

令和五年度東京大学宇宙線研究所共同利用研究成果発表会

Research Result Presentation meeting of
the ICRR Inter-University Research Program

**Filter cavity experiments
for Frequency Dependent Squeezed light source
(with Machine Learning Quantum State Tomography)
for KAGRA**

PhD students: Yi-Ru Chen, Hsun-Chun Wu, Hua Li Chen, Jingyu Ning,
Dr. Hsien-Yi Hsieh, Dr. Chien-Ming Wu, Ray-Kuang Lee 李瑞光*

National Tsing Hua University (NTHU), Taiwan

Shinji Miyoki

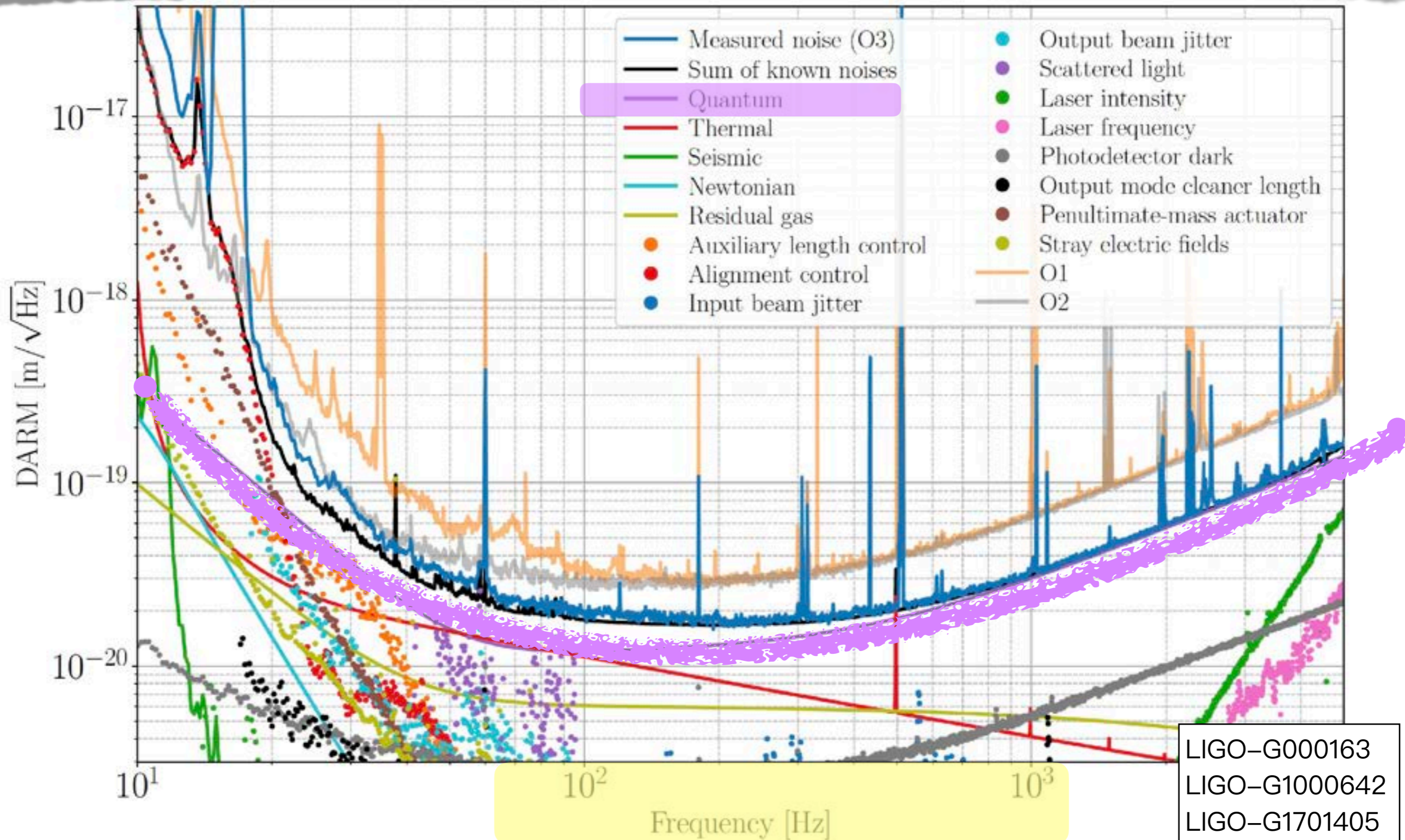
(+Marc Eisenmann, Michael Page, Yoichi Aso, Takayuki Tomaru)

(+Yu-hang Zhao, Matteo Leonardi)



Feb. 21st, 2024

Noise Budget:

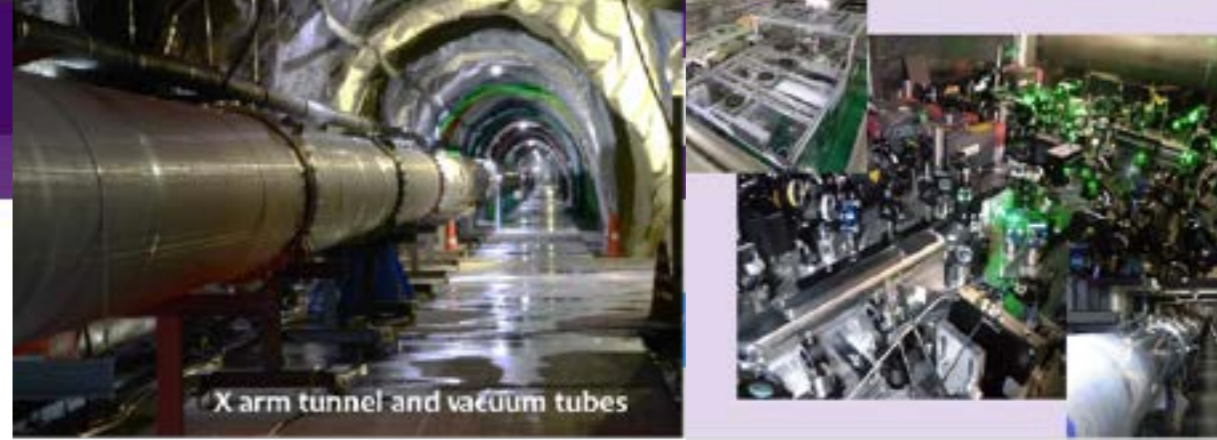


Synopsis: Feeling the Squeeze at All Frequencies

April 28, 2020 • Physics 13, s55

Two teams demonstrate frequency-dependent quantum squeezing, which could double the sensitivity of gravitational-wave detectors.

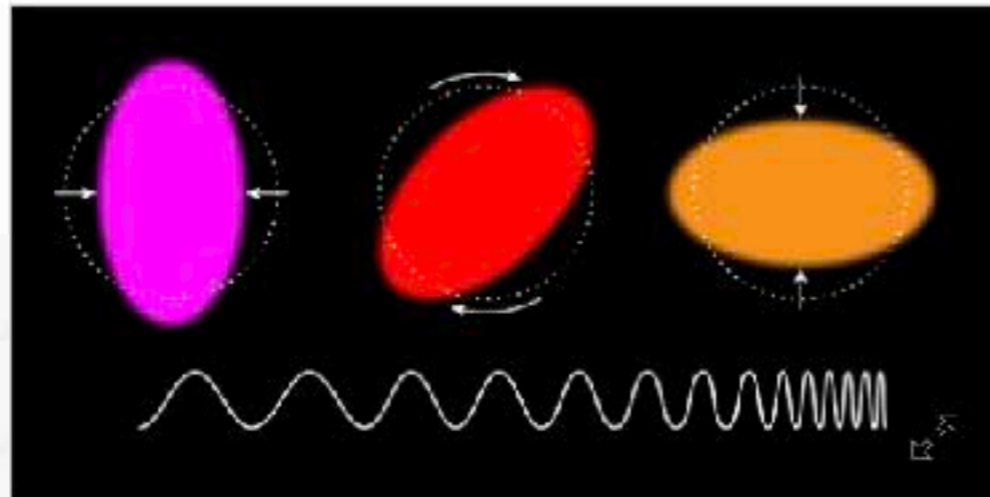
The First Experimental Realization of FDS at 70 Hz.



Frequency-Dependent Squeezed Vacuum Source for Broadband Quantum Noise Reduction in Advanced Gravitational-Wave Detectors

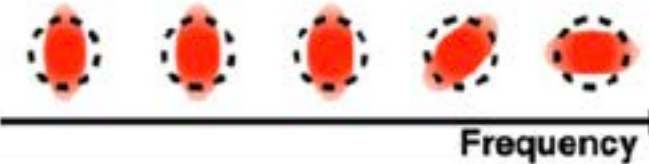
Yuhang Zhao, Naoki Aritomi, Eleonora Capocasa, Matteo Leonardi, Marc Eisenmann, Yuefan Guo, Eleonora Polini, Akihiro Tomura, Koji Arai, Yoichi Aso, Yao Chin Huang, Ray Kuang Lee, Harald Lück, Osamu Miyakawa, Pierre Prat, Ayaka Shoda, Matteo Tacca, Ryutaro Takahashi, Henning Vahlbruch, Marco Vardaro, Chien-Ming Wu, Matteo Barsuglia, and Raffaele Flaminio
 Phys. Rev. Lett. 124, 171101 (2020)
 Published April 28, 2020

