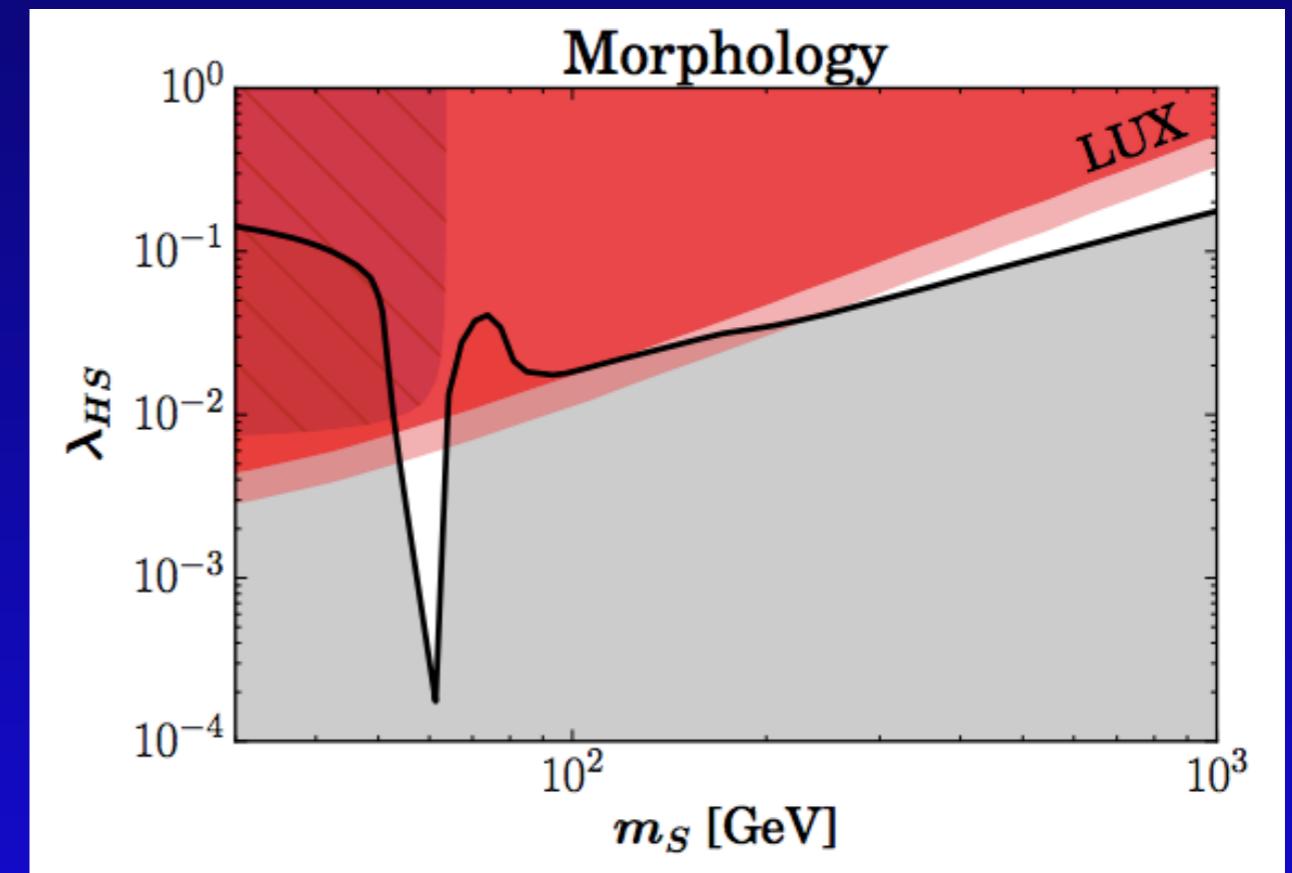
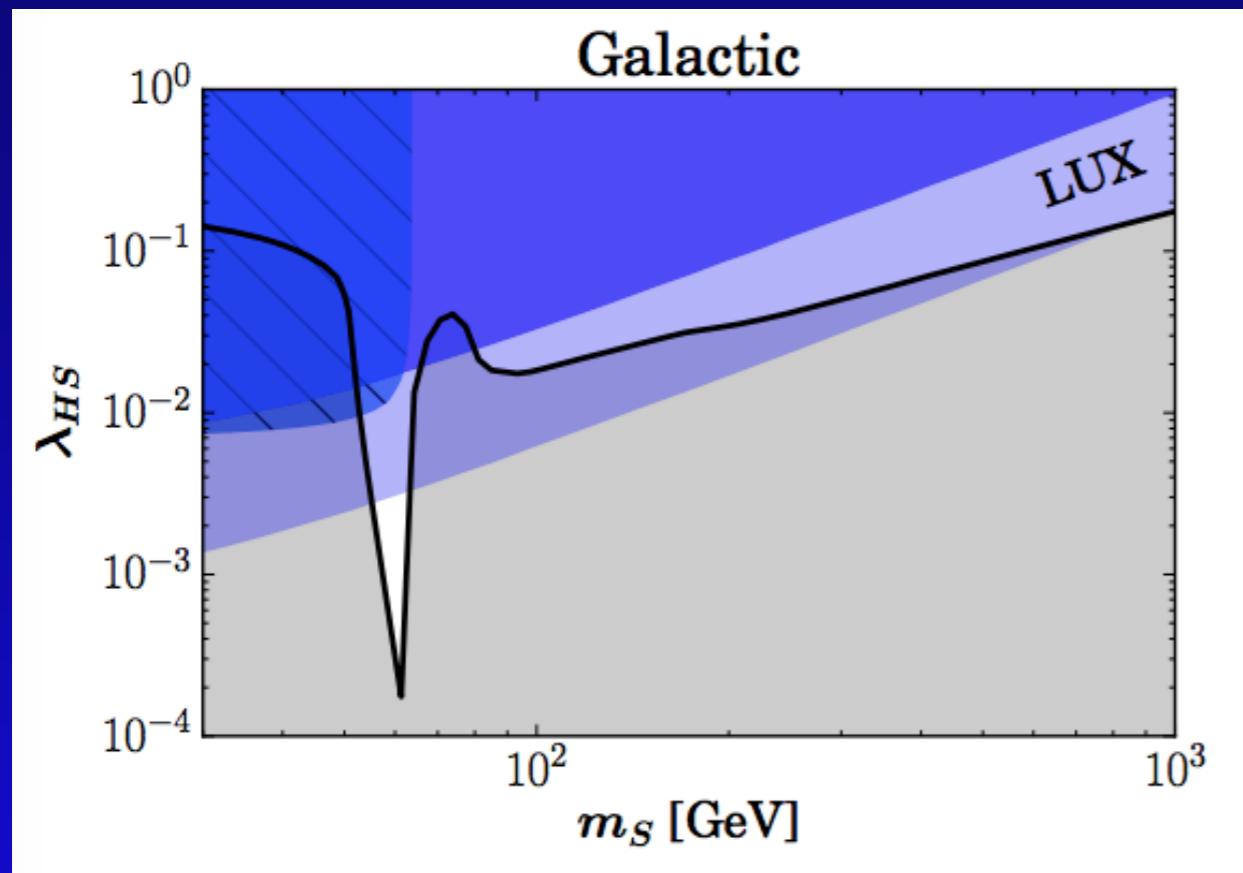
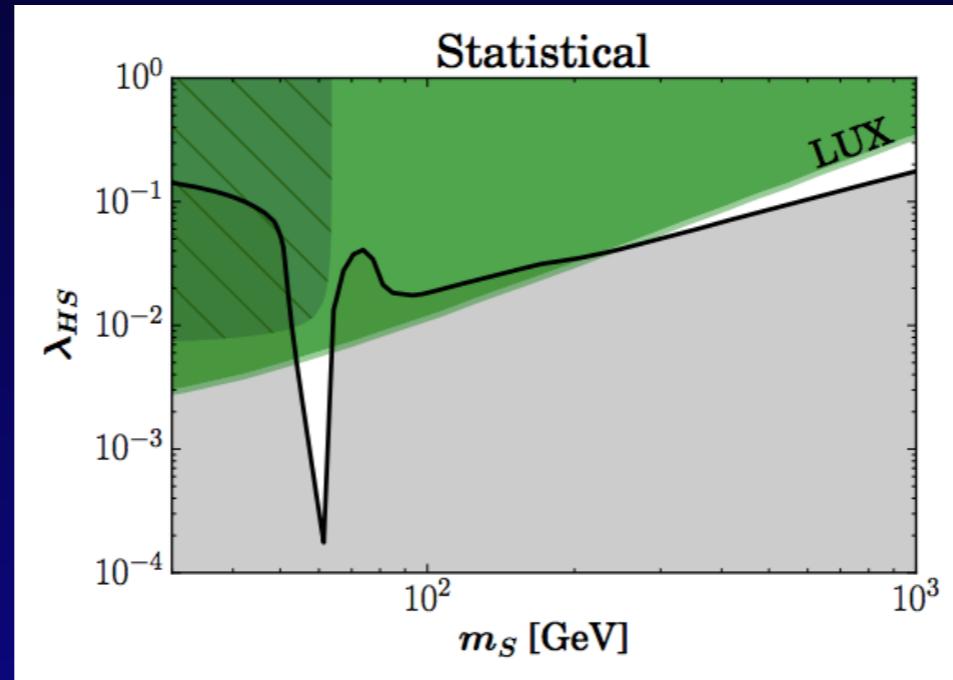
$$V = \mu_H^2 |H|^2 + \lambda_H |H|^4 + \mu_S^2 S^2 + \lambda_S S^4 + \lambda_{HS} |H|^2 S^2$$



