

# Constraining systematics at T2K and SuperKamiokande oscillation analyses using $\nu$ -nucleus interaction models

ICRR Inter-University Research Project Ref. J1  
(Research Center for Cosmic Neutrinos)

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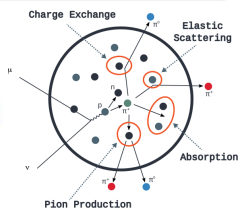
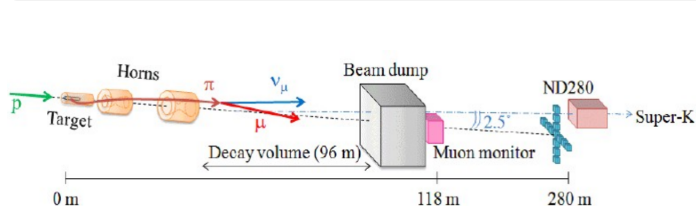
ICRR Inter-University Research Program Meeting, 21 February 2024

- **Ongoing project (2021 - )**
- **Budget approved: 90,000 yen. Purpose: travel and accommodation costs at ICRR.** They have not been requested in FY2023  $\Rightarrow$  Budget used to purchase equipment and supplies for the ICRR Neutrino Center.
- **Publications (acknowledging ICRR project in FY2023): 5** (1 of which under review).
  - *New model comparison for semi-inclusive charged-current electron and muon neutrino scattering by Ar40 in the energy range of the MicroBooNE experiment.* J. M. Franco-Patino et al., Phys. Rev. D 109, 013004 (2024).
  - *Superscaling in the resonance region for neutrino-nucleus scattering: The SuSAv2 dynamical coupled-channels model.* J. Gonzalez-Rosa et al., Phys. Rev. D 108, 113008 (2023).
  - *Measurements of neutrino oscillation parameters from the T2K experiment using  $3.6 \times 10^{21}$  protons on target.* K. Abe et al. [T2K Collaboration], Eur. Phys. J. C 83, 782 (2023).
  - *Parametrized uncertainties in the SF model of neutrino charged-current quasielastic interactions for oscillation analyses.* J. Chakrani et al., arXiv:2308.01838 [hep-ex] (2023).
  - *Weak Neutrino (Antineutrino) Charged-Current Responses and Scaling for Nuclear Matter in the Relativistic Mean Field.* S. Cruz-Barrios et al., Universe 2023, 9, 240 (2023).
- **PhD thesis defended by members of this project in FY2023: 1**  
J.M. Franco-Patino, Univ. of Seville. Supervisors: J.A. Caballero and M.B. Barbaro

# $\nu$ -A interaction models are essential for $\nu$ oscillation analyses

## Long-baseline accelerator neutrino oscillation experiments

Neutrinos produced as secondary decay products of hadrons ( $\pi$ ,  $K$ ) generated in primary reactions of  $p$  with nuclei  $\Rightarrow$  broad energy beam.



## Experimental difficulties:

- The neutrino flux: broad energy distribution around a maximum  $\rightarrow$  True energy for a detected event is unknown.
- To reduce flux uncertainties, two identical detectors are employed. *Near Detector* placed near the neutrino production region and *Far Detector* where a maximum/minimum oscillation is expected. MC simulations are employed to reconstruct  $E_\nu$  for each detected event.
- The reliability of  $\nu$ -oscillation experiments depends on a precise determination of the  $\nu$ -nucleus cross section measurements and on the  $\nu$  flux at ND.

➤ Global experimental **systematics** in T2K are around a 4% (7%) for  $\nu_\mu$  ( $\nu_e$ ) reactions and are dominated by flux and cross section uncertainties (3%)  $\Rightarrow$  Need for development and **implementation** of sophisticated neutrino interaction models in **event generators**.