KAGRA Filter Cavity (KFC) Team



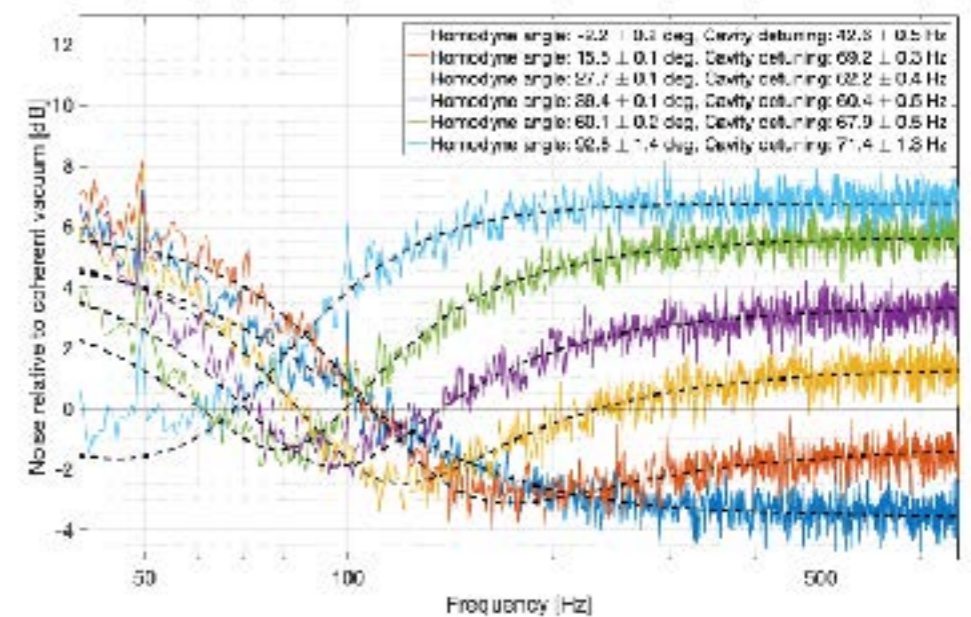
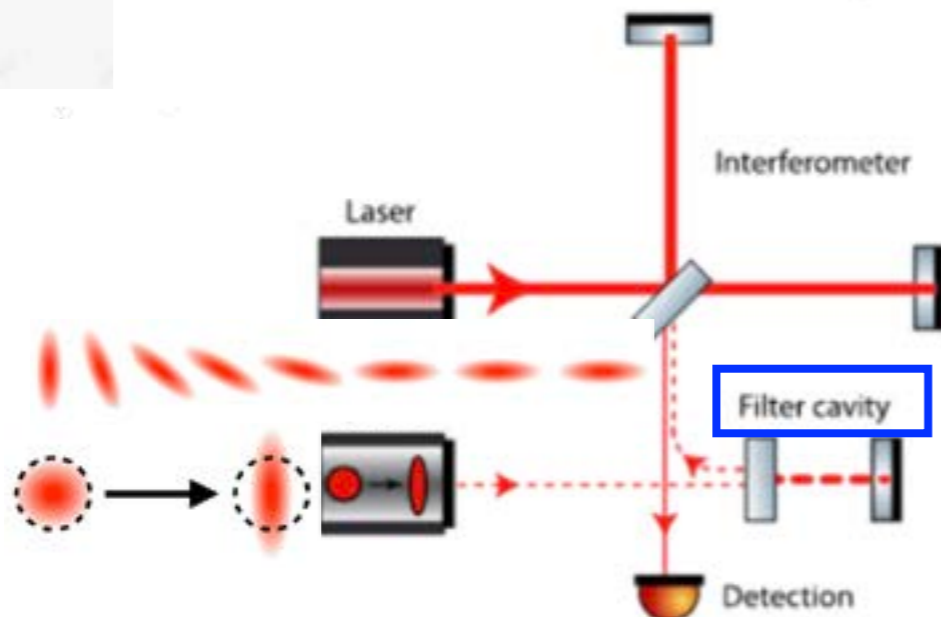
APS/Alan Stonebraker

Frequency dependent squeezed vacuum state



FDS

FIS



Degradation in Squeezers

- ✓ **Frequency-Dep. Squeezing (FDS) for GW detectors** w/ NAOJ PRL 124, 171101 (2020).

Unavoidable coupling from the noisy environment makes the quantum light in a mixed state with **Degradation** embedded.

- ✓ **Extract the Degradation Information in Squeezed States with Machine Learning**, Phys. Rev. Lett. 128, 073604 (2022); **Fiscal Year 2021**
- ✓ **Direct parameter estimations from Machine Learning-enhanced Quantum State Tomography**, Symmetry, 14, 874, (2022); **Fiscal Year 2022**
- ✓ **Neural network enhanced single-photon Fock state tomography**, Adv. Quant. Tech. (Invited Paper, 2024); **Fiscal Year 2023**
- ✓ **Reconstruct Wigner current in Decoherence**, Phys. Rev. A 108, 023729 (2023); **Fiscal Year 2023**
- **Utilize: Generation of heralded optical 'Schrodinger cat' states by photon-addition**, arXiv: 2306.13011 (2023); **Fiscal Year 2023**

Cavity Parameter

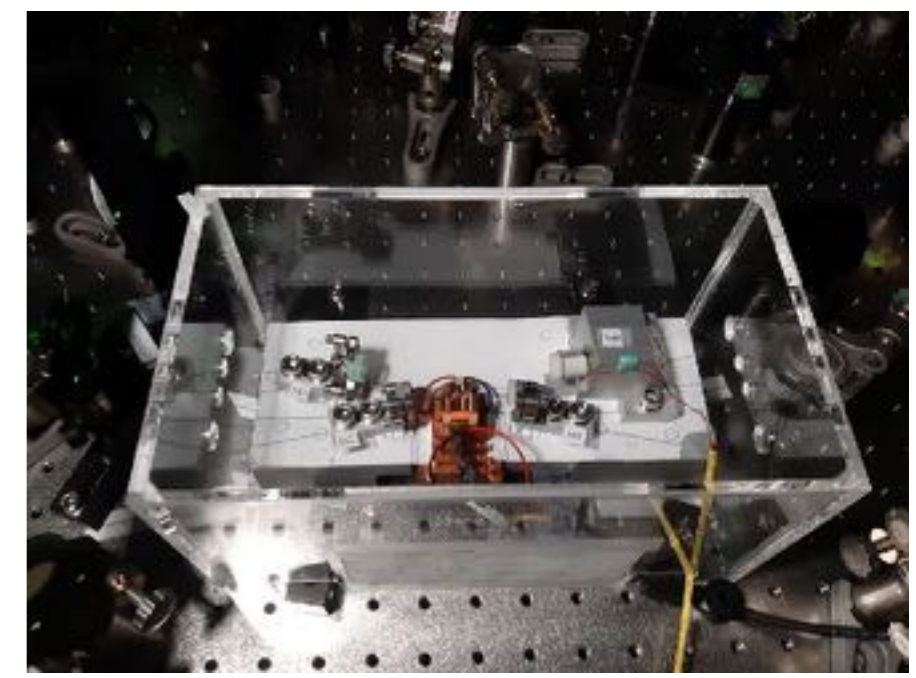
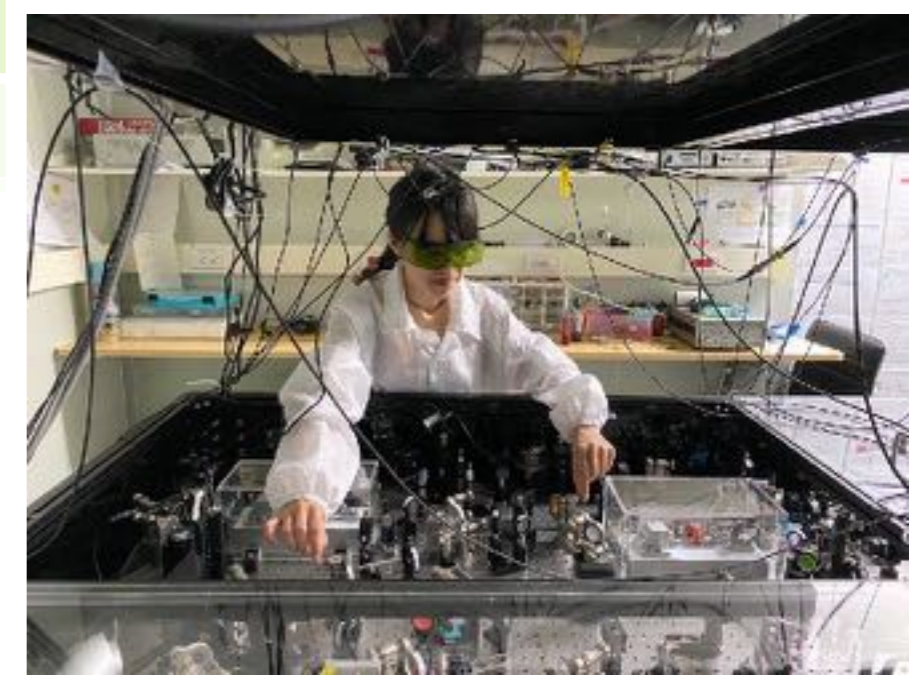
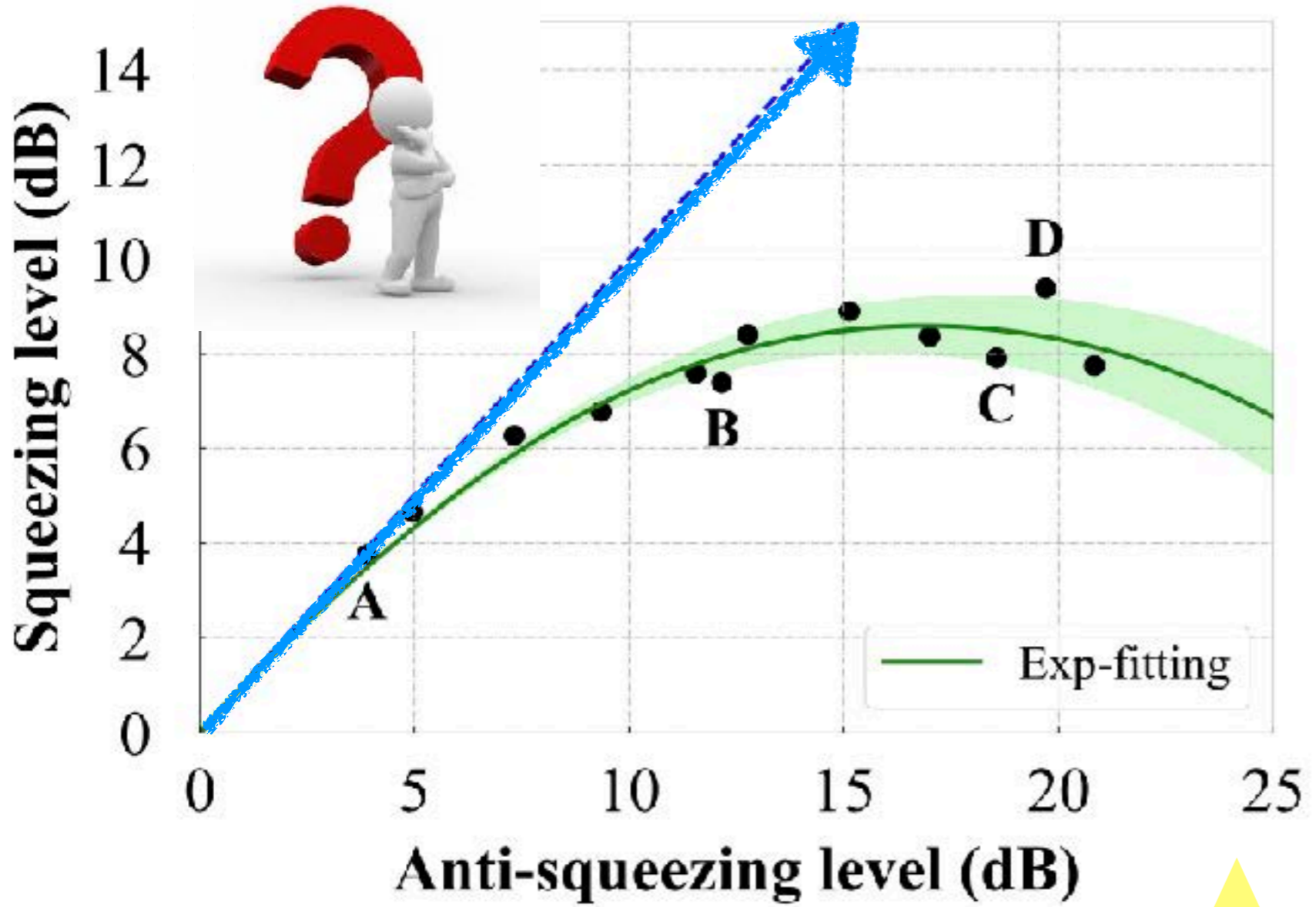
Value