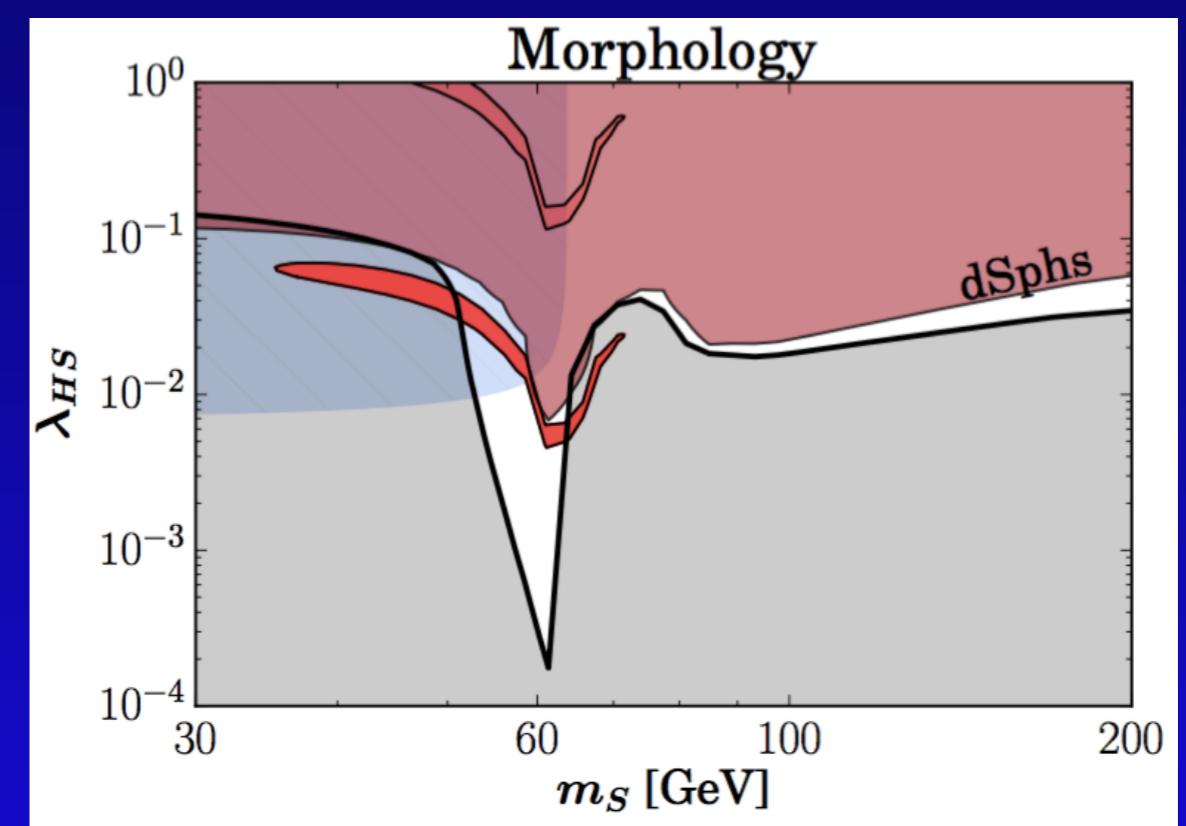
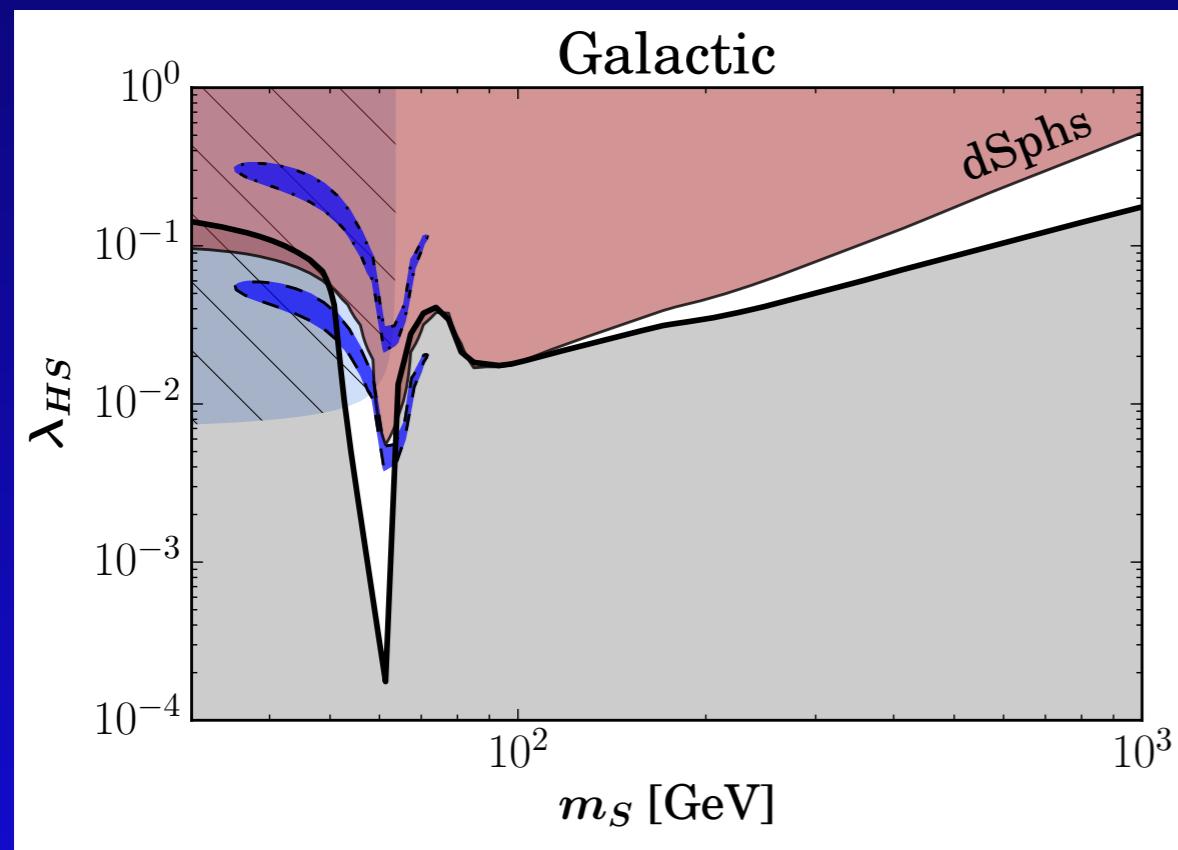
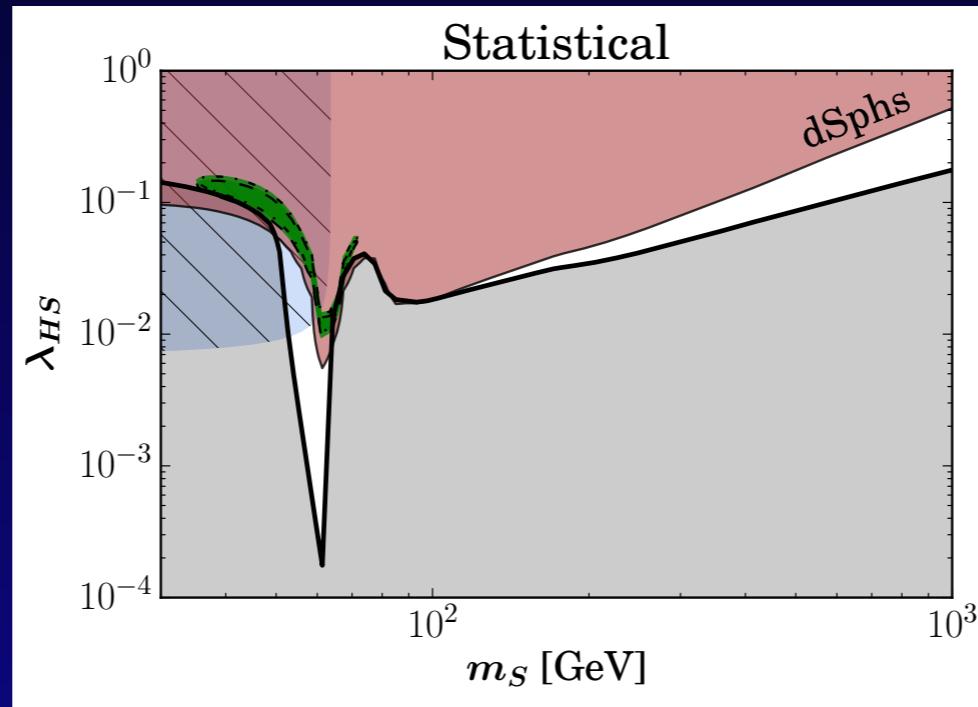
Let's look at the effect of astrophysics uncertainties: Direct Detection



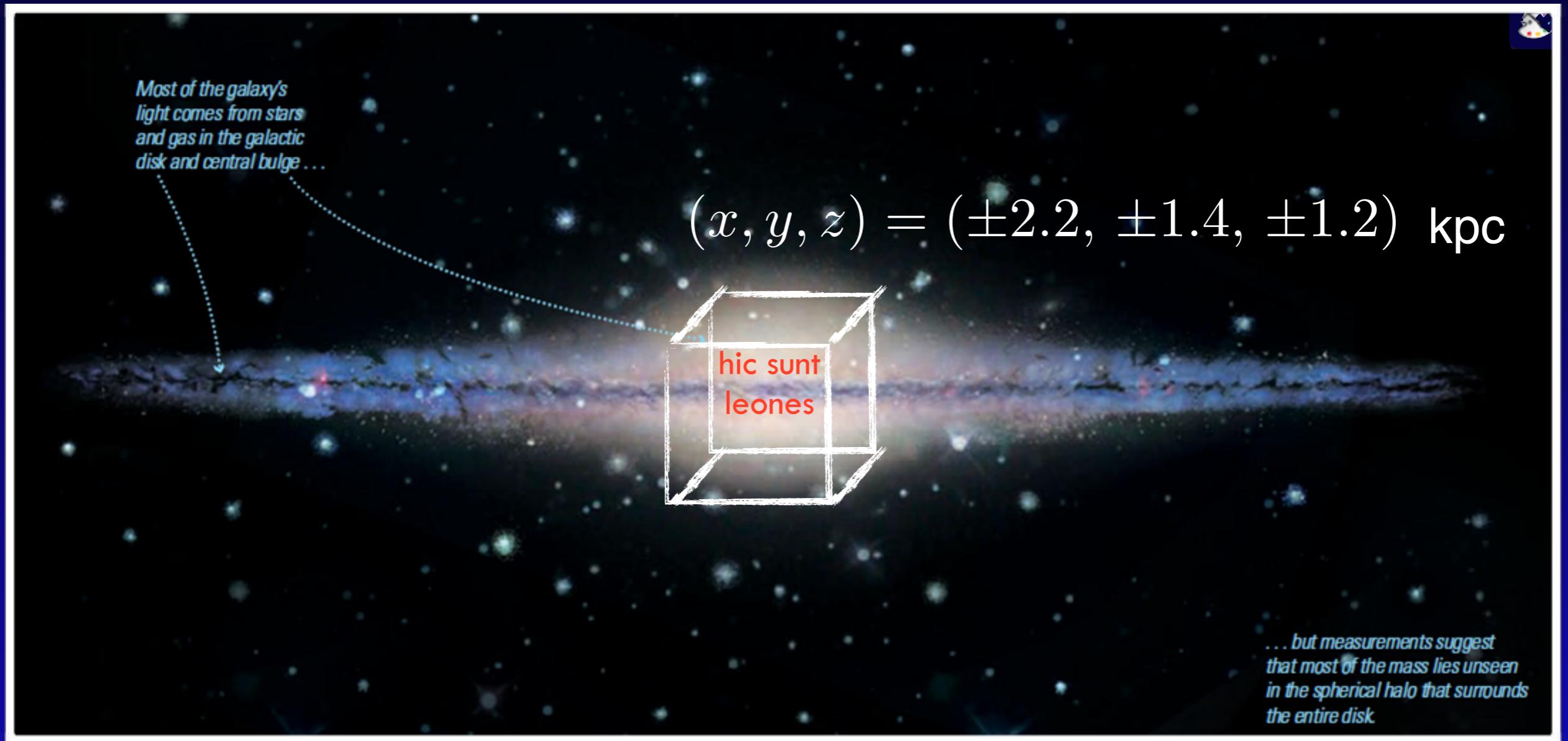
Let's look at the effect of astrophysics uncertainties: Direct Detection



Let's look at the effect of astrophysics uncertainties: Indirect Detection



Galactic Center: a beast of its own



Total mass

$$M_{total} = (1.85 \pm 0.05) \times 10^{10} M_{\odot}$$

Portail +

MNRAS 465 (2017)

Stellar mass

$$M_*^i = \int_{box} \rho_*^i(x, y, z) dV$$

[Iocco & Benito] PDU 15 (2017)

Methodology: Allowed DM mass

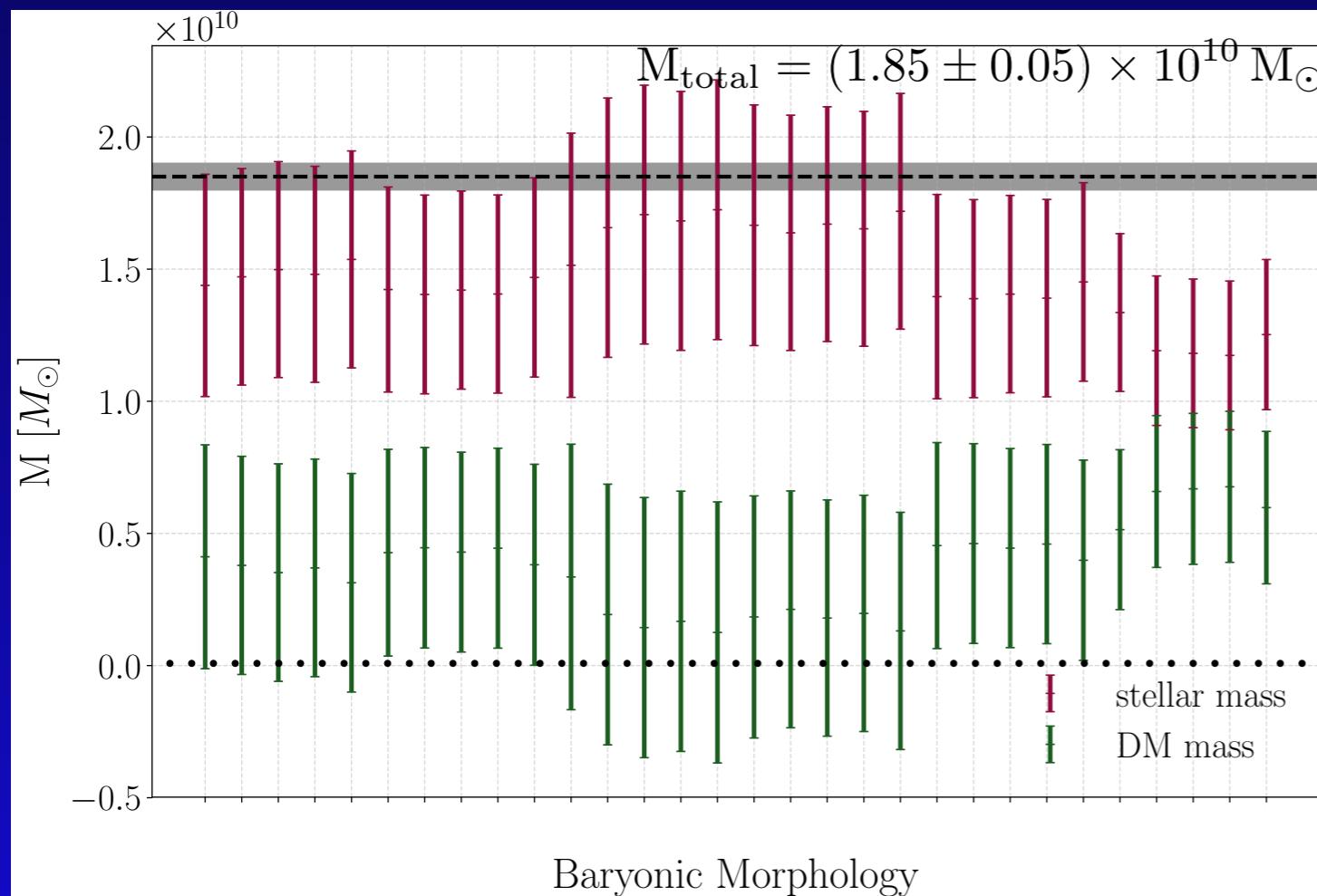
$$M_{\text{total}} - M_*^i = M_{\text{DM}}^i$$

$$\sigma_{M_{\text{DM}}} = \sqrt{\sigma_{M_{\text{total}}}^2 + \sigma_{M_*^i}^2}$$