## Modelling of $\nu$ interactions in generators:

**NEUT models** (SF, LFG) used in T2K start from **PWIA**: the interacting nucleon does not feel any nuclear potential after the interaction. Not realistic at low and intermediate energy transfer. Corrections are being considered to account for effects **beyond PWIA**:

- 2p2h nucleon ejection.
  - Improving descriptions of the initial state, removal energy and PB description.
  - RPA (nucleon-nucleon correlations) and FSI (Final State Interactions).
- **RPA and FSI effects** can introduce important differences in the experimental analyses.
- These differences affect OA: E dependence of the CS,  $\nu$  vs.  $\bar{\nu}$ ,  $\nu_e/\nu_\mu$ , C/O.
- Largest uncertainty in semi-inclusive neutrino CS (lepton+hadron kinematics).

## Description of final state interactions: Relativistic Mean Field and Optical potentials

- **FSI** can be treated as a distortion of the outgoing nucleon wave functions by a nuclear potential  $\Rightarrow$  **DWIA**: distorted wave impulse approximation.
- **RMF+FSI and ROP models** yield good agreement with  $e-A$  and  $\nu-A$  inclusive CS from low to high kinematics. **RMF potentials** fitted to saturation properties of nuclear matter, radii and nuclear masses. **Optical potentials (OP)** phenomen. fits adjusted to  $e-A$  data.

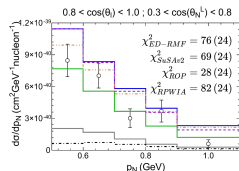
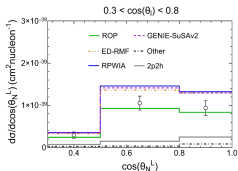
- **RMF and ROP models** can be implemented in **generators** to predict lepton and hadron kinematics in the FS. Partially implemented in GENIE. Work in progress for NEUT.
- **Uncertainties in nuclear potentials:** SF profiles, binding energies, occupancy, transparency, etc. can be added. See PRD106, 113005 (2022) and PRD109, 013004 (2024) for details.

## Scattered Nucleon Description

Regarding the scattered nucleon, we can consider several situations:

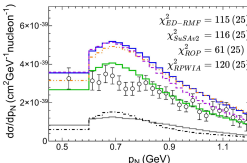
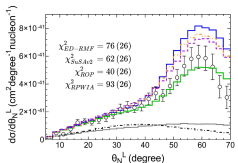
- **Relativistic Plane-Wave Impulse Approximation (RPWIA):** the ejected nucleon is considered a plane-wave (i.e., there are not final state interactions)
- **Energy-Dependent Relativistic Mean Field (ED-RMF):** W.F. solution of the Dirac equation in the continuum using the same RMF potential that describes the initial state times a phenomenological function that weakens the potentials at high energies.
- **Relativistic Optical Potential (ROP):** The scattered nucleon travels under the influence of a phenomenological relativistic optical potential fitted to elastic proton-nucleus scattering data.

## Cross sections vs proton kinematics: T2K and MINERvA



*Phys. Rev. D* 98, 032003(2018)

*T2K*  $\nu_\mu - CC0\pi Np$   
 $p_N > 500$  MeV/c



*Phys. Rev. D* 101, 092001(2020)

*MINERvA*  $\nu_\mu - CC0\pi Np$

$k'$	$\cos\theta_N$	$p_N$	$\cos\theta_N^L$	$\phi_N^L$
1.5-10 GeV	> 0.939	0.45-1.2 GeV	> 0.342	-

- **SuSAv2 model** based on scaling functions from RMF theory has been recently extended to the full inelastic regime (RES, SoftDIS, TrueDIS) where RMF models are not yet fully developed.
- **Unlike RMF**, SuSAv2 only predicts lepton kinematics but shows good agreement with  $e$  and  $\nu$  data.
- Recent implementation of **Osaka-DCC RES model (SuSAv2-DCC)**. Comparisons with **NEUT-DCC** are under way.