Units

Fundamental field Wavelength

1064

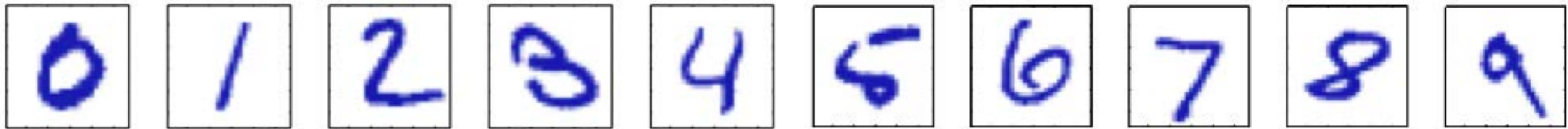
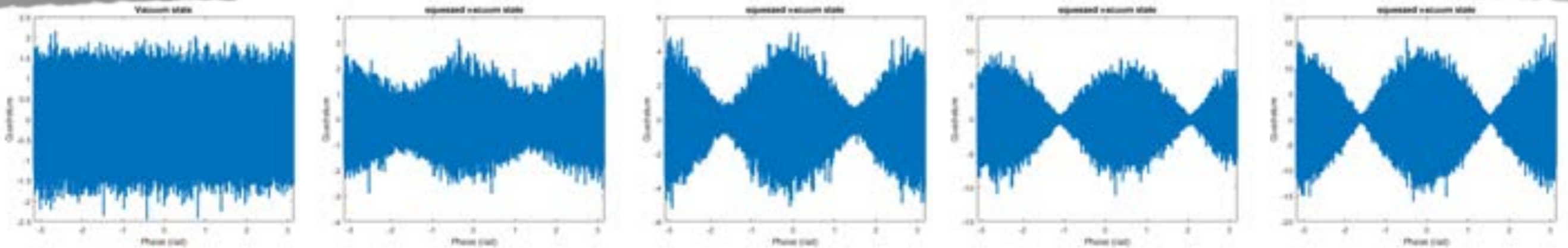
nm



Estimation:
16.2 dB Squeezing

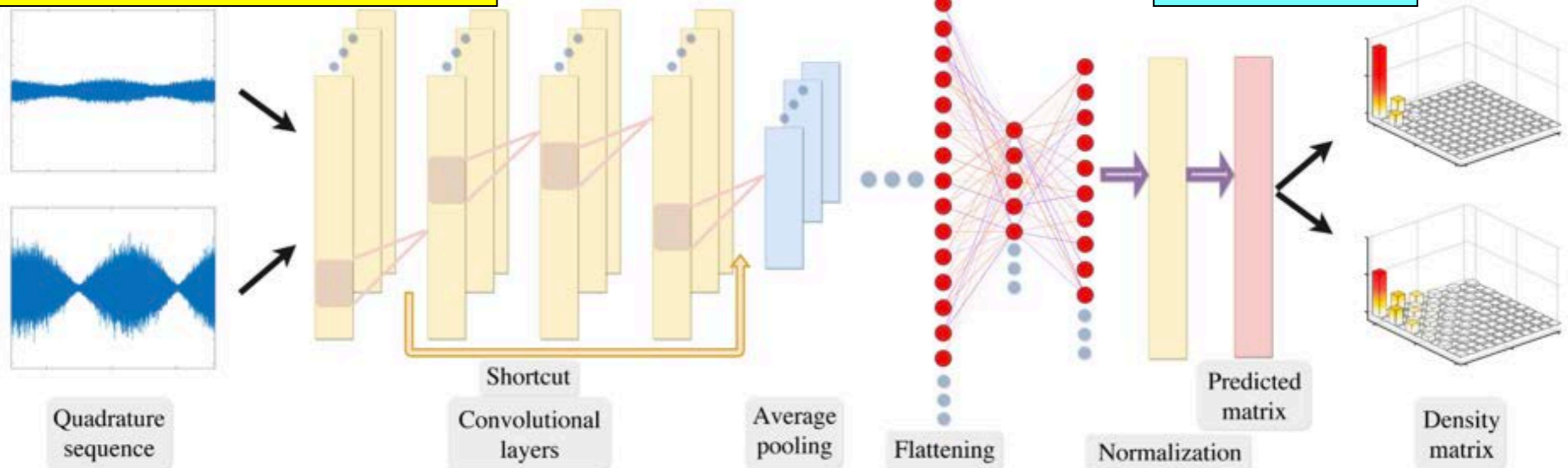
by
Yi-Ru Chen
Chien-Ming Wu

Pattern Recognition & Machine Learning



Convolution Neural Network (CNN)

by Hsieh-Yi Hsieh



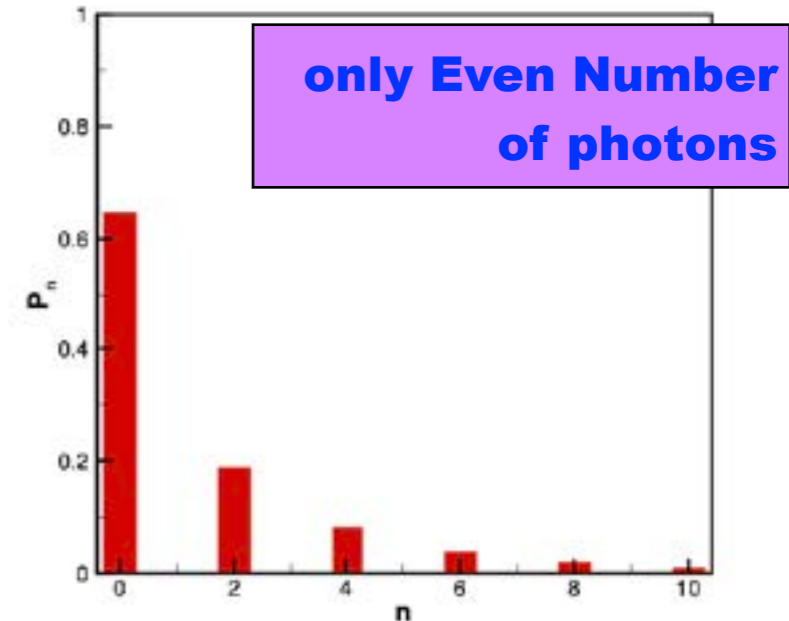
Applications of real-time tomography in squeezed state:

- Monitor the purity of a quantum state in real-time, and reveal the dynamics.
- The purity of a normalized quantum state is a scalar defined as:

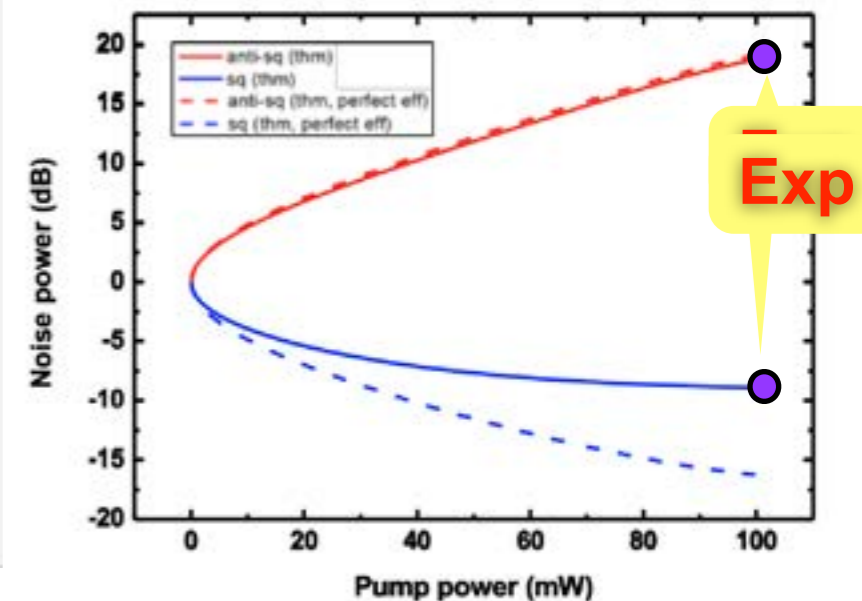
$$\gamma \equiv \text{tr}(\rho^2) , 0 < \gamma \leq 1$$