$$M_* = (1.1 - 1.7) \times 10^{10} M_\odot$$

$$M_{\text{DM}} = (0.1 - 0.7) \times 10^{10} M_\odot$$

DM mass corresponds to 7-37%



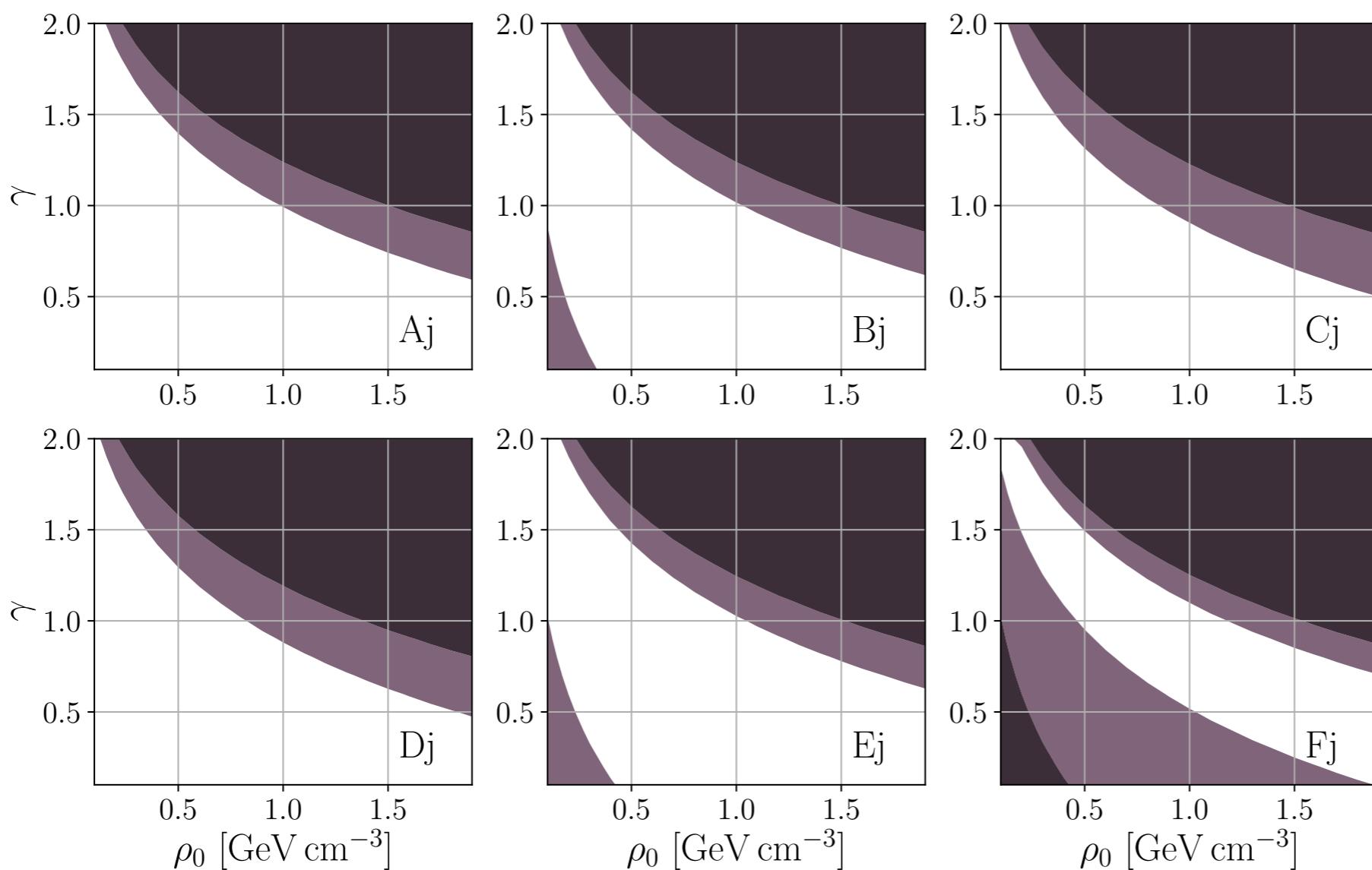
gNFW density profile

$$\rho_{\text{DM}}(r) = \rho_0 \left(\frac{R_0}{r} \right)^\gamma \left(\frac{R_s + R_0}{R_s + r} \right)^{3-\gamma}$$

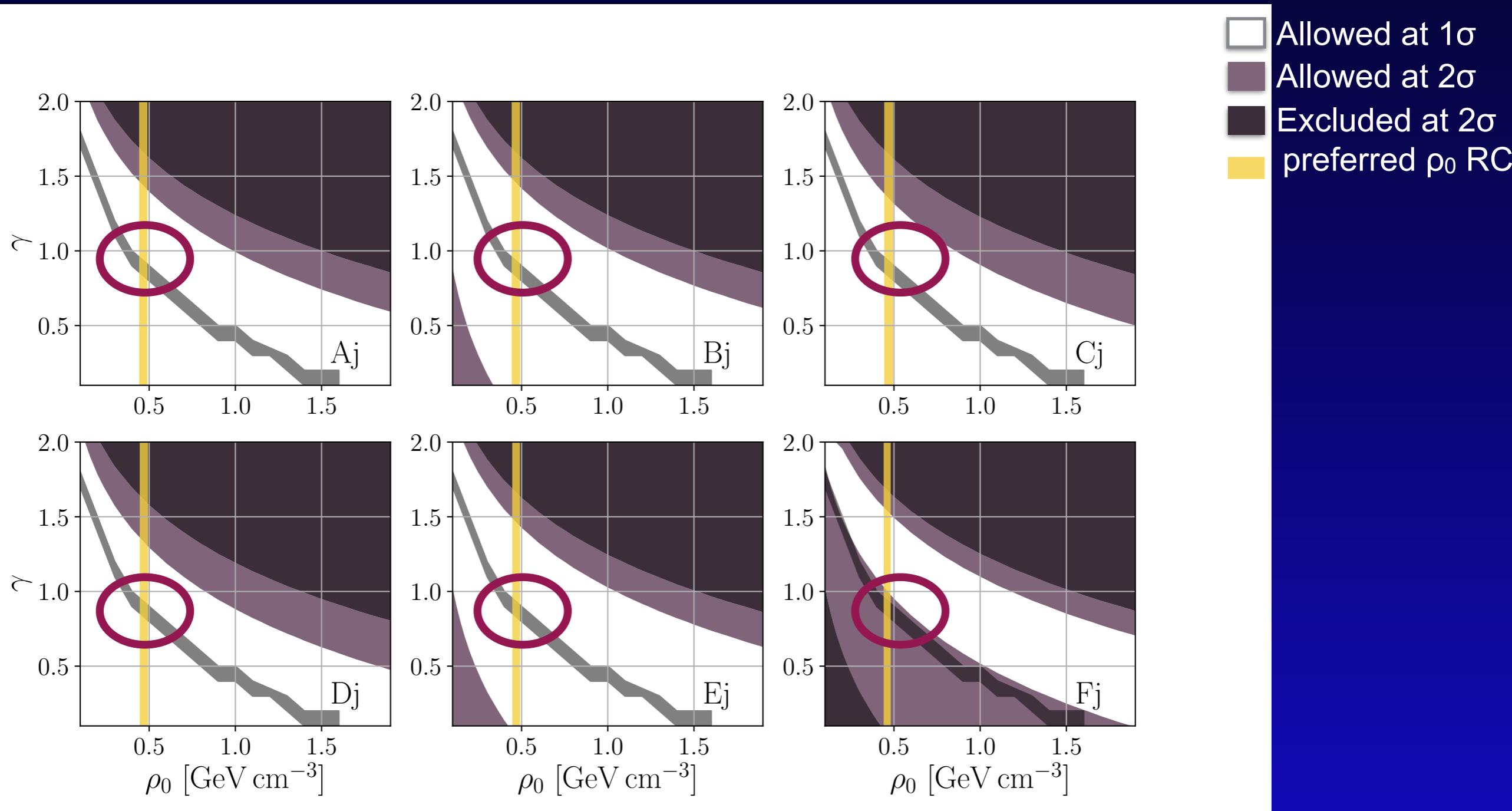
Study parameter space that gives a mass in excess or deficit with respect to the allowed DM mass

Galactic Bulge Region

Results: varying bulge morphology



Galactic Bulge Region and RC curve compatibility



$$M_{\text{DM}} = (0.32 \pm 0.05) \times 10^{10} M_{\odot}$$

“the dark matter density of our model has a [...] Portail + shallow cusp or a **core in the bulge region**”

MNRAS 465 (2017)

Iocco & Benito, 2017
arXiv:1611.09861
(+ M. Benito's thesis)

- South American Dark Matter workshop
December 2-4, 2020

Third of a new series (2017, 2018)
www.ictp-saifr.org/DMw2018

Previous speakers included:

... Azadeh Fattahi
Graciela Gelmini
Christopher McCabe
Cecilia Scannapieco
Tomer Volansky ...



International Centre for Theoretical Physics
South American Institute for Fundamental Research

São Paulo,
Brazil
(not Rio de Janeiro!)

Cuncta stricte

- Determining the local DM density from actual data is possible
- RC method is accurate and precise, in spite of large range of observational systematic and statistical uncertainties.
- Slope (i.e. full profile of MW) is not very accurate, and quite depending from several systematics. (Galactic Center region further complicated.)
- Astrophysical uncertainties are actually affecting determination of PP, in virtuous interplay with collider physics, direct and indirect probes.
- Providing a ready-to-use likelihood for PP use, including astrophysical uncertainties on DM distribution

One place among the many: home The Milky Way



The road to Zeus' mansion on Olympus
The sacred path of Iberian pilgrims
An average-sized 10^{12} Msun spiral,
but the truth is...