## Results: T2K

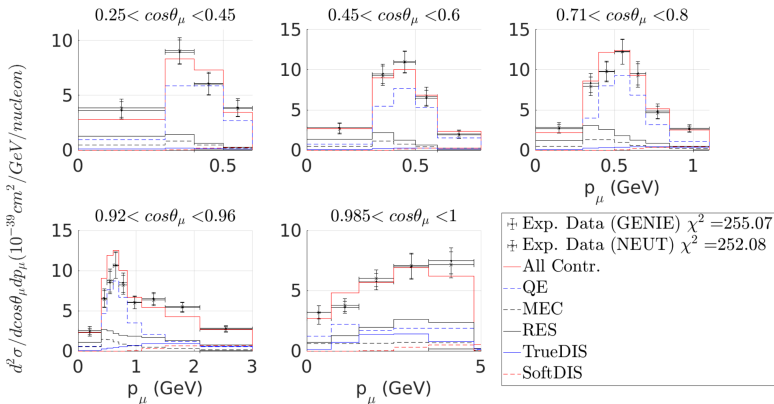
T2K CC  $\nu_{\mu} < E_{\nu_{\mu}} > \sim 0.6 \text{ GeV}$

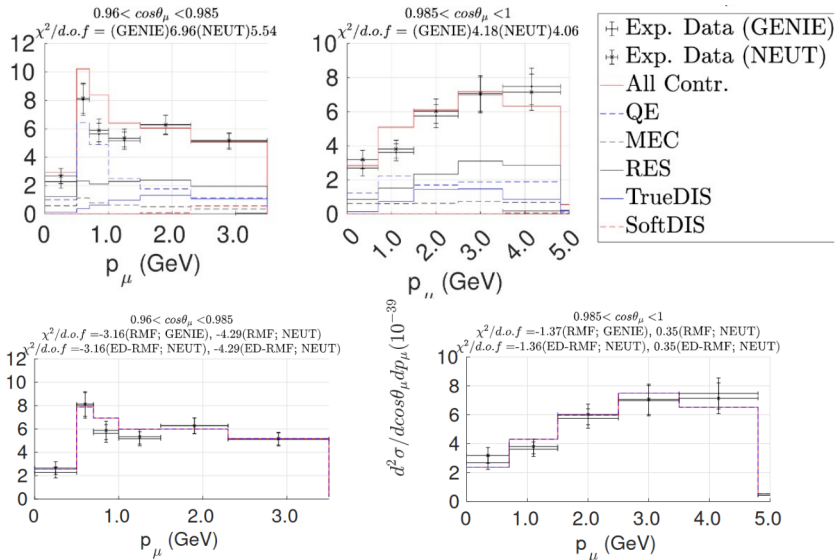
$$\chi^2 = 218.3$$

(GENIE)

$$\chi^2 = 192.0$$

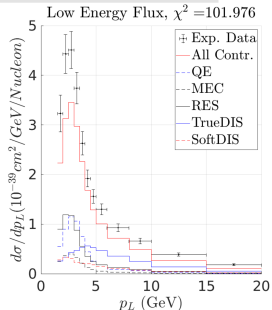
(NEUT)



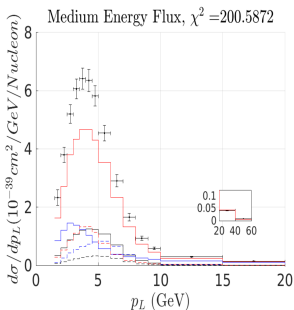


Overestimations at very forward angles in SuSAv2 are solved using RMF models.

