

Cogenesis of Dark Matter and Baryon Asymmetries in Scotogenic Model

(work in progress)

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- Motivation

- Scotogenic Model

- E. Ma , Phys. Rev. D **73** (2006) 077301

- Neutrino masses
 - Dark Matter

- Asymmetric Dark Matter (ADM) Model

- D. E. Kaplan, M. A. Luty, K. M. Zurek, Phys. Rev. D **79** (2009) 115016

- $\Omega_{\text{DM}} \cong 5\Omega_B$

Combine ADM scenario with Scotgenic Model
and explain Neutrino masses , Dark Matter ,
Baryon Asymmetry simultaneously

• Model

Standard Model

- + $N_i (i = 1, 2, 3)$ (singlet fermion)
- + η (doublet complex scalar)

Scotogenic Model

- + σ (singlet real scalar)

DM

field	fermion			scalar		
	L	e_R	N	H	η	σ
$SU(2)_L$	2	1	1	2	2	1
Z_2	+	+	-	+	-	-

Table 1 : Z_2 symmetry assignment

$$\mathcal{L} \supset -h_{\alpha i} \bar{L}_\alpha \tilde{\eta} N_i + \frac{1}{2} M_i \bar{N}_i N_i^c + h.c.$$

$$\begin{aligned}
 V(H, \eta, \sigma) = & m_H^2 |H|^2 + m_\eta^2 |\eta|^2 + m_\sigma^2 \sigma^2 + \frac{1}{2} \lambda_1 |H|^4 + \frac{1}{2} \lambda_2 |\eta|^4 + \frac{1}{2} \lambda_3 \sigma^4 + \lambda_4 |H|^2 |\eta|^2 \\
 & + \lambda_5 |H^\dagger \eta|^2 + \lambda_6 |H|^2 \sigma^2 + \lambda_7 |\eta|^2 \sigma^2 + \frac{1}{2} [\lambda_8 (H^\dagger \eta)^2 + h.c.] \\
 & + \frac{1}{\sqrt{2}} [\mu \sigma (H^\dagger \eta) + h.c.]
 \end{aligned}$$

Focus on this

• Model

Neutrino mass

$$\eta = (\eta^+, (\eta_R + i\eta_I)/\sqrt{2})^T$$

$$(\mathcal{M}_\nu)_{\alpha\beta} = \sum_i \frac{h_{\alpha i}^* h_{\beta i}^*}{32\pi^2} M_i \left[\frac{m_{\eta_R}^2}{m_{\eta_R}^2 - M_i^2} \ln \frac{m_{\eta_R}^2}{M_i^2} - \frac{m_{\eta_I}^2}{m_{\eta_I}^2 - M_i^2} \ln \frac{m_{\eta_I}^2}{M_i^2} \right]$$

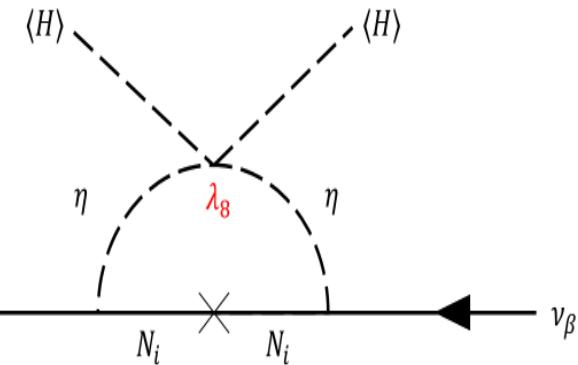
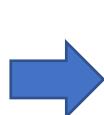