$\gamma = 1$ for pure squeezed state

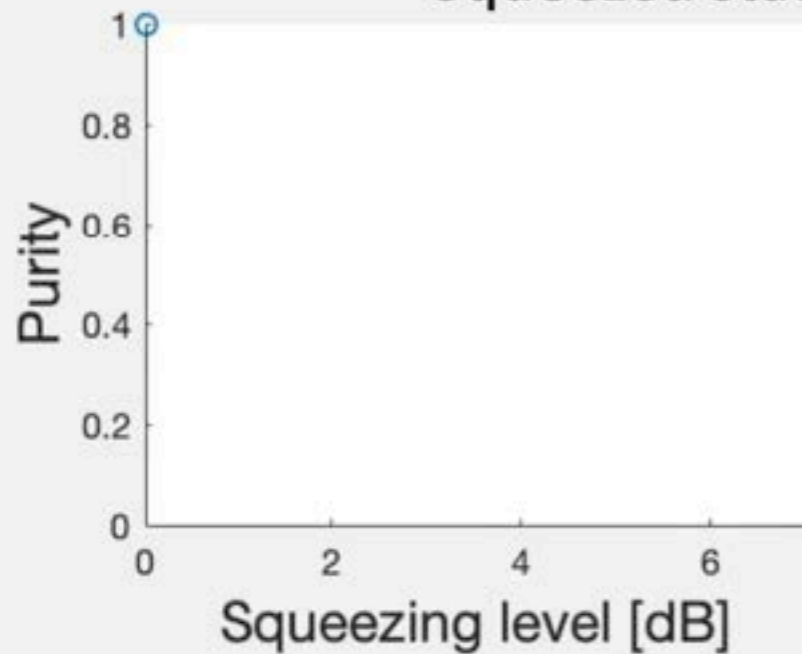
only Even Number of photons



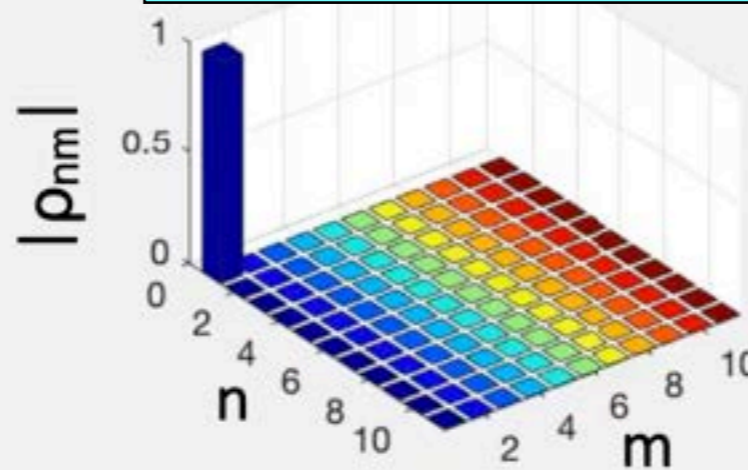
degrees of squeezing/anti-squeezing



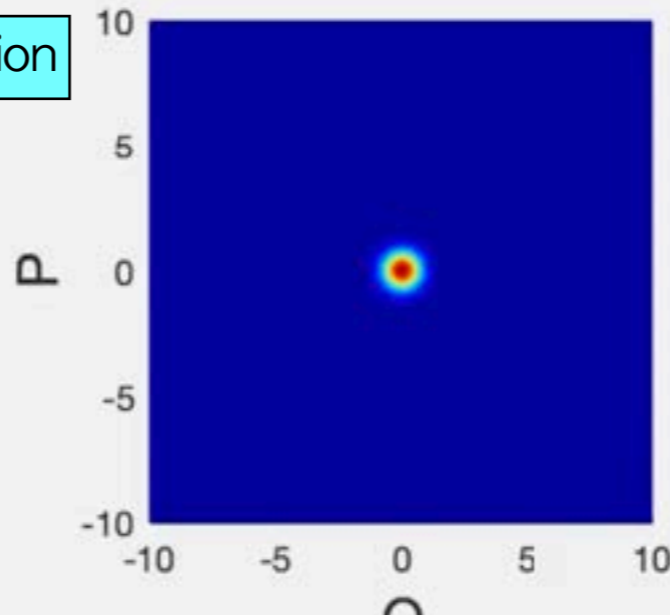
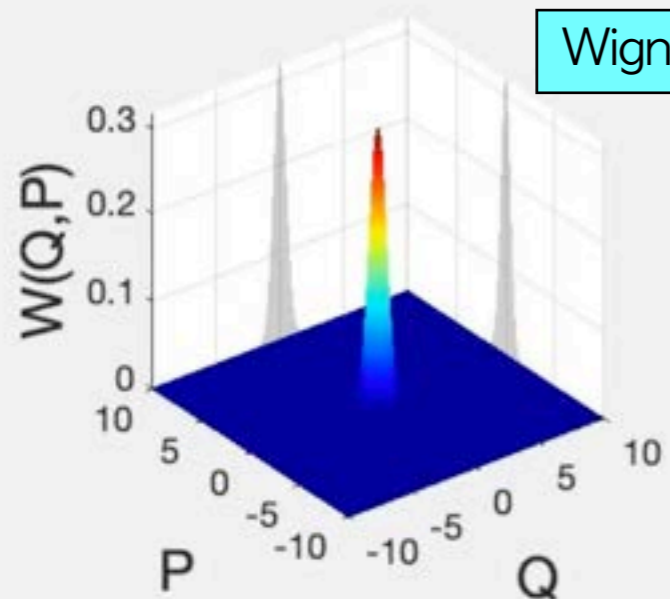
Squeezed state with loss



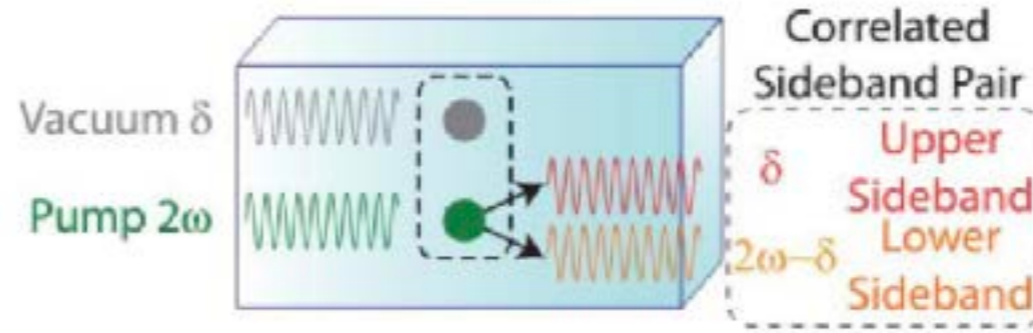
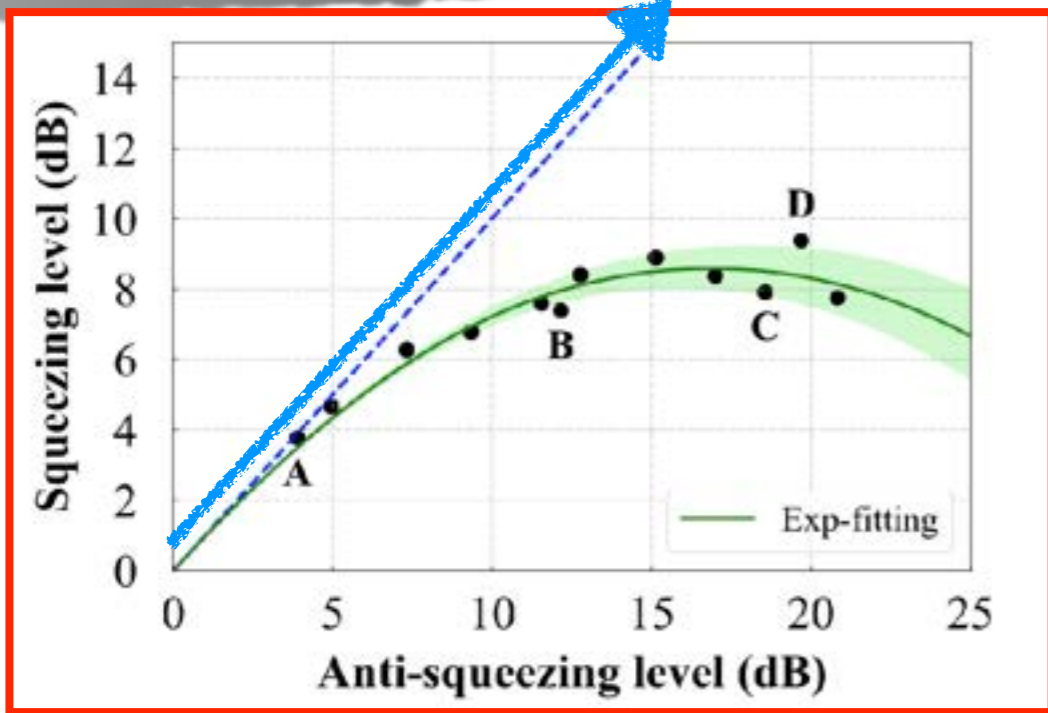
Density matrix in number basis