## Results: MINERvA



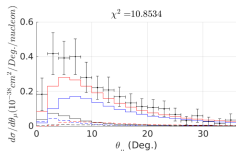
MINERvA CC  $\nu_\mu < E_{\nu_\mu} > \sim 3.5 \text{ GeV}$  (Low)



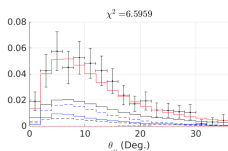
MINERvA CC  $\nu_\mu < E_{\nu_\mu} > \sim 6.0 \text{ GeV}$  (Medium)

More strength seems to be needed in **RES** channel to compare with **MINERvA** and **MnvGENIE**, unlike **ArgoNEUT** (similar  $E_\nu$ ) and **T2K** (lower  $E_\nu$ )

## Results: ArgoNEUT



ArgoNEUT CC  $\nu_\mu < E_{\nu_\mu} > \sim 9.6 \text{ GeV}$ ; CC  $\bar{\nu}_\mu < E_{\nu_\mu} > \sim 3.6 \text{ GeV}$



See *PRD 105, 093009 (2022)* and *PRD 108, 113008 (2023)* for details.

Analysis with *NOvA* results are under way.

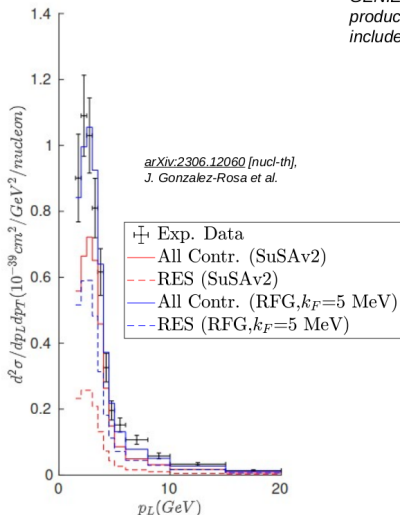


# Uncertainties in nuclear models, reweighting and tuning

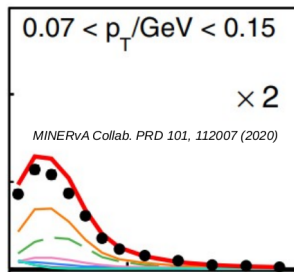
MINERvA Low Flux

$0.075 < p_T/\text{GeV} < 0.15$

$\chi^2 = 3.49$  (SuSAv2); 3.44 (RFG)



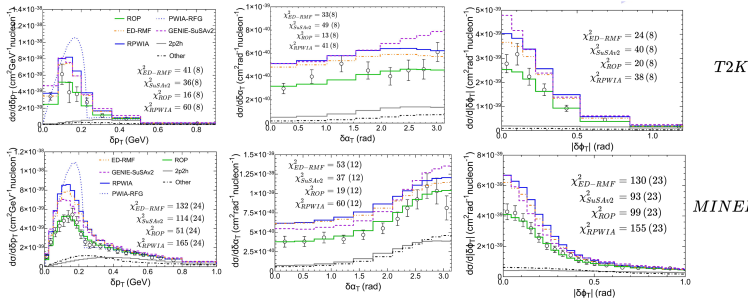
- MC tuning, reweighting or model approaches in the RES and SoftDIS (Background) channels for neutrinos should be validated against electron scattering data.
- GENIE Mnv RES approach is based on a single-nucleon Rein-Sehgal pion production model with lepton mass corrections and other modifications to include nuclear effects. But, it looks similar to a low- $p_F$  RFG model.



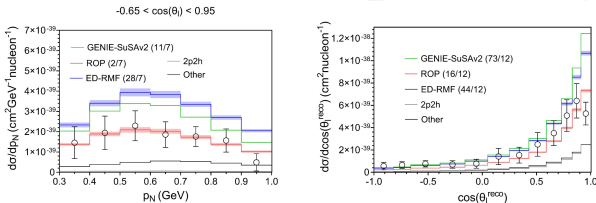
- ✦ MINERvA data
- MnvGENIE v1
- - QE+2p2h
- RES
- True DIS
- Soft DIS
- Other CC
- Background



# Cross sections vs transverse kinematic imbalances

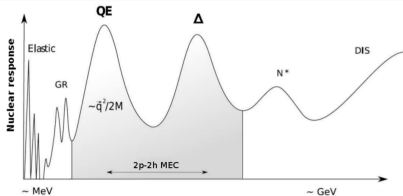


# Cross sections vs MicroBooNE $\nu_\mu \rightarrow 40\text{Ar} \text{CC}0\pi\text{IN}$

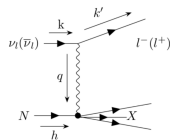


We can also add uncertainties in the nuclear potential parameters, SF profile, binding energies, occupancy, transparency, etc. Error bands included in MicroBooNE plots for reference.