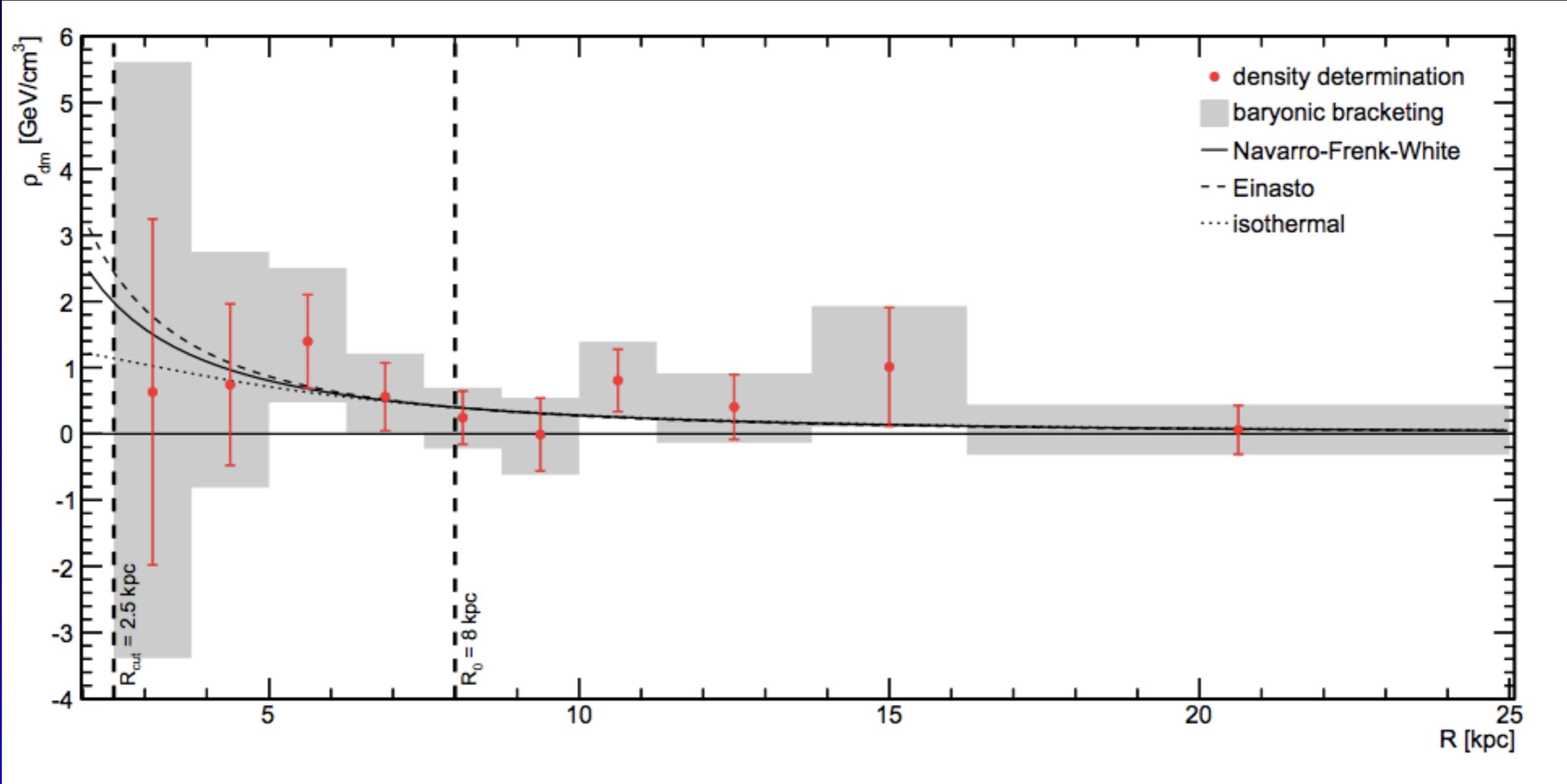


The Milky Way: observed rotation curve the data: a new compilation

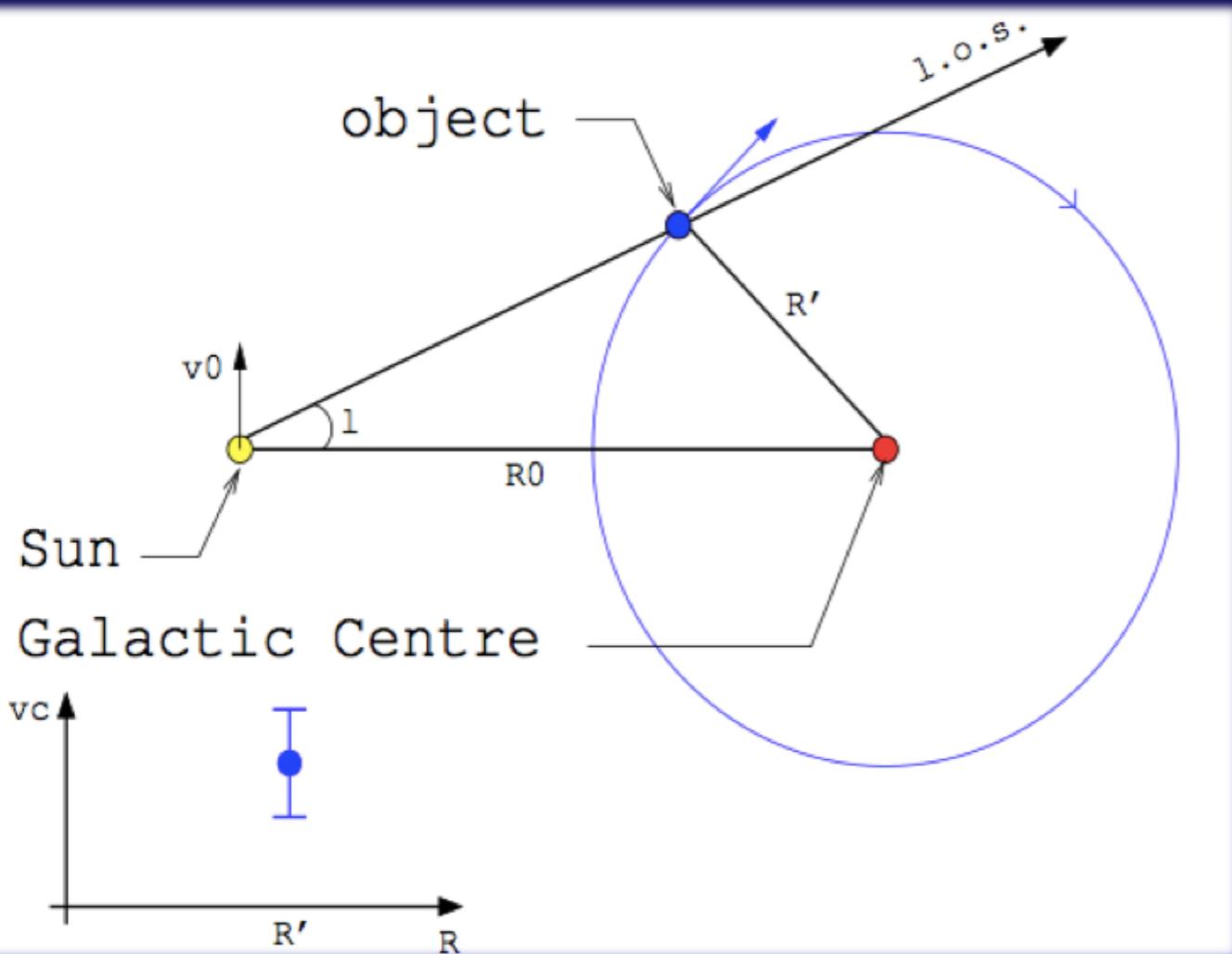
	Object type	R [kpc]	quadrants	# objects
gas	HI terminal velocities			
	Fich+ '89	2.1 – 8.0	1,4	149
	Malhotra '95	2.1 – 7.5	1,4	110
	McClure-Griffiths & Dickey '07	2.8 – 7.6	4	701
	HI thickness method			
	Honma & Sofue '97	6.8 – 20.2	–	13
	CO terminal velocities			
	Burton & Gordon '78	1.4 – 7.9	1	284
	Clemens '85	1.9 – 8.0	1	143
	Knapp+ '85	0.6 – 7.8	1	37
	Luna+ '06	2.0 – 8.0	4	272
	HII regions			
	Blitz '79	8.7 – 11.0	2,3	3
	Fich+ '89	9.4 – 12.5	3	5
	Turbide & Moffat '93	11.8 – 14.7	3	5
stars	Brand & Blitz '93	5.2 – 16.5	1,2,3,4	148
	Hou+ '09	3.5 – 15.5	1,2,3,4	274
	giant molecular clouds			
	Hou+ '09	6.0 – 13.7	1,2,3,4	30
	open clusters			
	Frinchaboy & Majewski '08	4.6 – 10.7	1,2,3,4	60
	planetary nebulae			
	Durand+ '98	3.6 – 12.6	1,2,3,4	79
	classical cepheids			
	Pont+ '94	5.1 – 14.4	1,2,3,4	245
masers	Pont+ '97	10.2 – 18.5	2,3,4	32
	carbon stars			
	Demers & Battinelli '07	9.3 – 22.2	1,2,3	55
	Battinelli+ '13	12.1 – 24.8	1,2	35
	masers			
	Reid+ '14	4.0 – 15.6	1,2,3,4	80
	Honma+ '12	7.7 – 9.9	1,2,3,4	11
	Stepanishchev & Bobylev '11	8.3	3	1
	Xu+ '13	7.9	4	1
	Bobylev & Bajkova '13	4.7 – 9.4	1,2,4	7

“Mom look, no hands!”

A non-parametric reconstruction of the DM profile



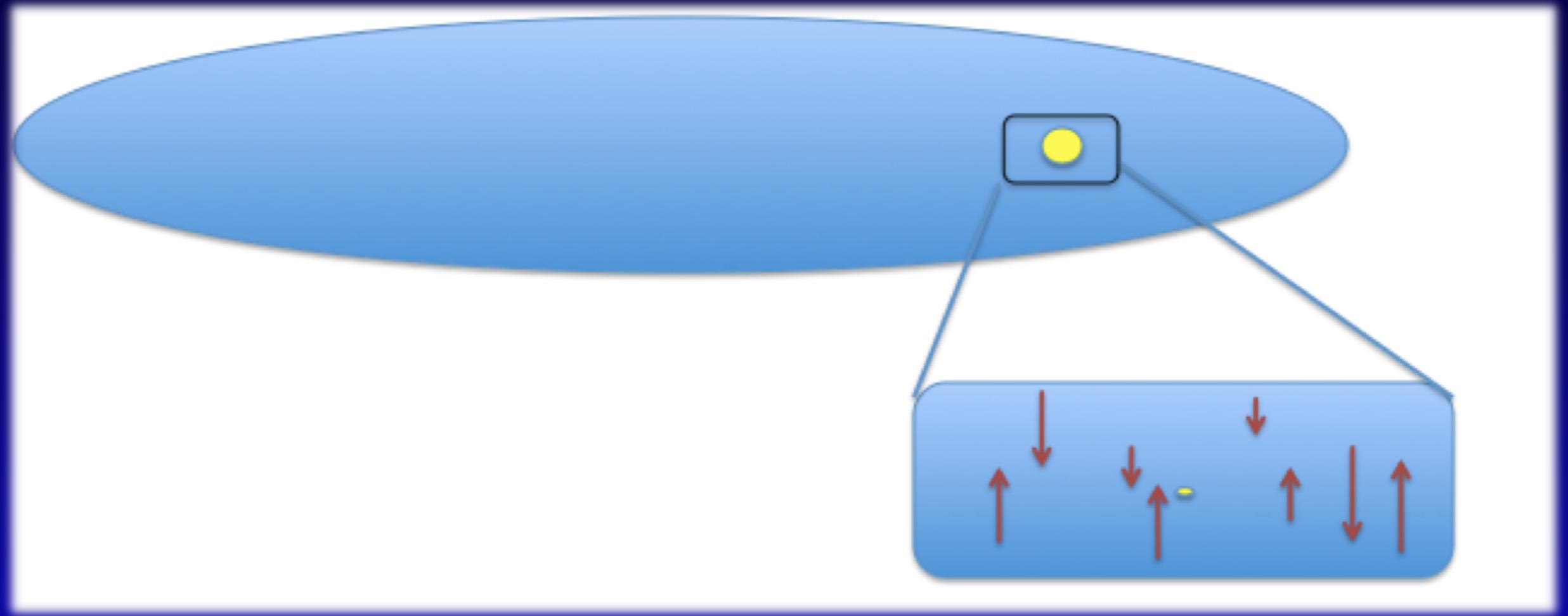
The Milky Way: observed rotation curve I. principles



$$v_{\text{L.S.R.}}^{\text{l.o.s.}} = \left(\frac{v_c(R')}{R'/R_0} - v_0 \right) \cos b \sin \ell$$

observing tracers from our own position,
transforming into GC-centric reference frame

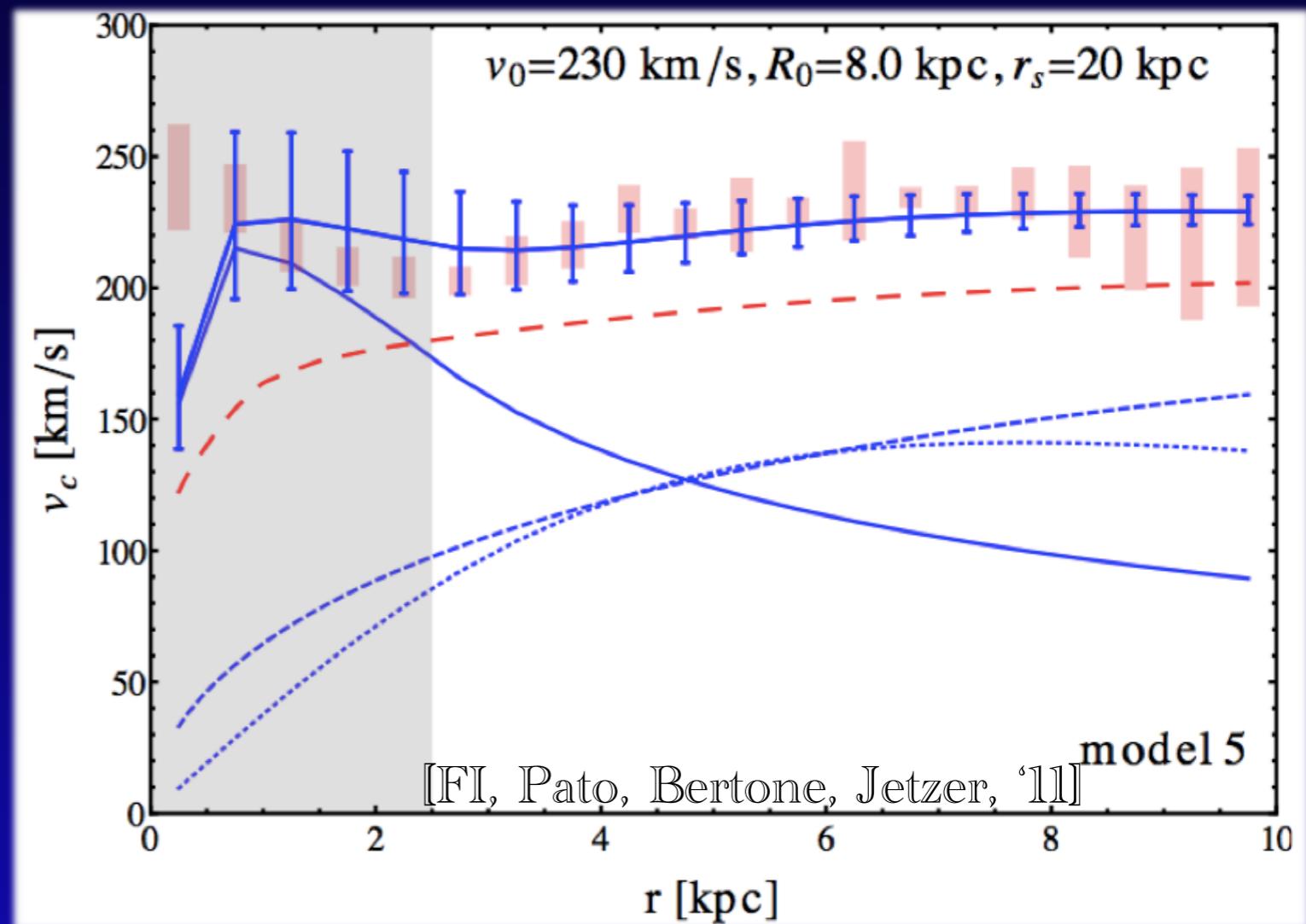
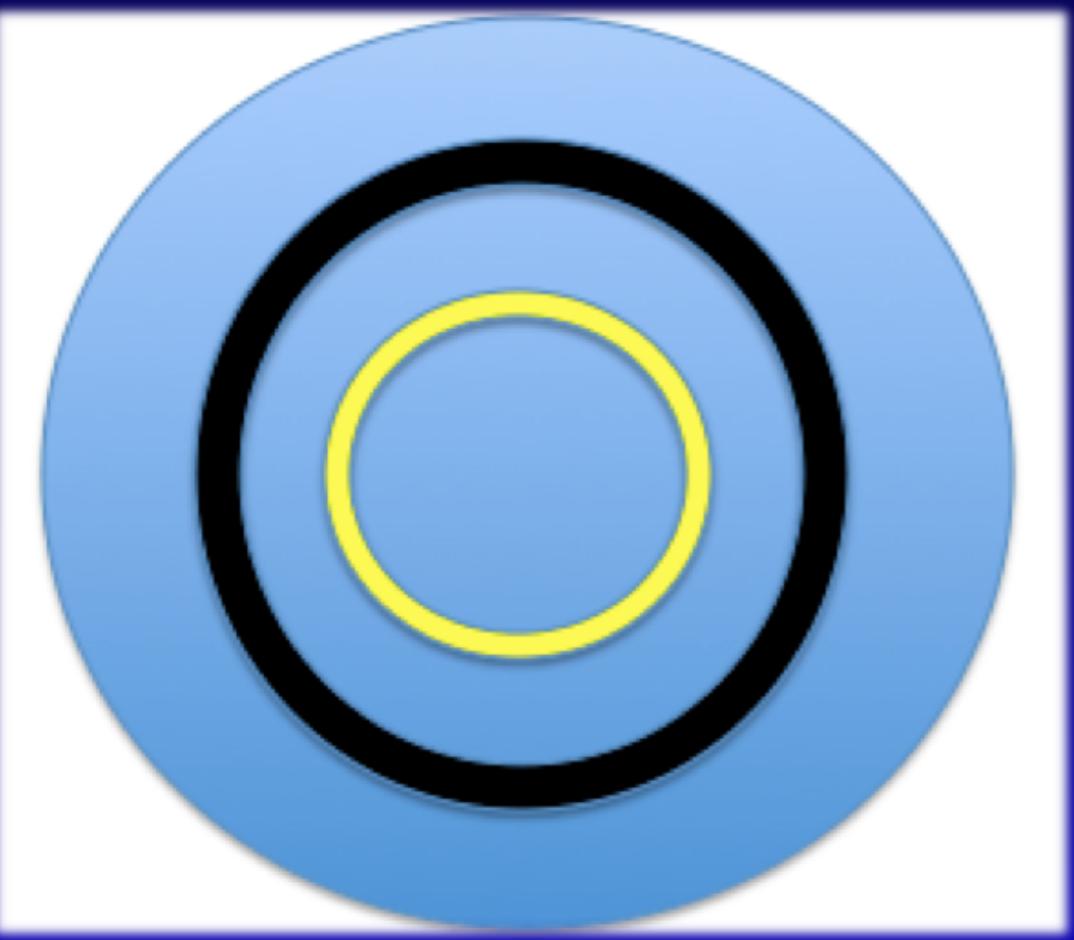
Local determination of ρ_0