Fig.1 : One-loop diagram



$$\mathcal{M}_\nu = h^* \mathcal{D}_\Lambda^{-1} h^\dagger$$

$$(\mathcal{D}_\Lambda)_{ii} = \frac{2\pi^2}{\lambda_8} \xi_i \frac{2M_i}{v^2} \equiv \Lambda_i$$

$$U^T \mathcal{M}_\nu U = \text{diag}(m_1, m_2, m_3) \equiv D_\nu$$

U : Maki-Nakagawa-Sakata(MNS)matrix

Casas-Ibarra parametrization

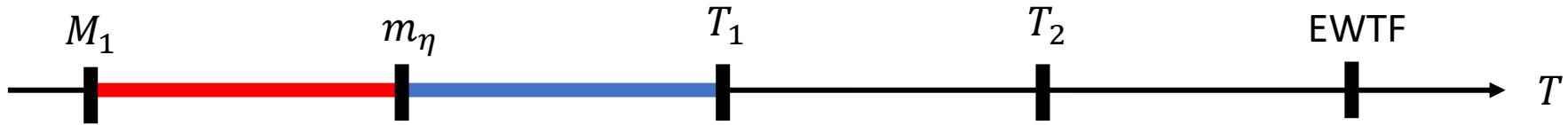
$$h_{\alpha i} = \left(U D_\nu^{\frac{1}{2}} R^\dagger D_\Lambda^{\frac{1}{2}} \right)_{\alpha i}$$

R : complex orthogonal matrix

Yukawa matrix depends on λ_8, M_i

• Cogenesis

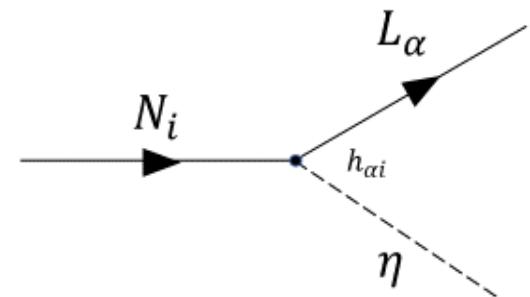
- Story of the generation of dark matter



- $M_1 > T > m_\eta$

The lightest heavy neutrino N_1 decays into L_α and η

$$n_{L-\bar{L}} \cong n_{\eta-\bar{\eta}}$$



- $m_\eta > T > T_1$

The inert higgs η annihilates into SM particle

$$n_\eta \cong n_{\eta-\bar{\eta}} \gg n_{\bar{\eta}}$$

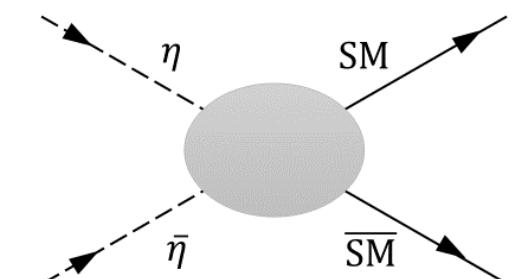
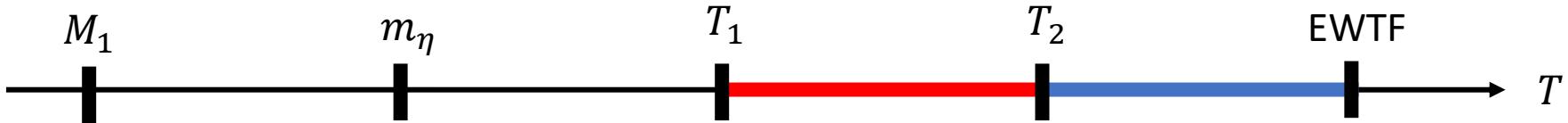