Wigner function



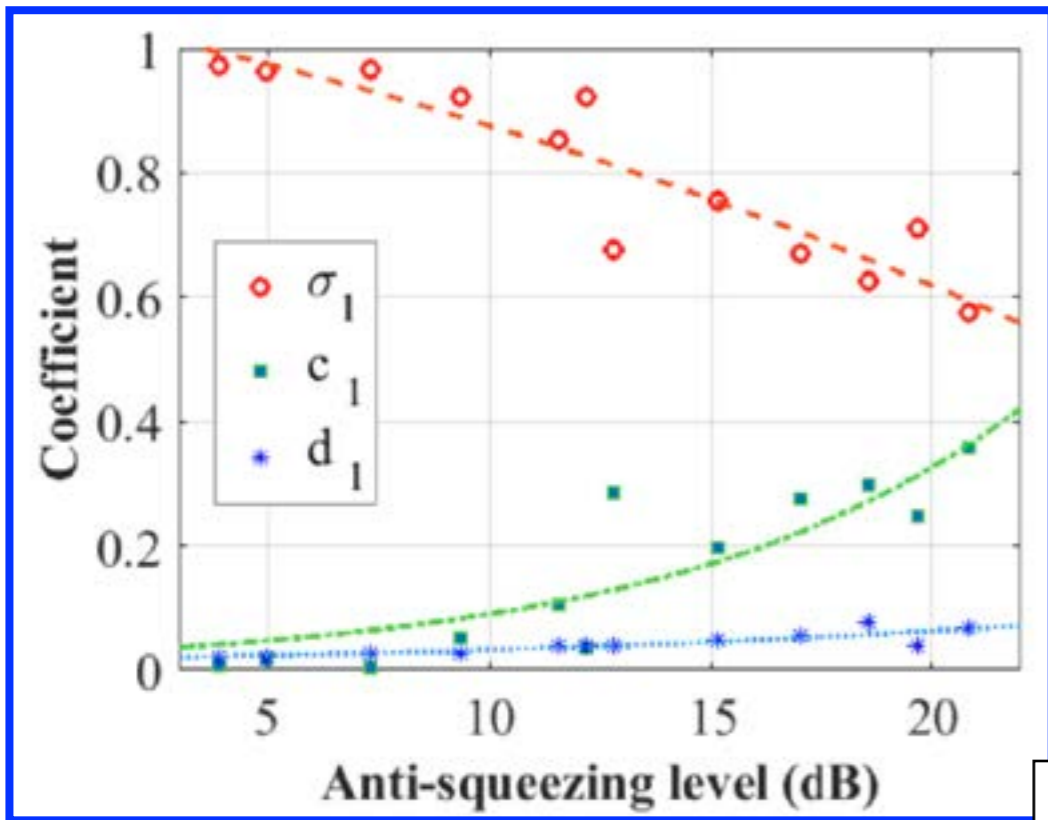
Degradation: Loss and Phase noise



Loss: L
Phase noise: θ

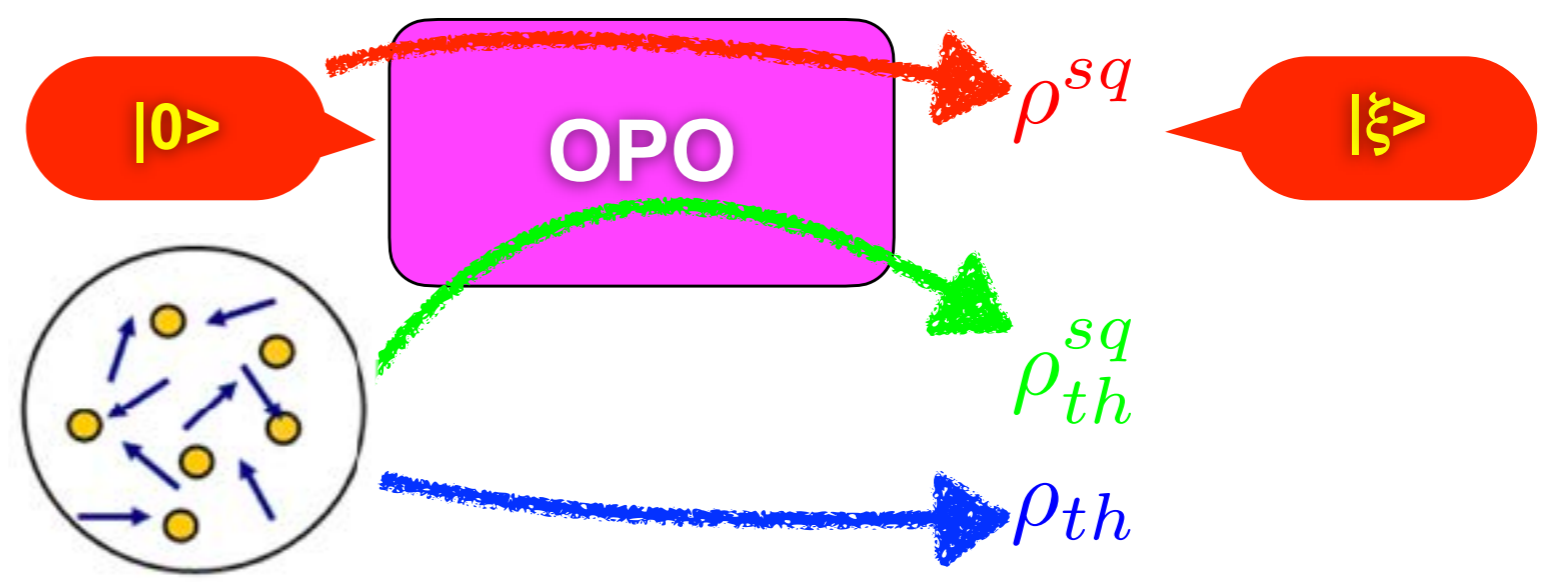
$$V^{sq} = (1 - L)[V_{id}^{sq} \times \cos^2\theta + V_{id}^{as} \times \sin^2\theta] + L,$$

$$V^{as} = (1 - L)[V_{id}^{as} \times \cos^2\theta + V_{id}^{sq} \times \sin^2\theta] + L,$$