Vertical motion of stars, determining the whole local potential

Global determination of $\rho(r)$

Fitting a DM profile to the Rotation Curve, on top of other components



$$\phi_{\text{tot}} = \phi_{\text{bulge}} + \phi_{\text{disk}} + \phi_{\text{gas}} + \phi_{\text{dm}}$$

Underlying assumption on DM presence and distribution shape

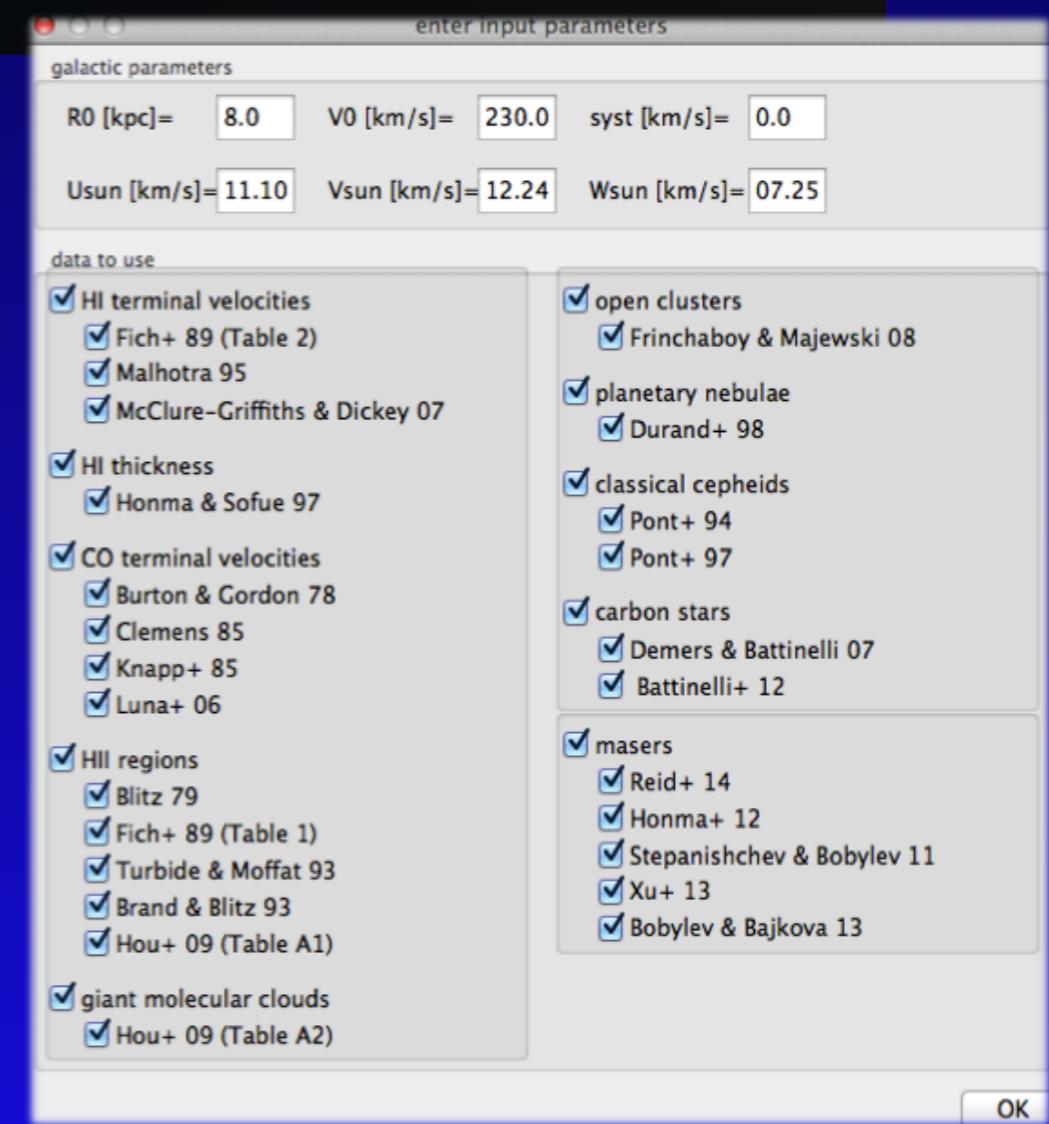
The Milky Way: observed rotation curve IV. public tool: galkin

```
#####
# galkin, version 1.0, by Miguel Pato and Fabio Iocco.
# Last update: MP 02 Jul 2015.
#####
# A tool to handle the available data on the rotation curve of the Milky Way.
#####
```

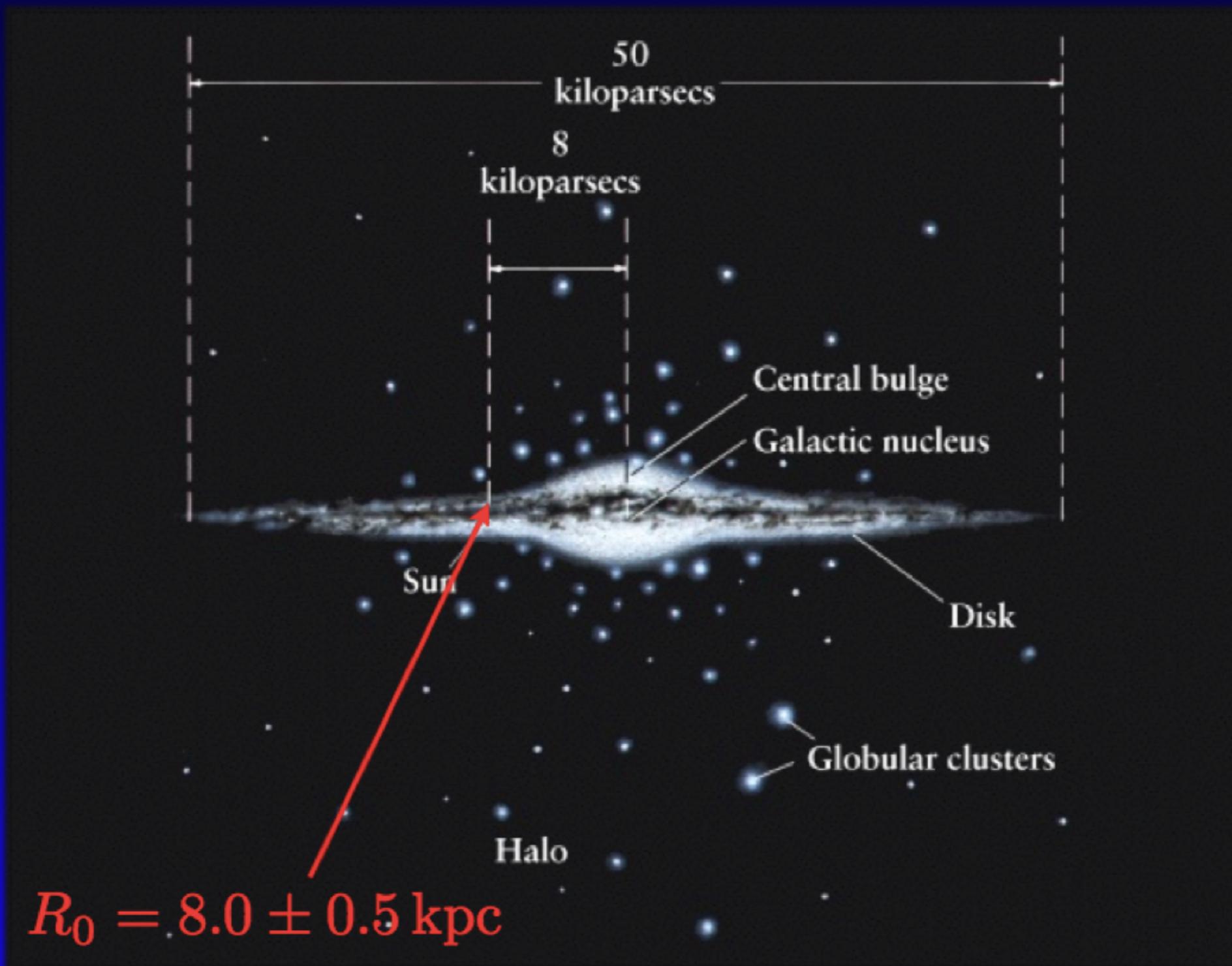
Customizable galactic parameters
(R_0, V_0)
peculiar motions, etc...