Fig.3 : The annihilation of η

• Cogenesis

- Story of the generation of dark matter



- $T_1 > T > T_2$

The inert higgs η decays into Dark Matter σ

$$n_{\eta-\bar{\eta}} \rightarrow n_{\text{DM}}$$

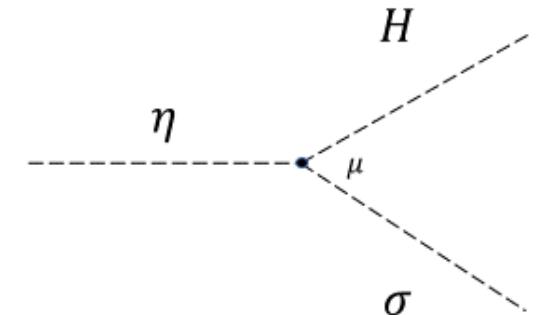


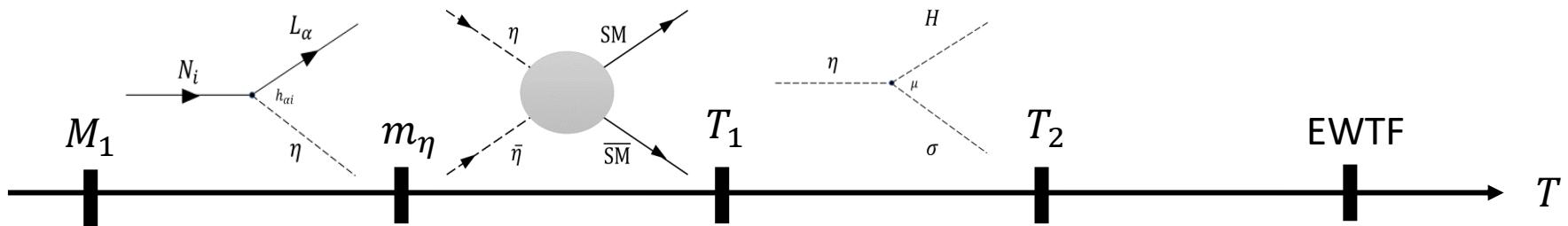
Fig.4 : The decay of η

- $T_2 > T > 10^2 \text{GeV}$

The decay of inert higgs η completes at this era

$$n_{\eta-\bar{\eta}} \approx 0 \text{ and } n_{L-\bar{L}} \approx n_{\text{DM}}$$

• Cogenesis



$\eta\bar{\eta} \rightarrow HH$ should be out of equilibrium from M_1 to T_2

If it occurs



$$n_{L-\bar{L}} \neq n_{\eta-\bar{\eta}}$$

Interactions	m_η	T_1	T_2	EWTF
$\bar{\eta} \eta \rightarrow \overline{SM} SM$	○	✗	✗	
$\eta \rightarrow \sigma H$	✗	○	○	
$\bar{\eta} \rightarrow \sigma \bar{H}$	✗	○	○	
$\eta\bar{\eta} \rightarrow HH$	✗	✗		○
$\bar{\eta}\eta \rightarrow \bar{H}H$				

• Cogenesis

The Yukawa matrix and the interaction of $\eta\eta \rightarrow HH$ depend on λ_8

$$h_{\alpha i} = \left(U D_{\nu}^{\frac{1}{2}} R^{\dagger} D_{\Lambda}^{\frac{1}{2}} \right)_{\alpha i}$$

$$\mathcal{M}_{\nu} = h^* \mathcal{D}_{\Lambda}^{-1} h^{\dagger}$$

$$(\mathcal{D}_{\Lambda})_{ii} = \frac{2\pi^2}{\lambda_8} \xi_i \frac{2M_i}{v^2} \equiv \Lambda_i$$

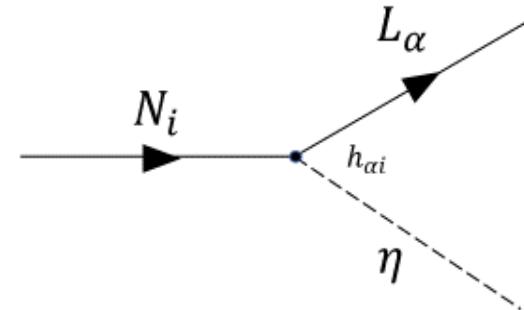


Fig.2 : The decay of N_i

- Condition for λ_8

$$\Gamma_{\eta\eta \rightarrow HH} < H \text{ (Hubble parameter)}$$

$$\therefore \lambda_8 < 3.4 \times 10^{-8} \sqrt{m_{\eta}/[\text{GeV}]}$$

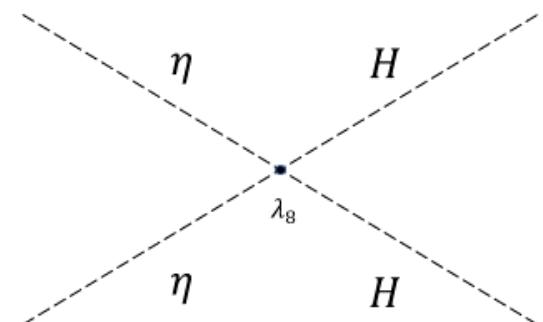
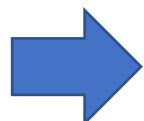