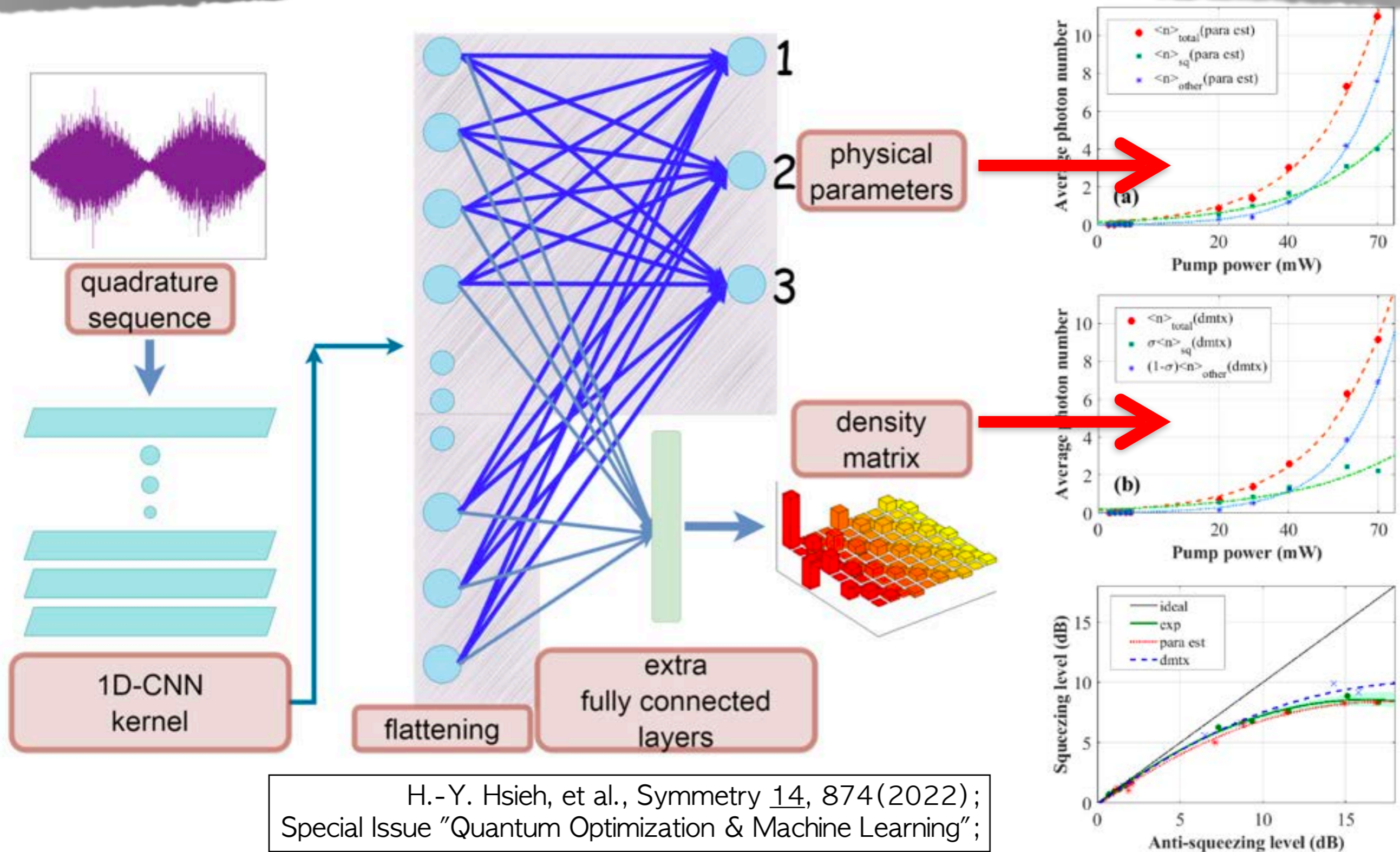


$$\rho = \sigma_1 \rho^{sq} + c_1 \rho_{th}^{sq} + d_1 \rho_{th}$$

SVD



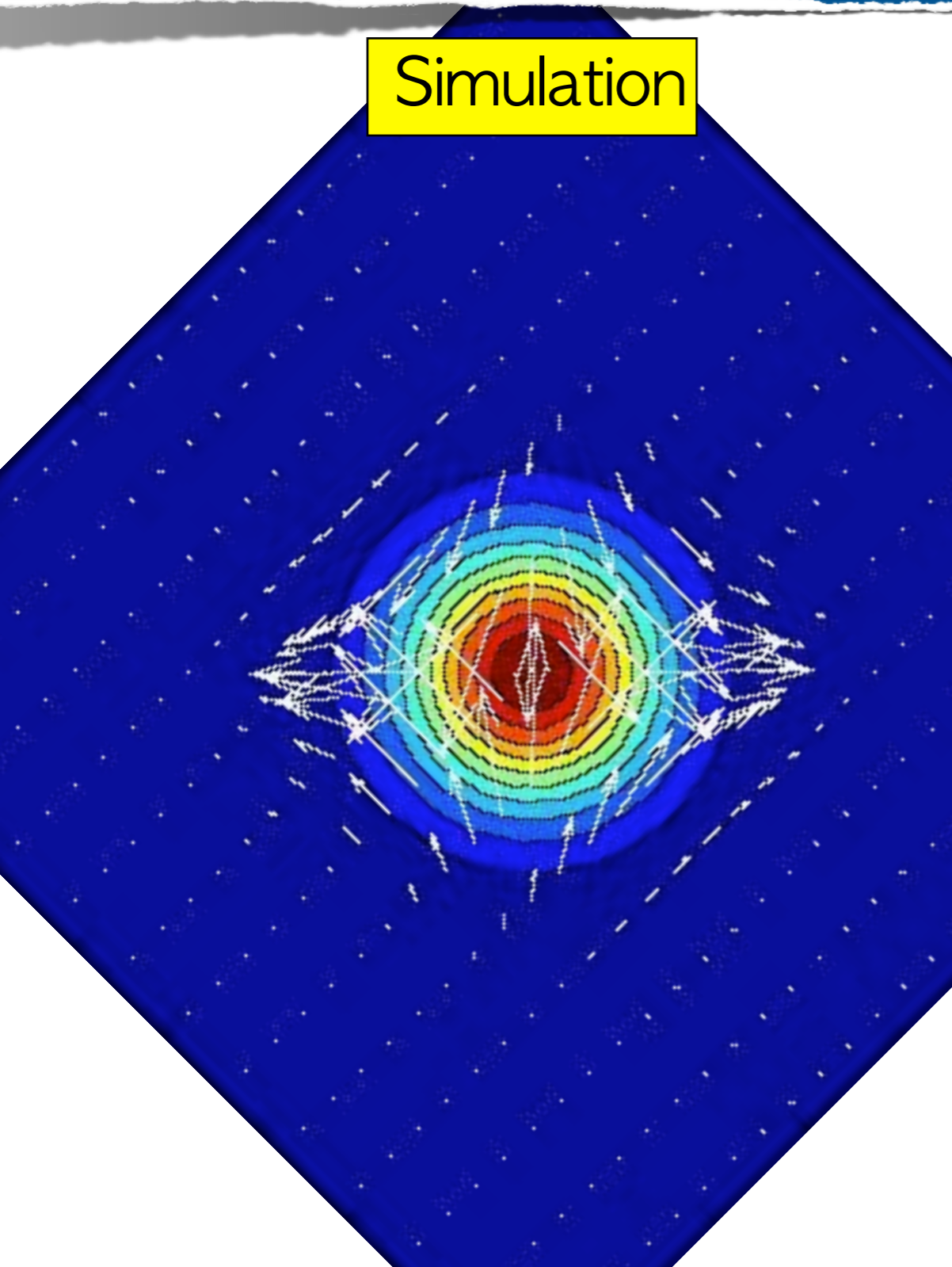
ML: Direct Parameter Estimations



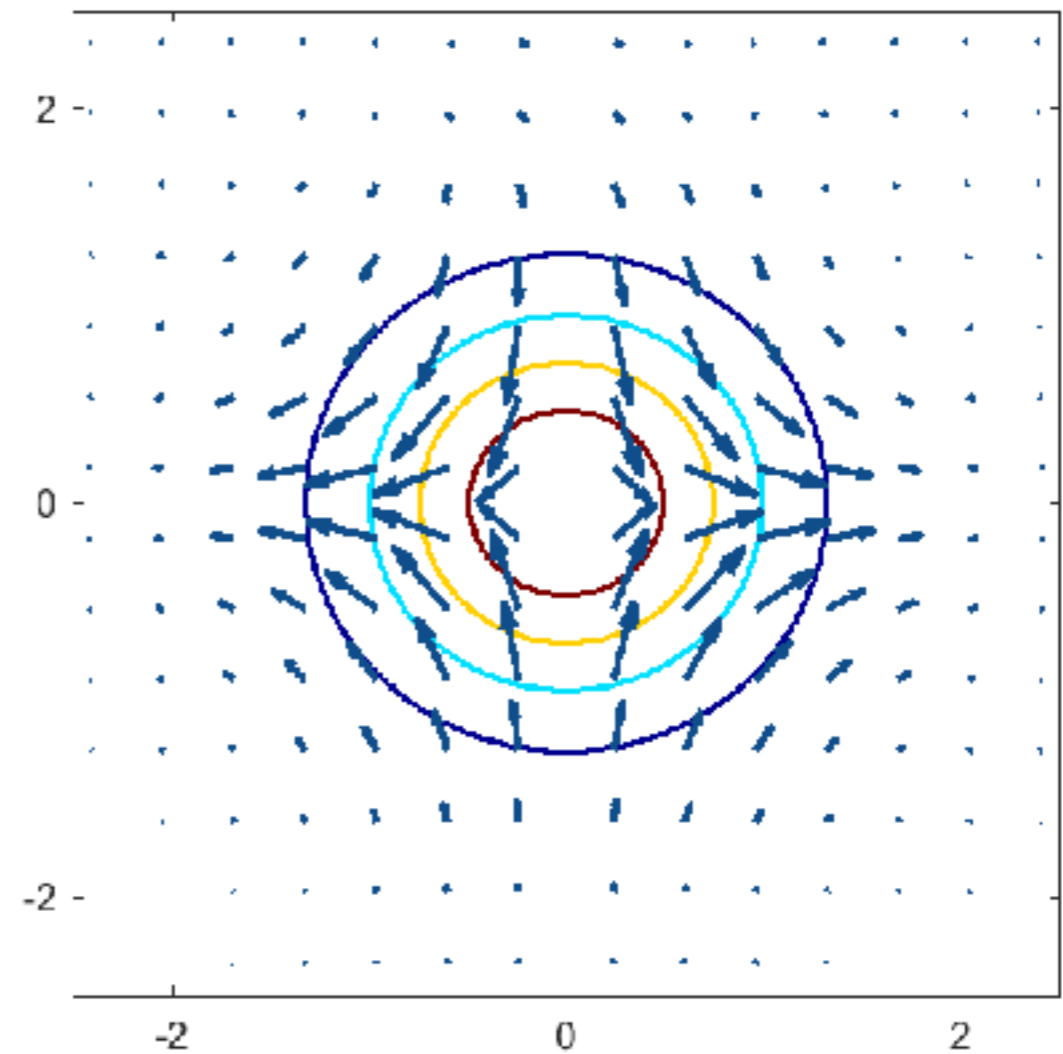
H.-Y. Hsieh, et al., Symmetry 14, 874(2022);
Special Issue "Quantum Optimization & Machine Learning";