Finally available:
download your copy now

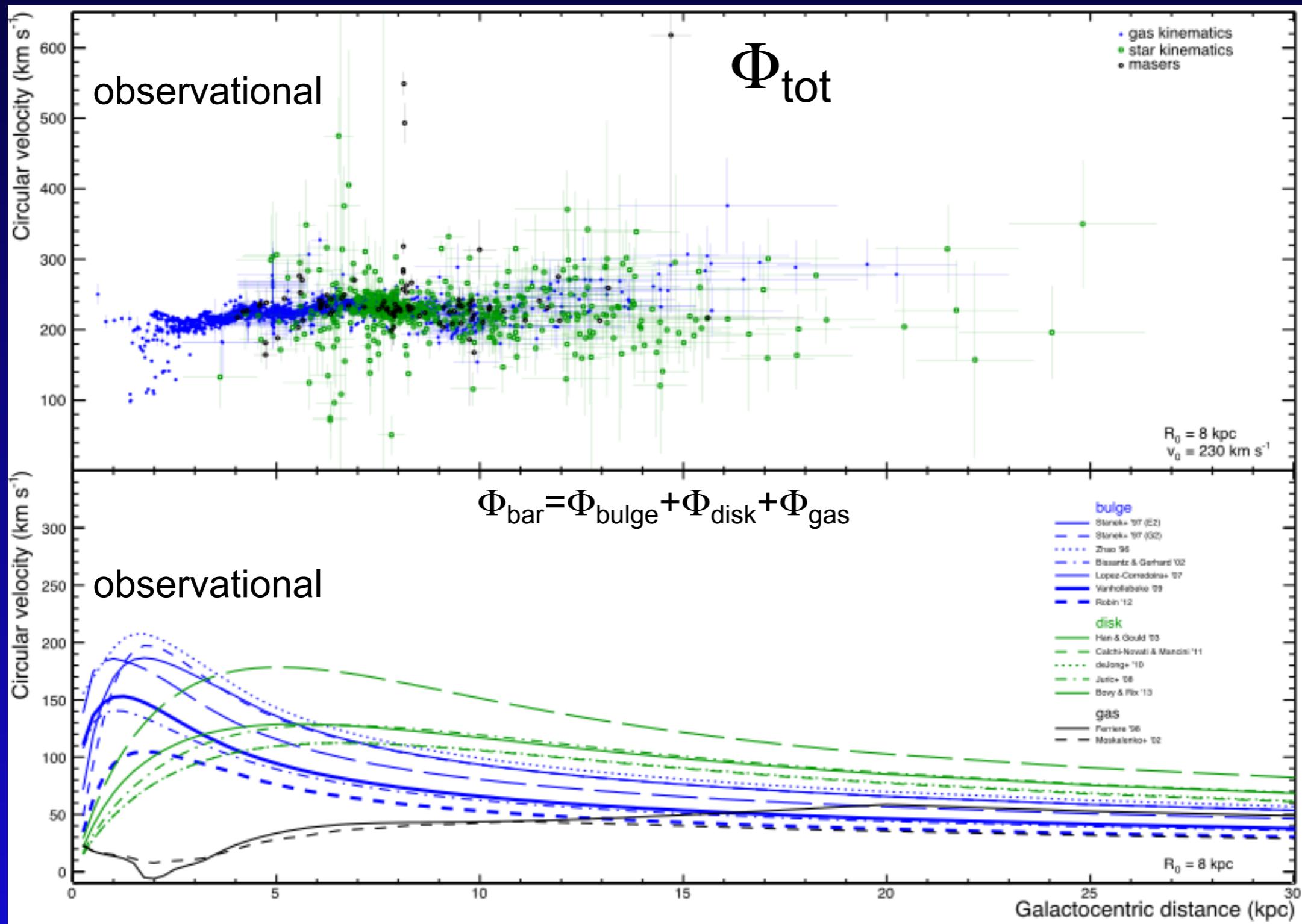
github.com/galkintool/galkin



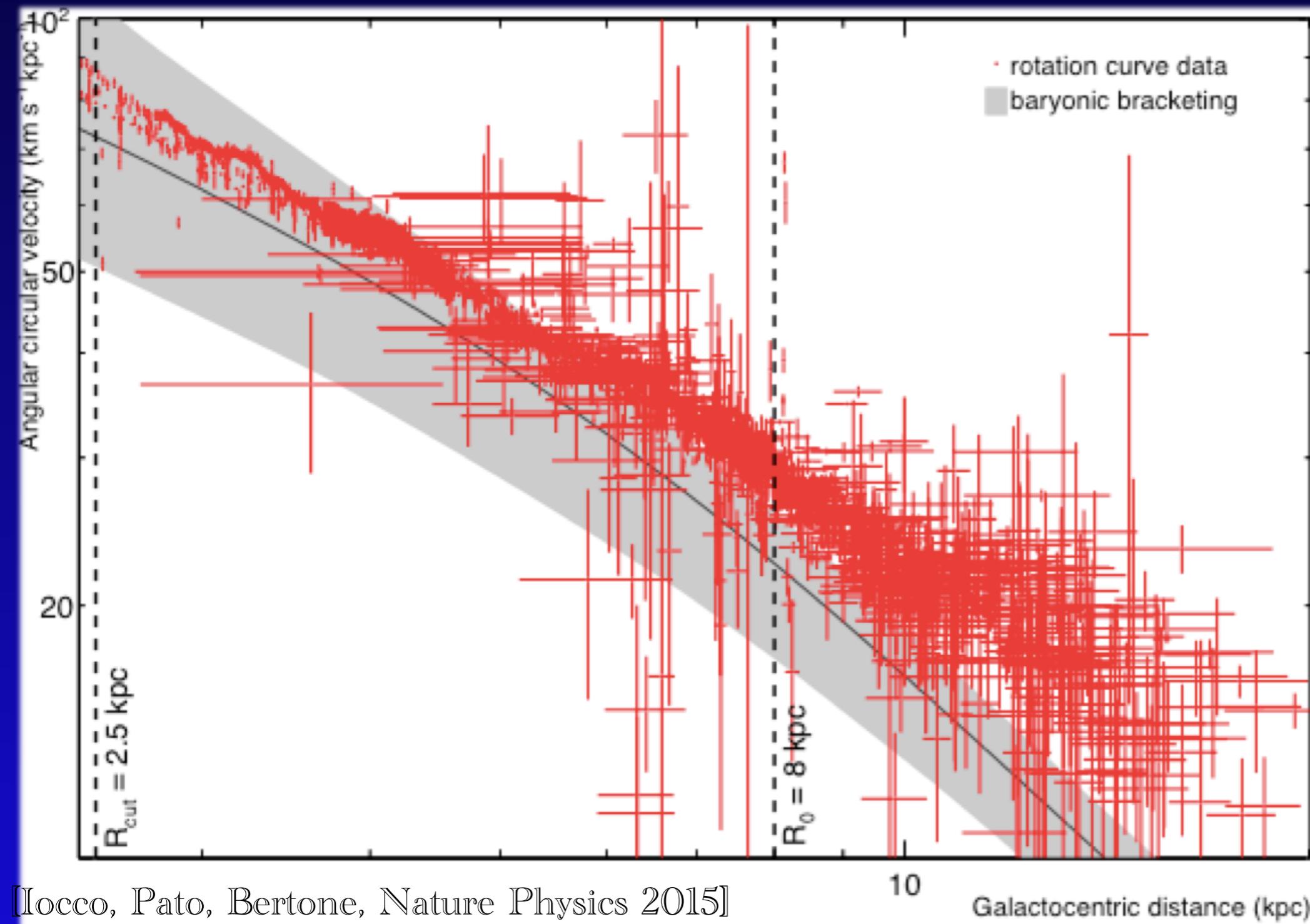
Modeling the Milky Way: morphological observations



The Milky Way: testing expectations



The Milky Way: testing expectations (with no additional assumption) ((and some technical detail))



The Milky Way:
testing expectactions
(with no additional assumptions)
((and some technical detail))

- Computing the “badness-of-fit” (discrepancy) of each baryon rot. curve (no DM!!) to observed one
- One COULD bin (and we have done it) but loss of information: using 2D chi-square (uncertainties on R, as well)

$$\chi^2 = \sum_{i=1}^N d_i^2 \equiv \sum_{i=1}^N \left[\frac{(y_i - y_{b,i})^2}{\sigma_{y,i}^2} + \frac{(x_i - x_{b,i})^2}{\sigma_{x,i}^2} \right]$$

The case of the Milky Way: the question

$$\Phi_{\text{tot}} = \Phi_{\text{bulge}} + \Phi_{\text{disk}} + \Phi_{\text{gas}} \quad ??$$

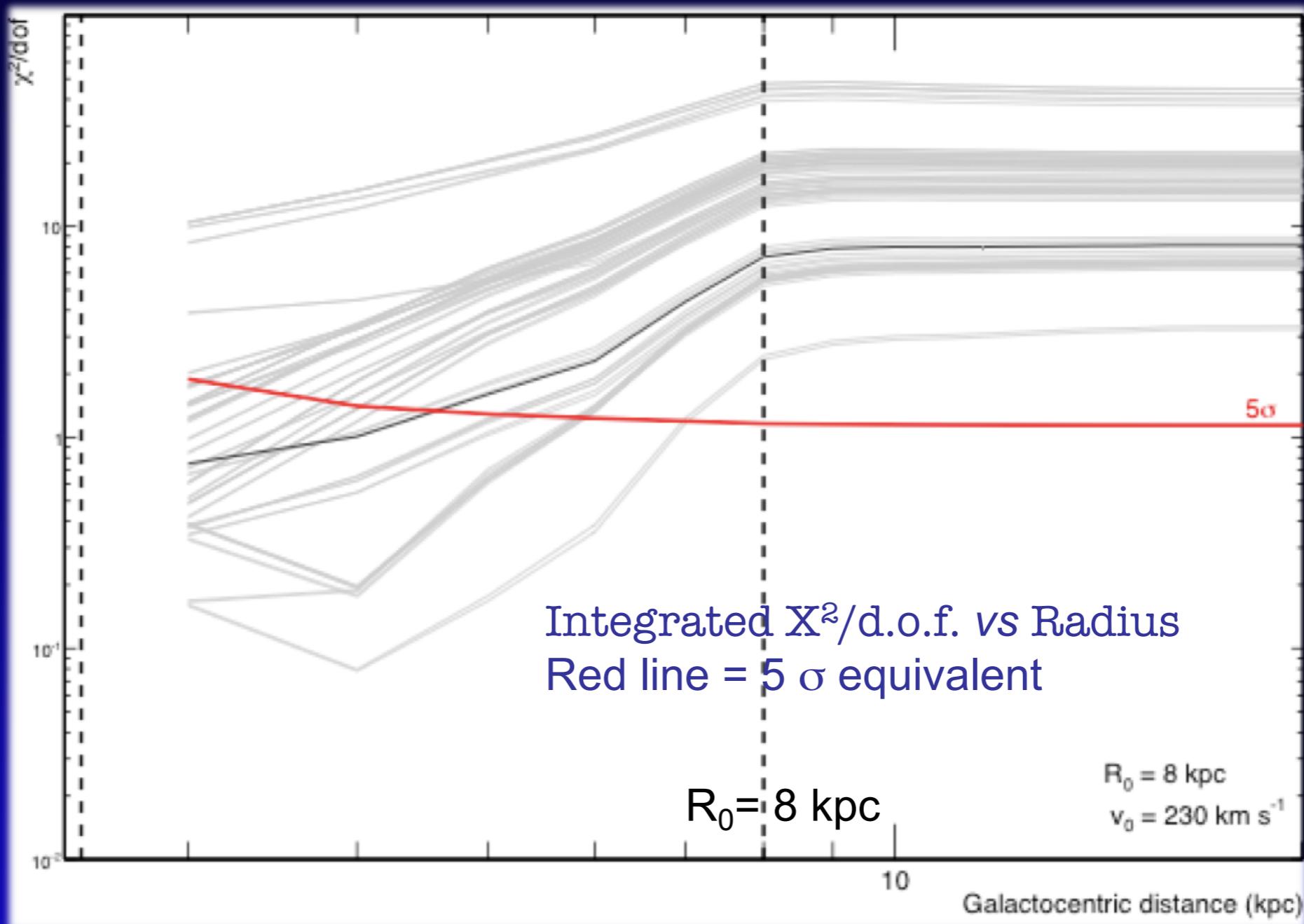
[can the observed, luminous components make up to the whole gravitational potential?]

$$v_c^2 = r \frac{d\phi_{\text{tot}}}{dr}$$

Rotation curve as a tracer of the total potential

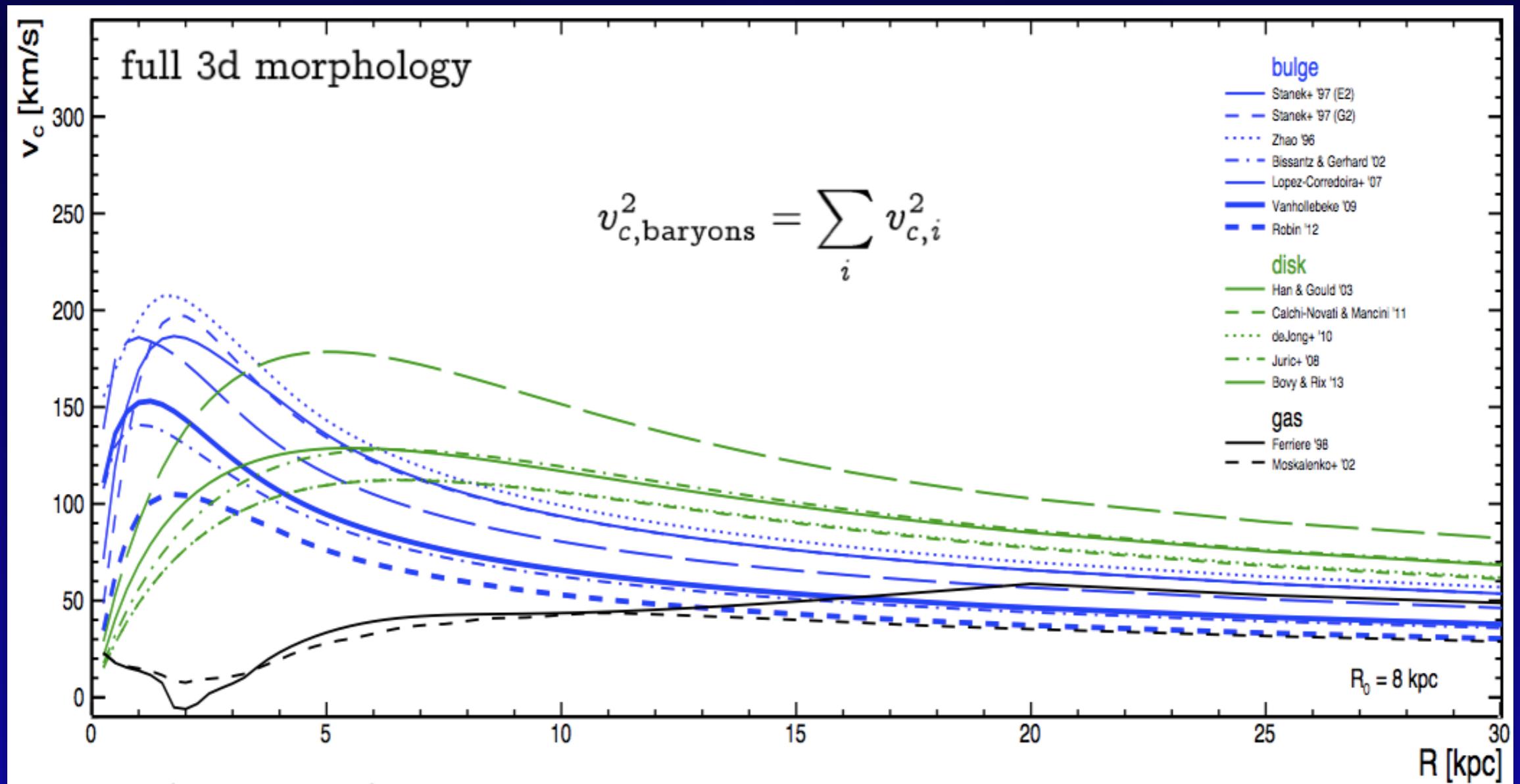
...and if not...

Do the baryon-only curves fit with the observed RC?



Answer is NO:
Every single model above 5σ , already at $R < R_0$!!