Fig.5 : $\eta\eta \rightarrow HH$



Calculate Lepton asymmetry under this condition

• Calculation

- Calculate baryon to photon ratio η_B in a standard Leptogenesis

$$\eta_B \approx -0.01\epsilon_1\kappa_1$$

ϵ_1 : asymmetry parameter

κ_1 : efficiency factor

$$\epsilon_i = \frac{1}{8\pi} \frac{1}{(h^\dagger h)_{ii}} \sum_{j \neq i} \text{Im} \left[\left\{ (h^\dagger h)_{ij} \right\}^2 \right] \frac{1}{\sqrt{r_{ji}}} F(r_{ji}, \eta_i) \quad \eta_i = m_\eta^2/M_i^2$$

$$F(r_{ji}, \eta_i) = \sqrt{r_{ji}} \left[f(r_{ji}, \eta_i) - \frac{\sqrt{r_{ji}}}{r_{ji} - 1} (1 - \eta_i)^2 \right] \quad r_{ji} = M_j^2/M_i^2$$

$$f(r_{ji}, \eta_i) = \sqrt{r_{ji}} \left[1 + \frac{(1 - 2\eta_i + r_{ji})}{(1 - \eta_i)^2} \ln \left(\frac{r_{ji} - \eta_i^2}{1 - 2\eta_i + r_{ji}} \right) \right]$$

$$\kappa_1(K_1) \simeq \frac{1}{1.2K_1 [\ln K_1]^{0.8}}$$



This approximation holds in the range: $10 < K_1 < 50$

$$\begin{aligned} K_1 &= \frac{1}{8\pi} \sqrt{\frac{90}{8\pi^3 g_*}} \frac{M_{\text{Pl}}}{M_1} (h^\dagger h)_{11} (1 - \eta_1)^2 \quad K_1 : \text{decay parameter} \\ &= \frac{2\pi^2}{\lambda_5} \xi_1 \sqrt{\frac{45}{64\pi^5 g_*}} \frac{M_{\text{Pl}}}{v^2} (R D_{\mathcal{M}_\nu} R^\dagger)_{11} (1 - \eta_1)^2 \end{aligned}$$