Dynamics of Squeezers

Simulation

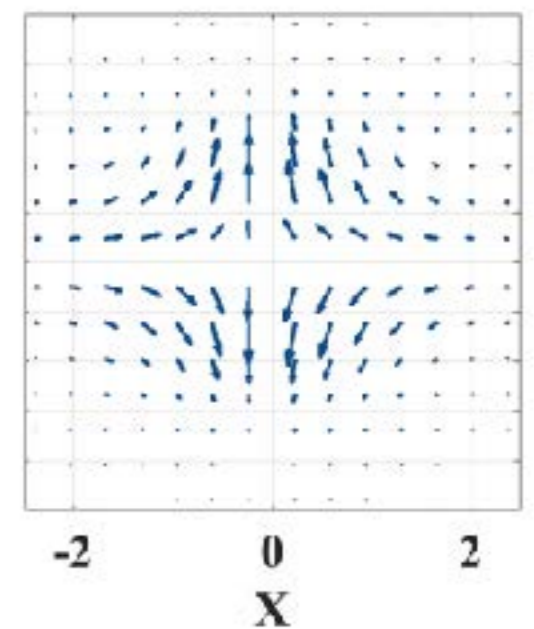
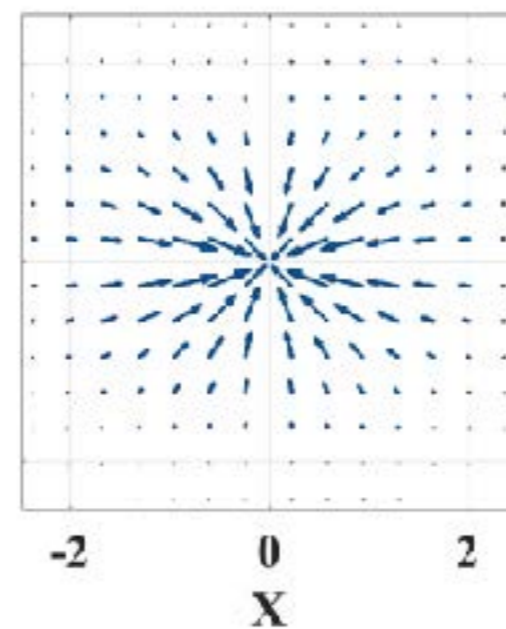
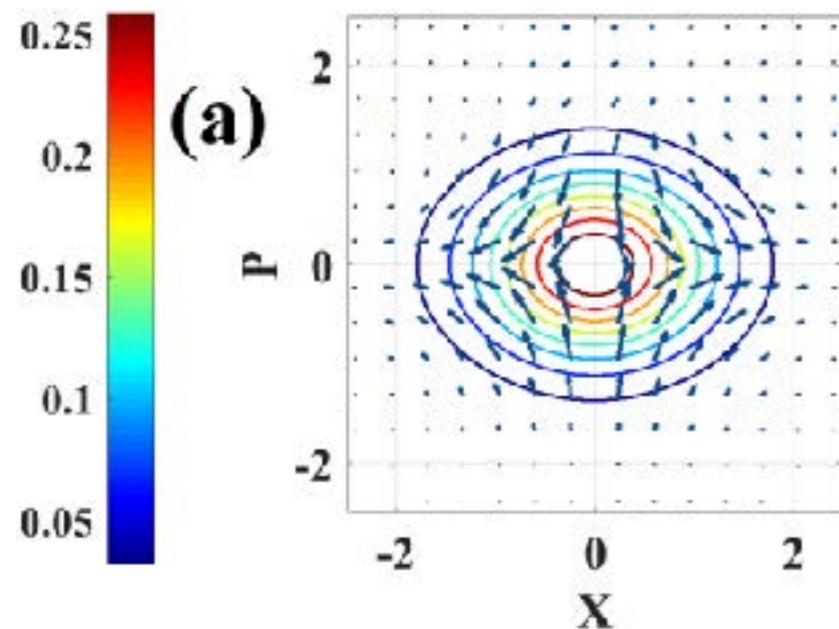
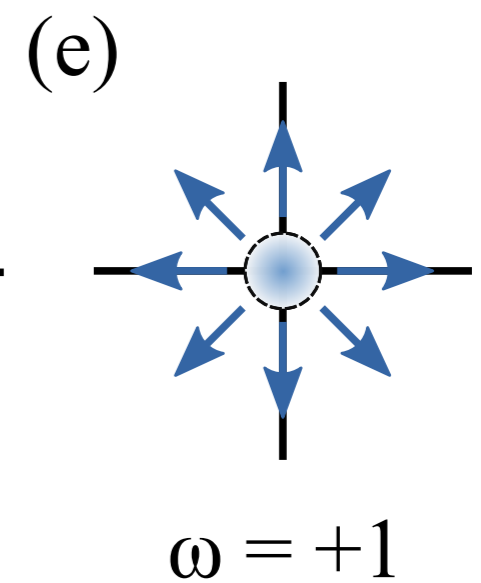
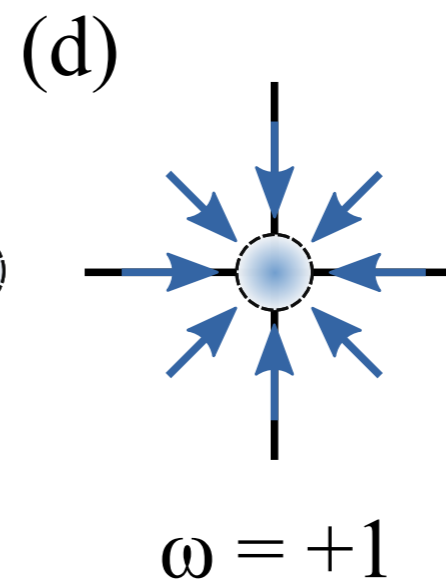
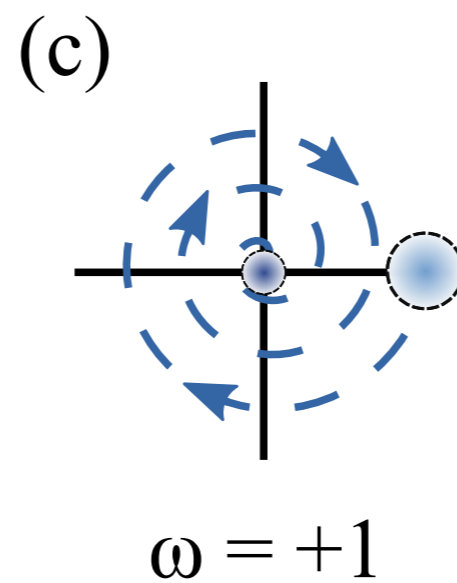
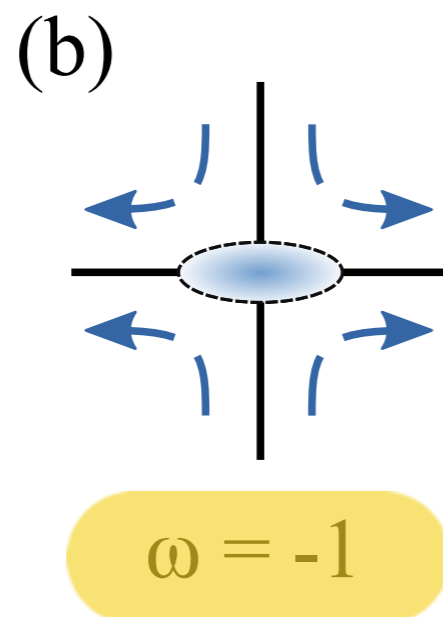
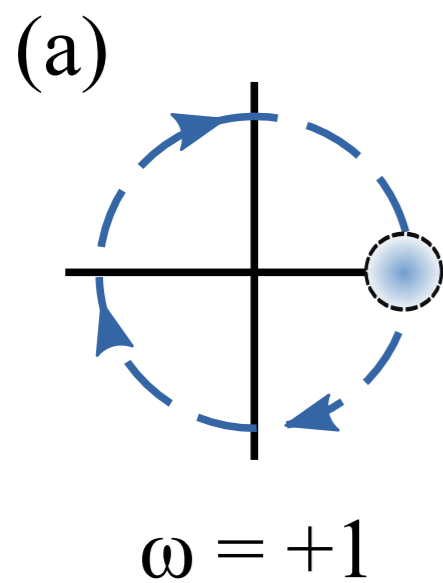


Exp. Reconstruction



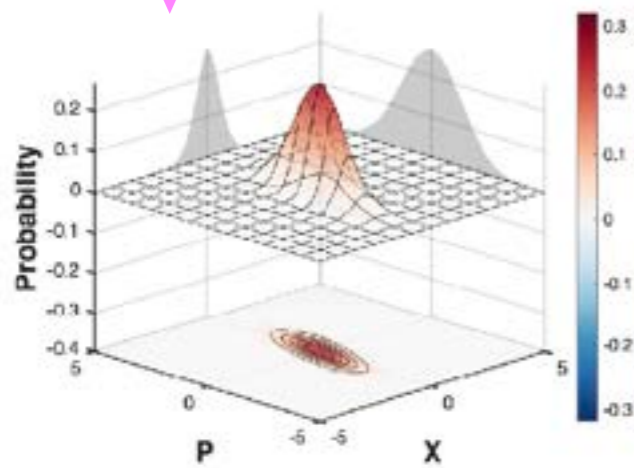
Yi-Ru Chen et al., Phys. Rev. A 108, 023729 (2023).

Topological Charges:

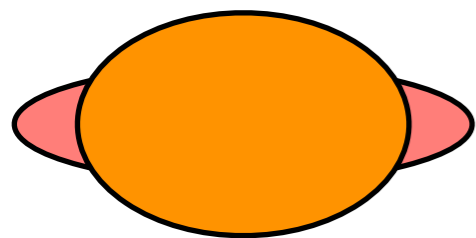
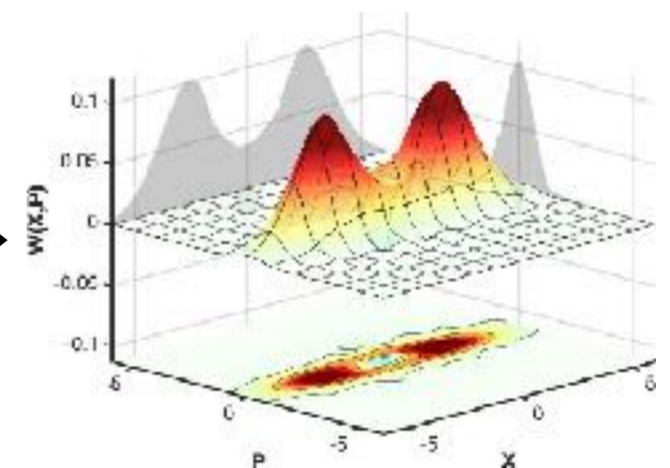
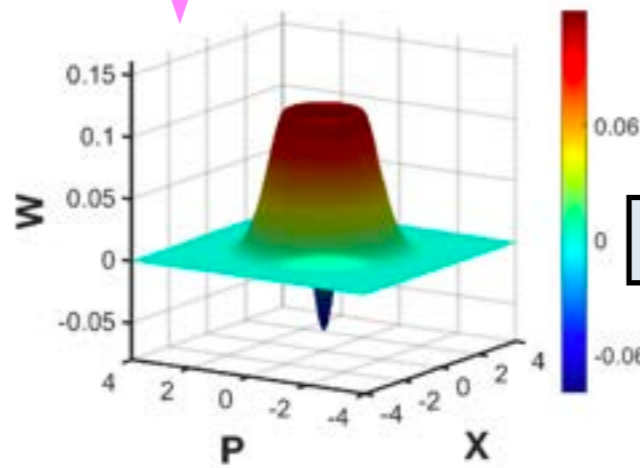


Photon-Addition

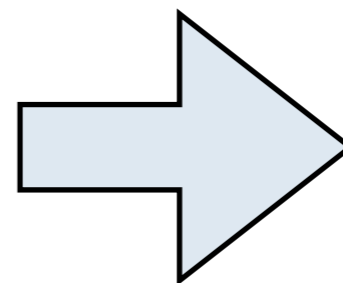
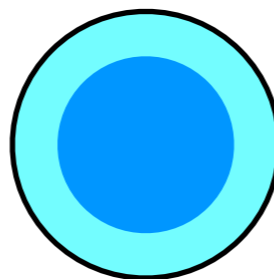
SQZ, $|\xi\rangle$