There's more than you are usually told:
 visible morphology is uncertain
 (and don't forget the dependence on Gal Parameters)



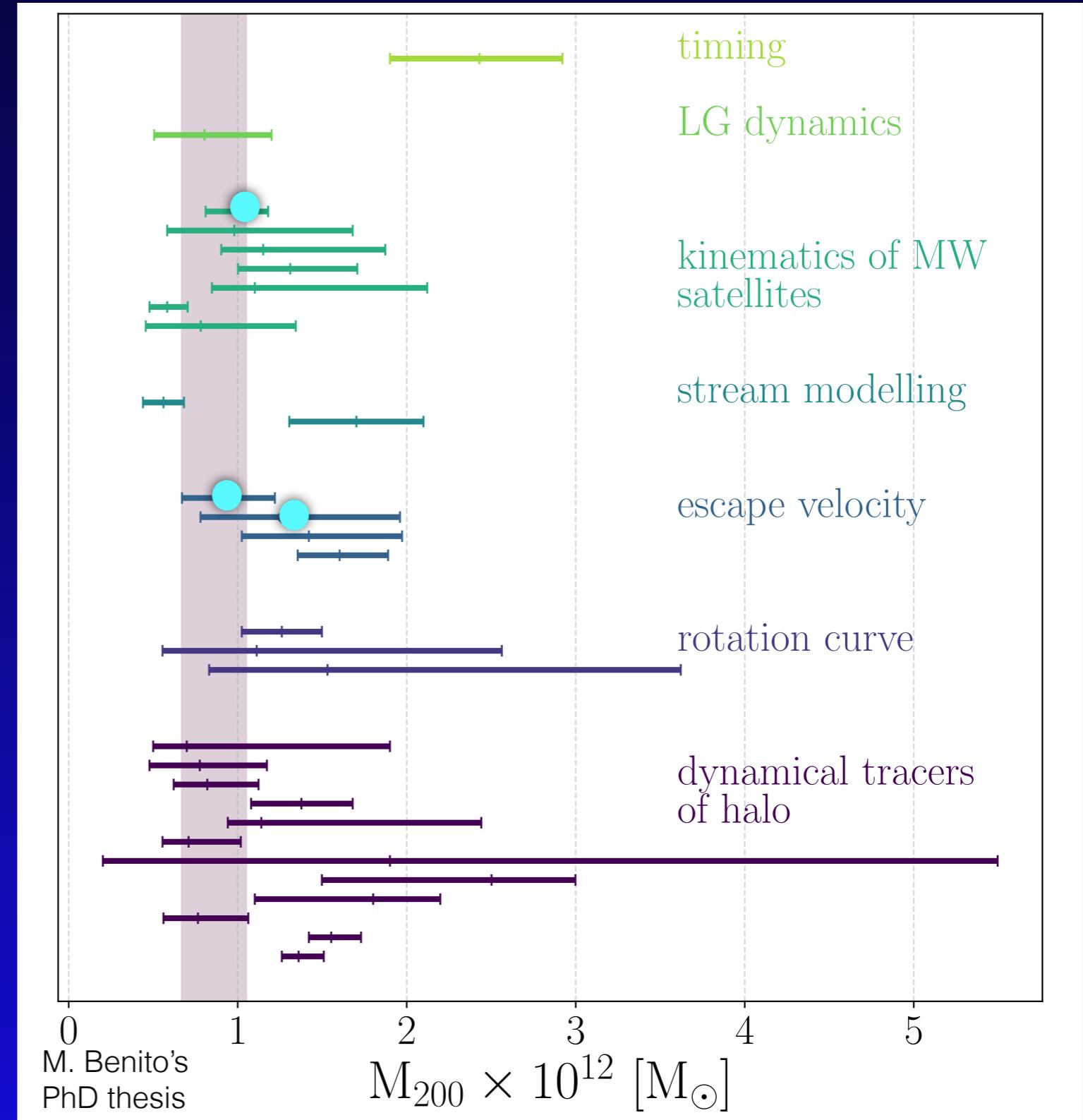
Also possible to determine the total mass of the MW

$$M_{200} = [8.0^{+1.1}_{-0.8} \text{ (stat)}^{+1.5}_{-0.7} \text{ (sys)}] \times 10^{11} M_\odot$$
$$M_{\text{bar}} = [0.65 \pm 0.04 \text{ (stat)}^{+0.04}_{-0.07} \text{ (sys)}] \times 10^{11} M_\odot$$
$$M_{\text{tot}} = [8.7^{+1.0}_{-0.8} \text{ (stat)}^{+1.4}_{-0.8} \text{ (sys)}] \times 10^{11} M_\odot$$

**Band (our result)
takes into account:**

- ▶ Different baryonic morphologies (syst)
- ▶ Statistical uncertainties

● Determinations with Gaia data



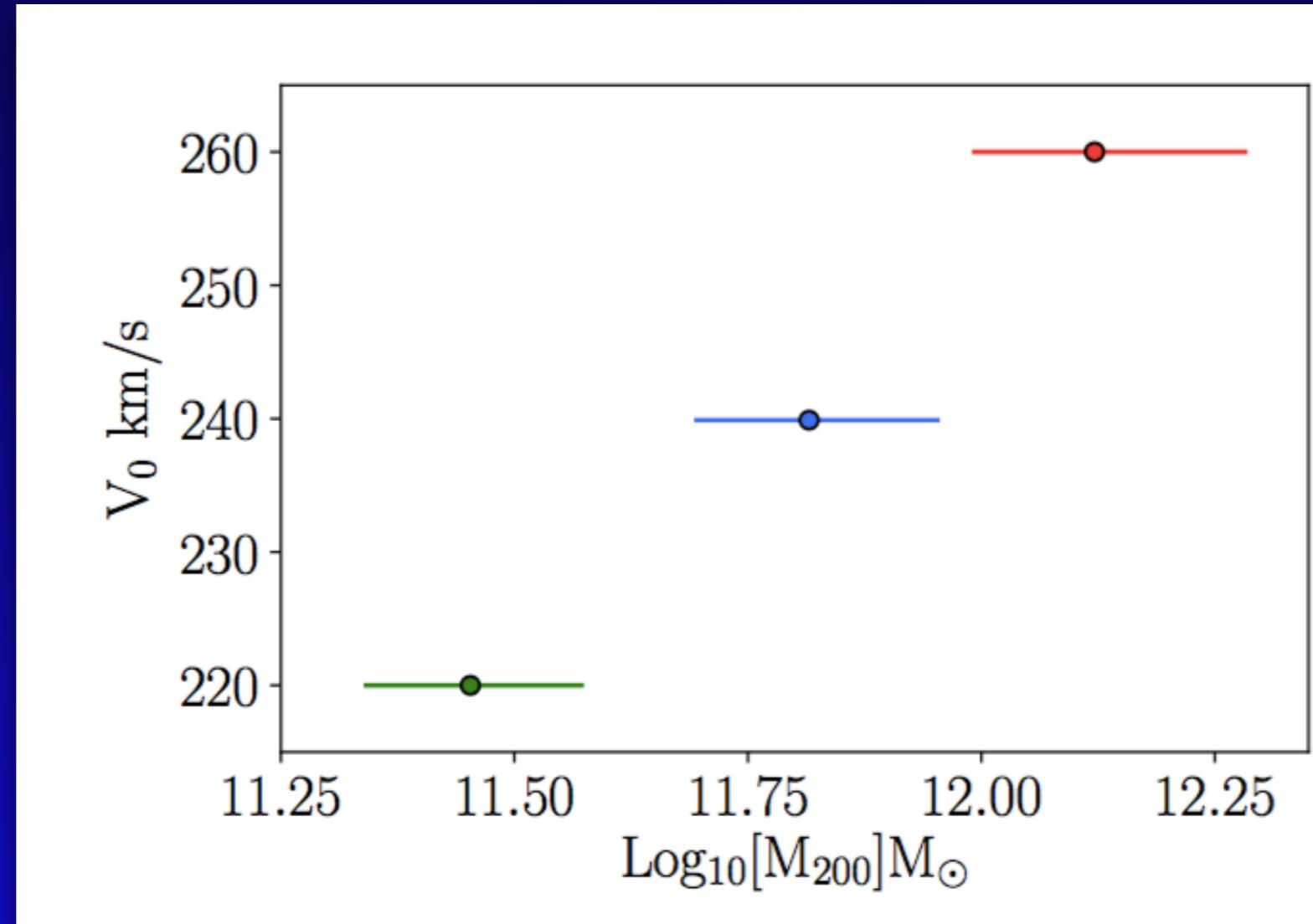
**Also possible to determine
the total mass of the MW**

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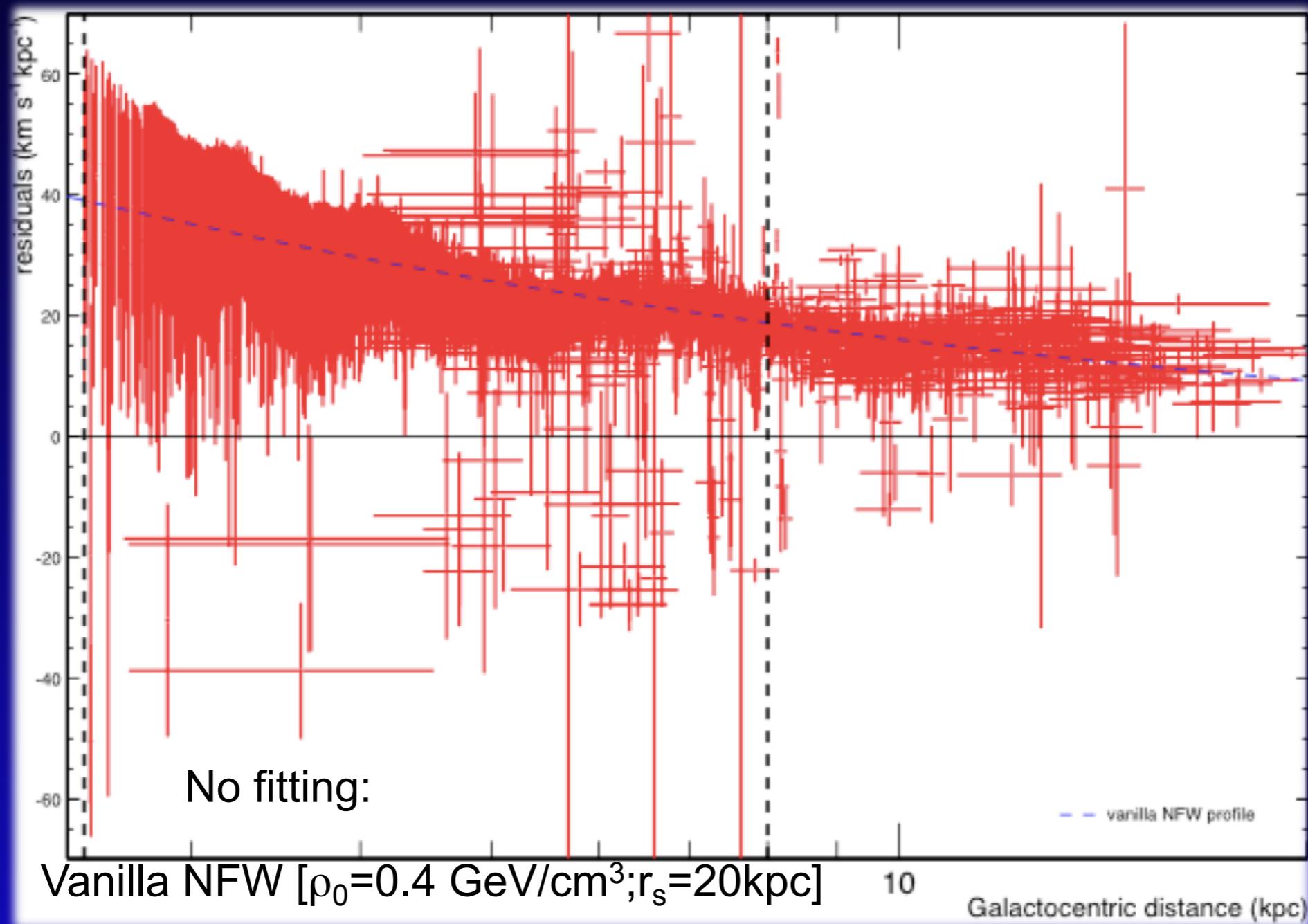
Determination of mass integrates out
►uncertainties on gamma

Still (mild) dependence on
Galactic Parameter(s)