• Result

Calculation of baryon-to-photon ratio

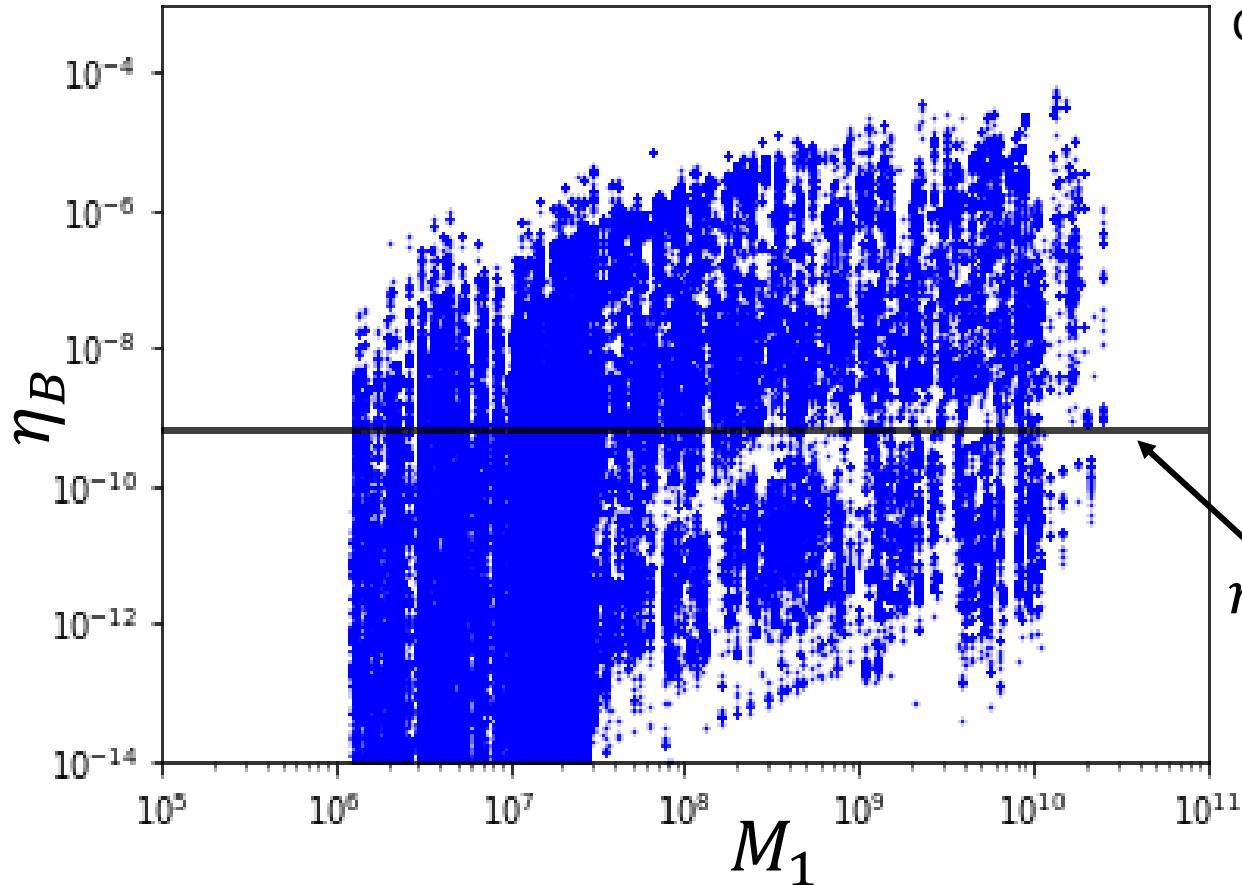


Fig.6 : Result of calculation

Conditions

- All components of the Yukawa matrix are less than 1
- $10 < K_1 < 50$
- $\lambda_8 = 3.4 \times 10^{-8} \sqrt{m_\eta / [\text{GeV}]}$
- $M_i = 1.5M_{i+1}$
- $M_1 = m_\eta \times 10^2$

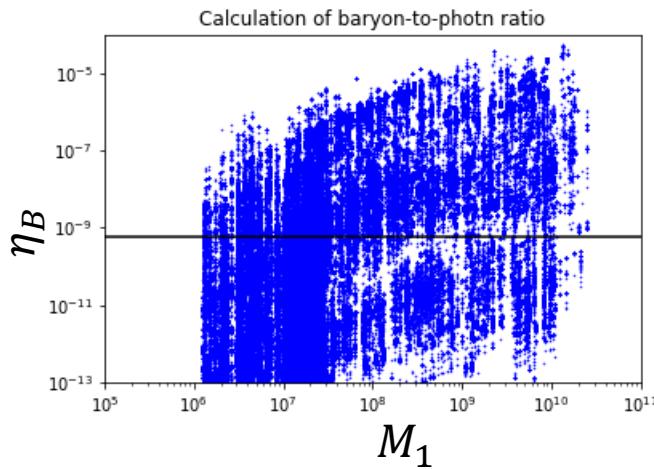
$$\eta_B = 6.1 \times 10^{-10}$$

- Summary
 - Combine ADM scenario to Scotgenic Model
-
- λ_8 is involved in the the Yukawa matrix and the interaction of $\eta\eta \rightarrow HH$.
 - There are parameters that satisfy under these conditions.
 - As a future prospect, we will verify whether there are parameters that satisfy other conditions