See Phys. Rev. D 106, 113005 (2022) and Phys. Rev. D 109, 013004 (2024) for details.



- Quasielastic region.
- 2p-2h excitations.
- $\Delta$  resonance, other resonances and DIS.



SuSAv2-inelastic model describes the full inelastic spectrum ( $\Delta$ , other res. And DIS) [G. D. Megias, PhD Thesis (2017), M. B. Barbaro et al., Phys. Rev. C 69, 035502 (2004), J. Gonzalez-Rosa et al., Phys. Rev. D 105, 093009 (2022)]. Good agreement with  $(e, e')$  data.

$$R_{inel}^K(\kappa, \tau) = \frac{N}{\eta_F^2 \kappa} \xi_F \int_{\mu_X^{min}}^{\mu_X^{max}} d\mu_X f^{model}(\psi_X') U^k$$

- TrueDIS (Deep inelastic scattering)

$$W_x^{min} = 2.1 \text{ GeV}; W_x^{max} = m_N + \omega - E_S$$

Bodek-Ritchey/ Bosted-Christy/ Parton Distribution Function

- RES (Resonances)

$$W_x^{min} = m_N + m_\pi; W_x^{max} = 2.1 \text{ GeV}$$

Dynamical Coupled Channels

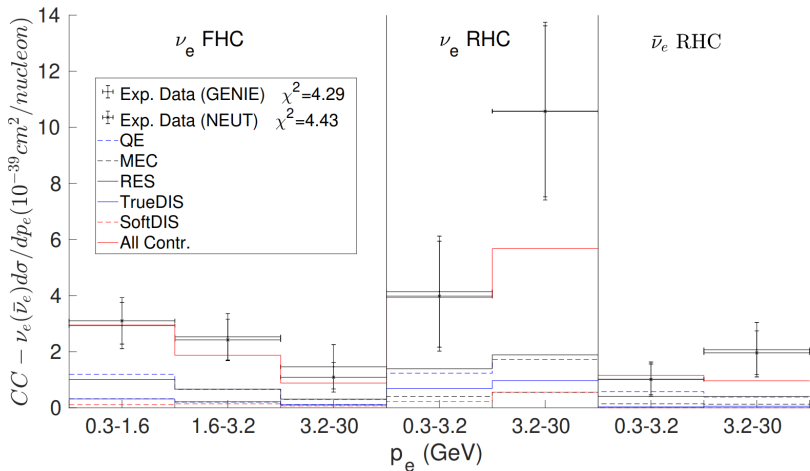
- SoftDIS (Deep inelastic scattering in the resonance region)

$$W_x^{min} = m_N + m_\pi; W_x^{max} = 2.1 \text{ GeV}$$

Dynamical Coupled Channels and Bodek-Ritchie/Bosted-Christy

- **SuSAv2 model for QE** uses RMF scaling function to model nuclear dependence. Similar approach is done for **inelastic regime**.
- **Inelastic hadron tensor** includes: **RES** (DCC model) + **DIS** (Bodek-Ritchey/Bosted-Christy/PDFs) + **soft DIS** (merge).
- **SuSAv2 inelastic** can be implemented in NEUT or GENIE to predict lepton kinematics and shortly for nucleon kinematics (work in progress with S. Dolan and L. Munteanu).
- Comparisons with **NEUT DCC (RFG)** in collaboration with Hayato-san *et al.* are under way.
- This approach can **incorporate** other inelastic models.

# SuSAv2 model for inelastic electron neutrino-nucleus scattering



Overestimations at large  $p_e$  in RHC mode will be studied.