V_0



Motivating dark haloes



$$v_{\text{Residual}} = (v_{\text{tot}}^2 - v_{\text{bar}}^2)^{1/2}$$

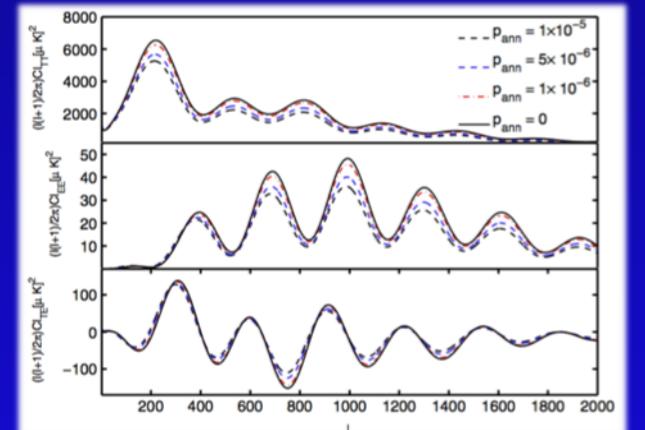
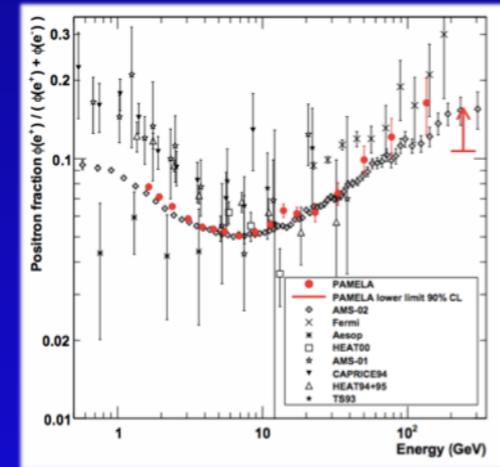
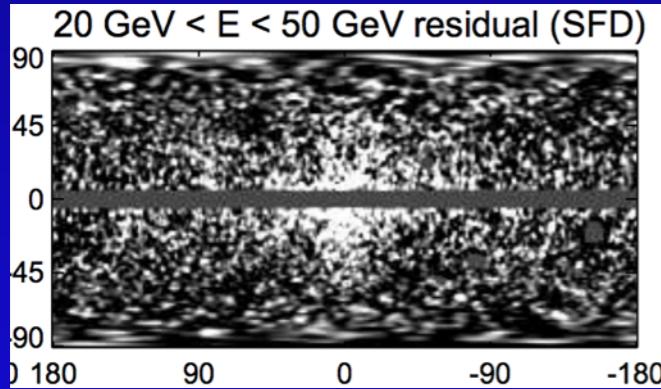
Indirect Detection: principles and dependencies

Galactic center, Dwarf Galaxies, Galactic Halo...
dependence on density structure
discovery (or constraints) subject to same uncertainty

$$F_i \propto \frac{1}{4\pi d^2} B_i \frac{\langle \sigma v \rangle}{m_\chi} \int \rho^2(r) dV$$

$$J_{annih} \propto \int_{los} \rho^2(r) dV$$

$$\Phi_{DM}(E) = \Phi_{PP}(E) \mathcal{J}$$

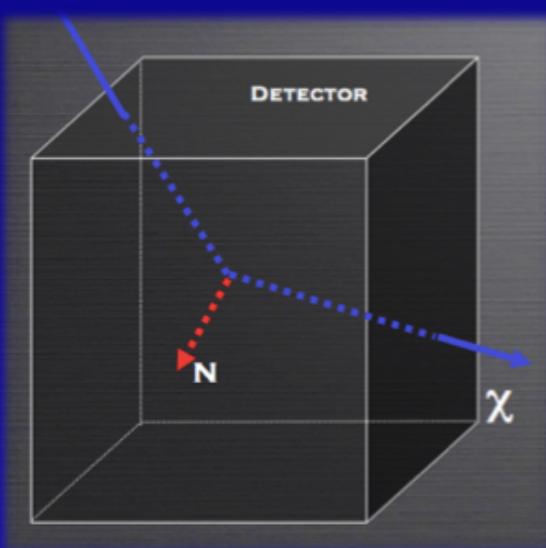


Direct Detection: principles and dependencies

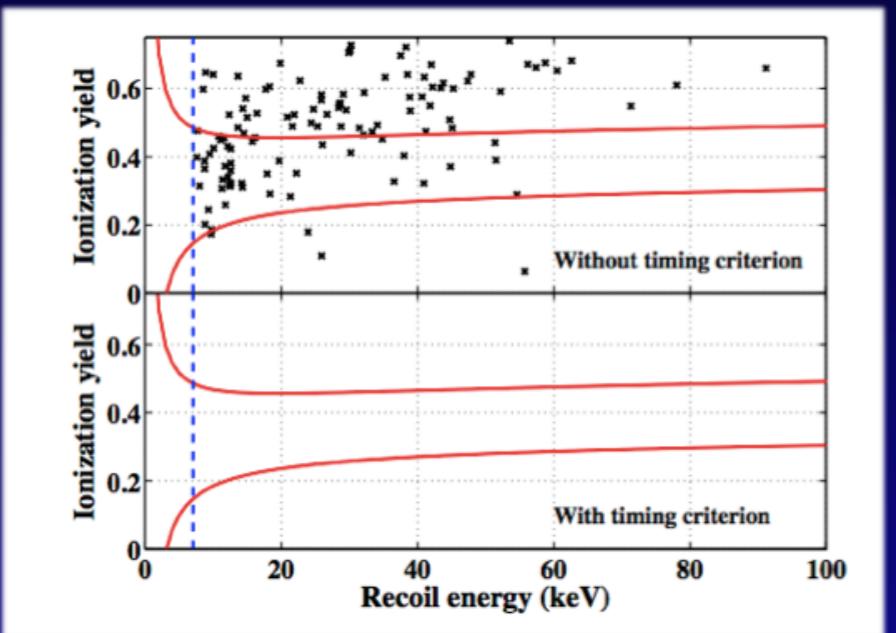
A big mountain
(or a deep mine)



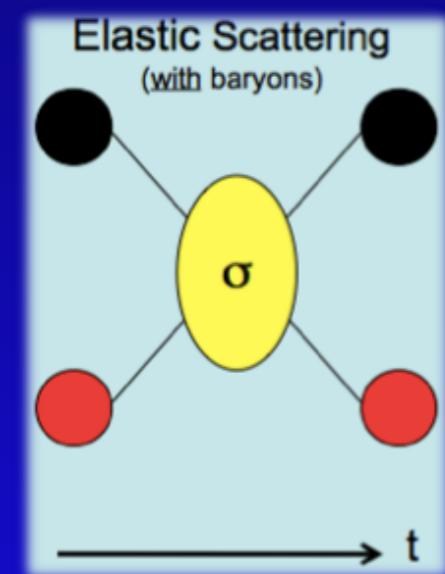
a relatively cheap detector



Your observed data



Your ticket to Stockholm



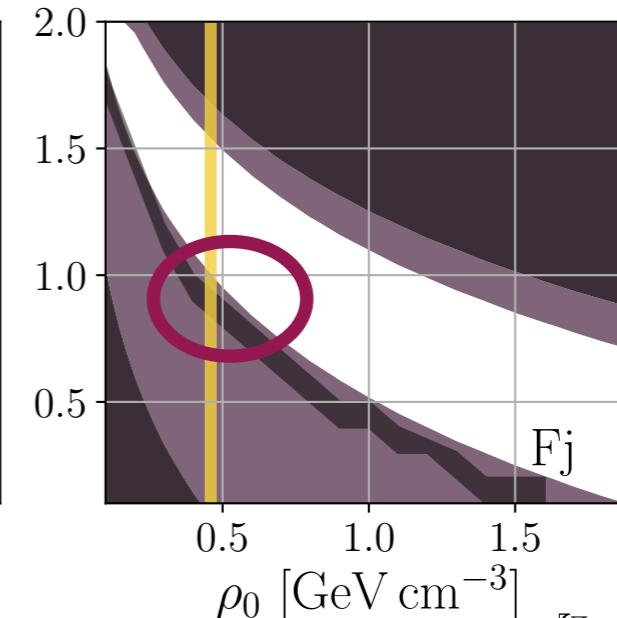
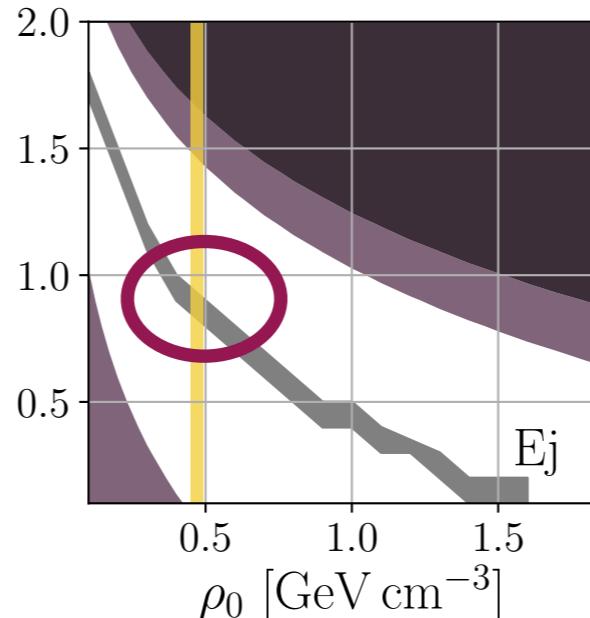
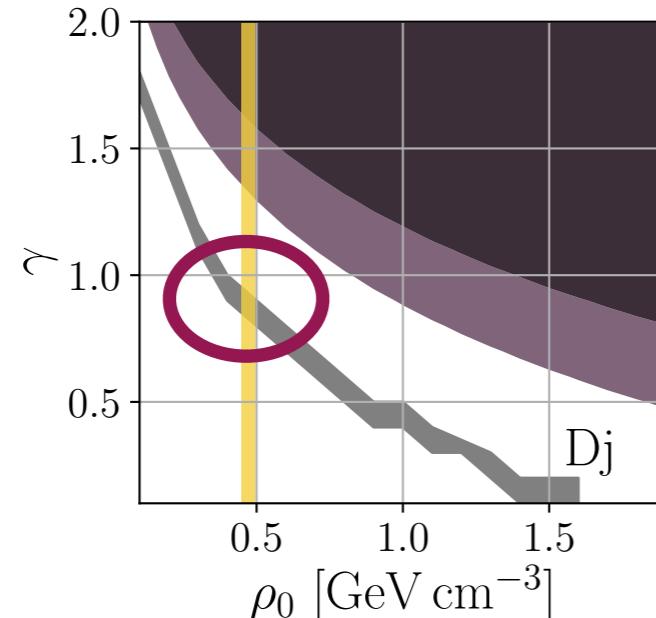
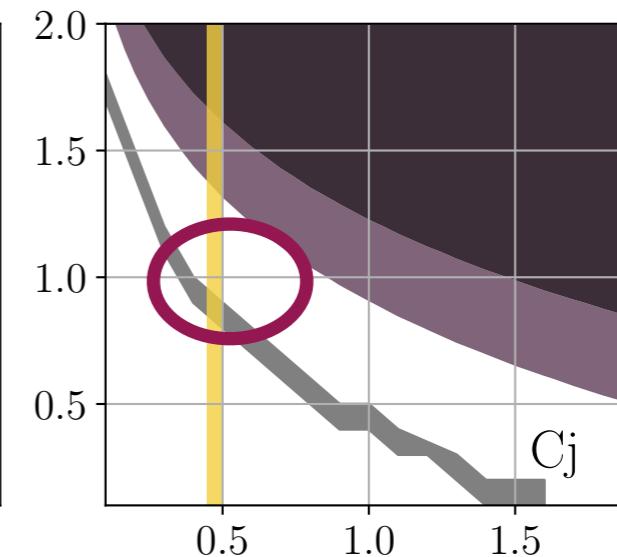
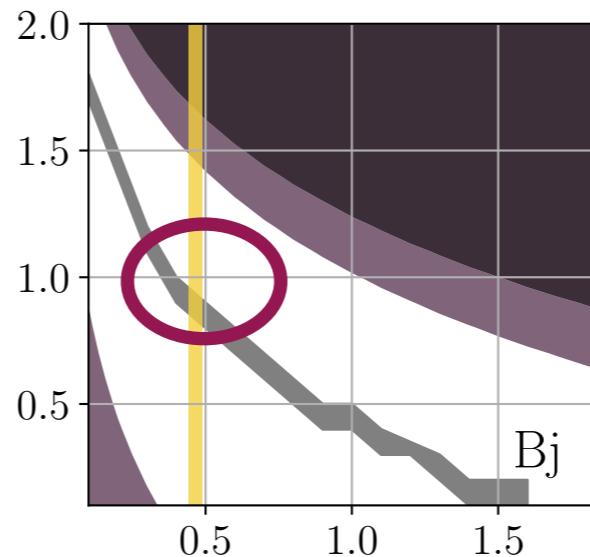
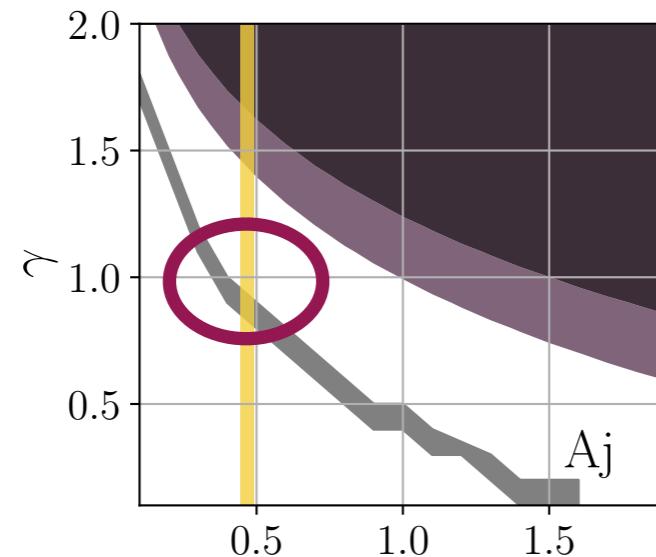
Galactic Bulge Region - Results: varying bulge morphology

“the dark matter density of our model has a [...] shallow cusp or a core in the bulge region”

$$M_{\text{DM}} = (0.32 \pm 0.05) \times 10^{10} M_{\odot}$$

Portail +
MNRAS 465 (2017)

Legend:
White: Allowed at 1σ
Dark purple: Allowed at 2σ
Black: Excluded at 2σ
Yellow: preferred ρ_0 (RC)



Core is not a necessary condition!

[Iocco & Benito, 2017]
arXiv:1611.09861
(+ M. Benito's thesis)