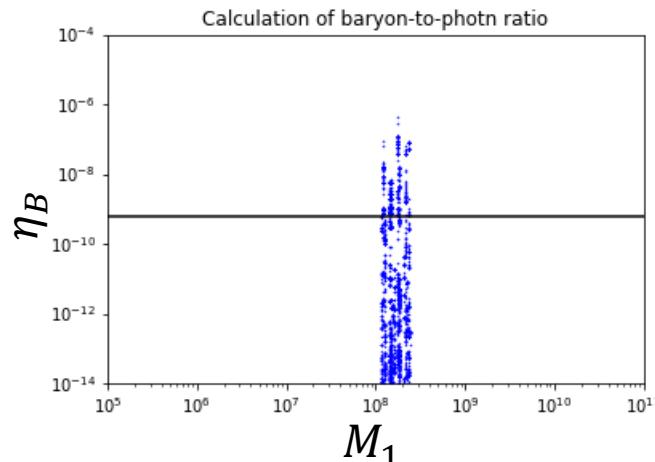
Thank you for your attention.

Appendix

- $\lambda_8 = 3.4 \times 10^{-8} \sqrt{m_\eta/\text{[GeV]}}$
- $M_1 = m_\eta \times 10^2$

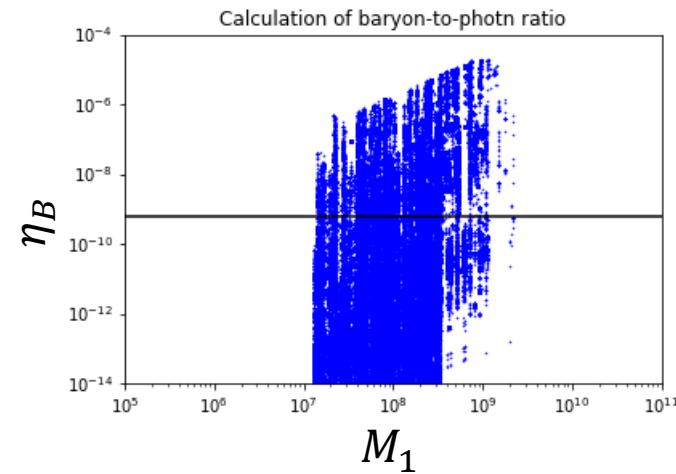


- $\lambda_8 = 3.4 \times 10^{-9} \sqrt{m_\eta/\text{[GeV]}}$
- $M_1 = m_\eta \times 10^2$

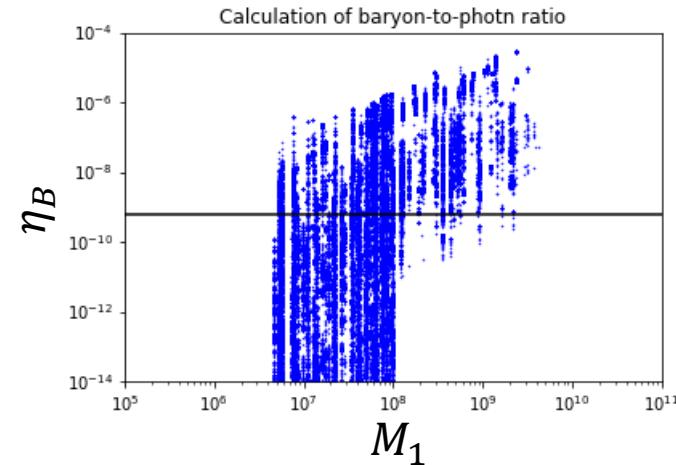


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- $\lambda_8 = 1.0 \times 10^{-8} \sqrt{m_\eta/\text{[GeV]}}$
- $M_1 = m_\eta \times 10^2$



- $\lambda_8 = 3.4 \times 10^{-8} \sqrt{m_\eta/\text{[GeV]}}$
- $M_1 = m_\eta \times 10^3$



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