Single-photon, $|n=1\rangle$



+



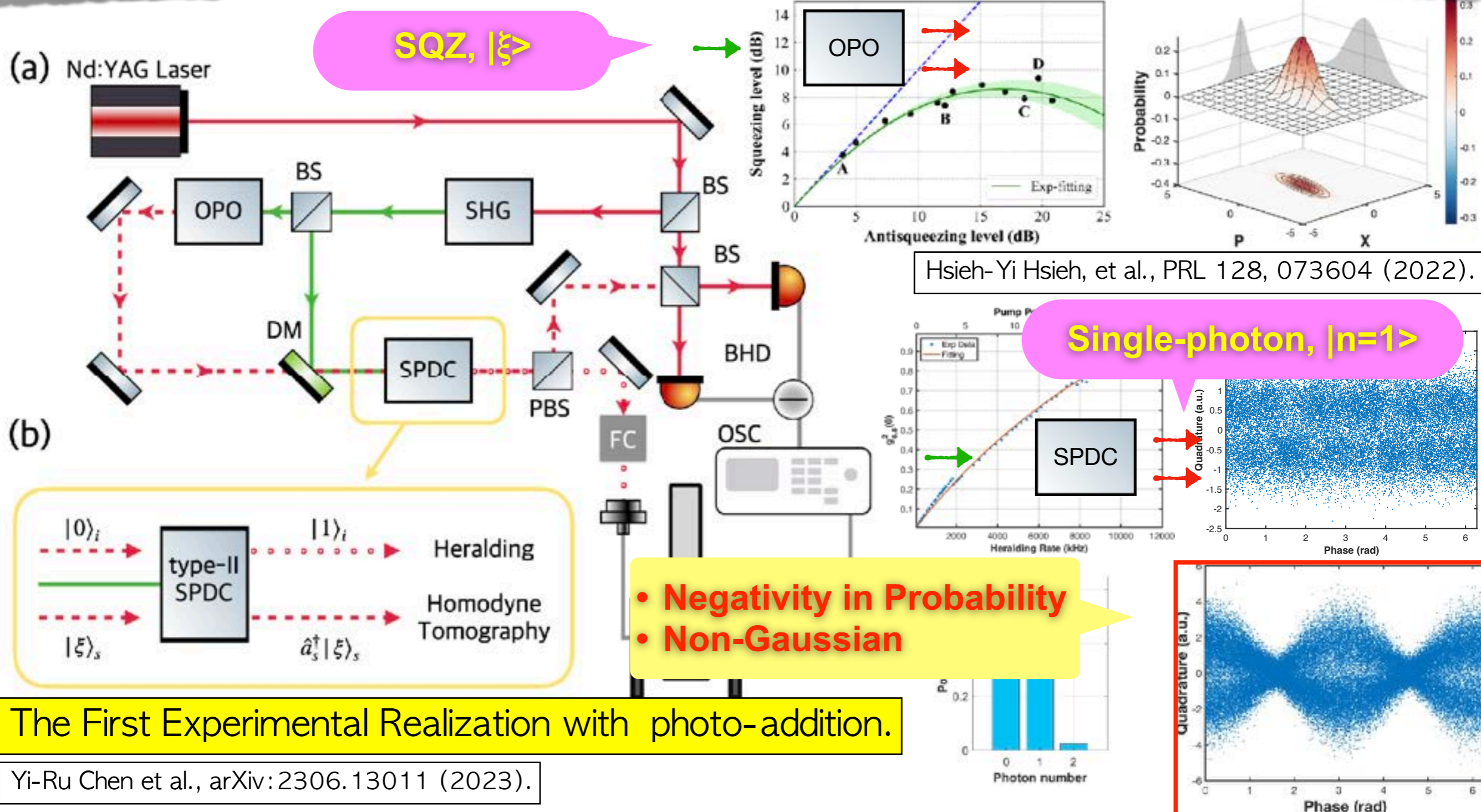
$\hat{a}^\dagger \hat{S} |0\rangle$



$$\hat{S}(g) = e^{g(\hat{a}_1 \hat{a}_2 - \hat{a}_1^\dagger \hat{a}_2^\dagger)} \approx 1 + g(\hat{a}_1 \hat{a}_2 - \hat{a}_1^\dagger \hat{a}_2^\dagger)$$

$$\hat{S}(g) \hat{S} |0\rangle_1 |0\rangle_2 \approx \hat{S} |0\rangle_1 |0\rangle_2 - g \hat{a}_1^\dagger \hat{S} |0\rangle_1 |1\rangle_2$$

Optical Cat states: by photon-addition



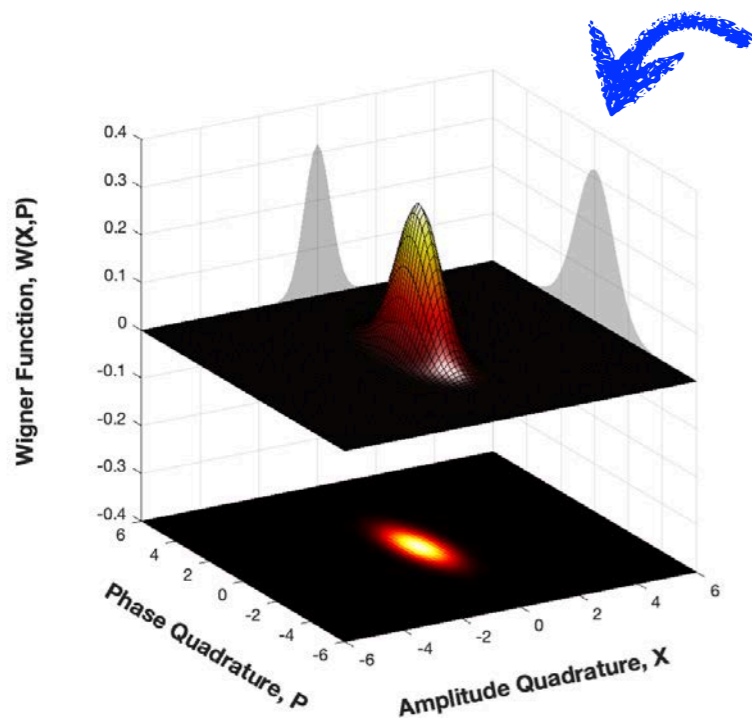
The First Experimental Realization with photo-addition.

Yi-Ru Chen et al., arXiv:2306.13011 (2023).

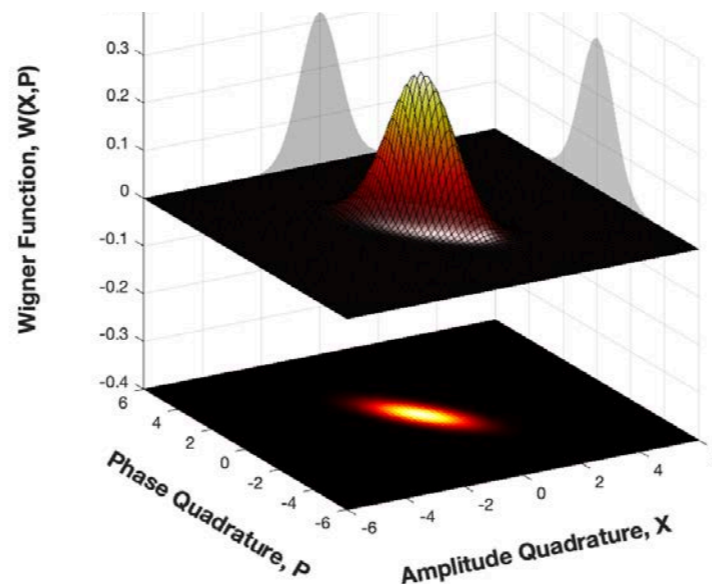
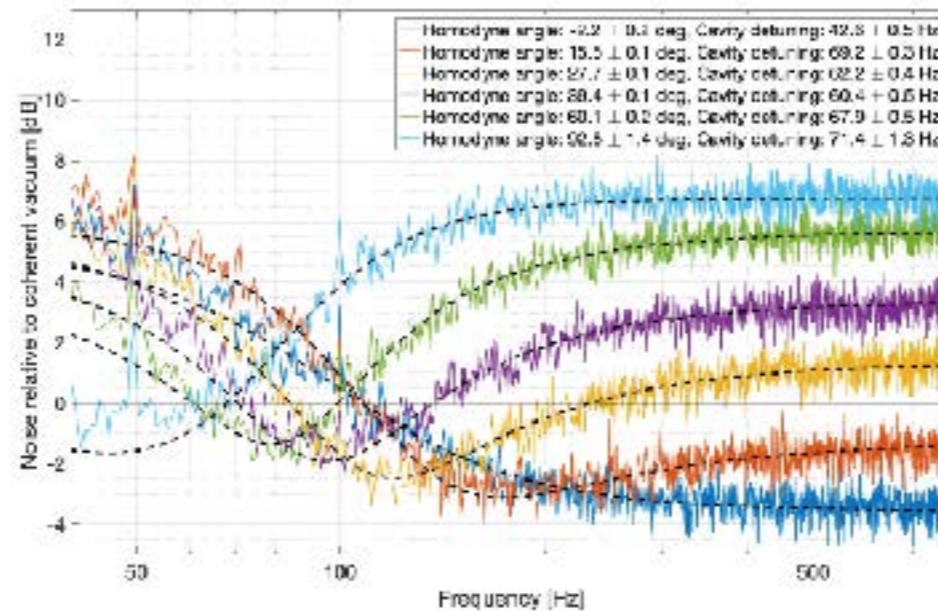
Neural network enhanced single-photon Fock state tomography, Invited paper to Adv. Quant. Tech. (2024).

Quantum State Tomography:

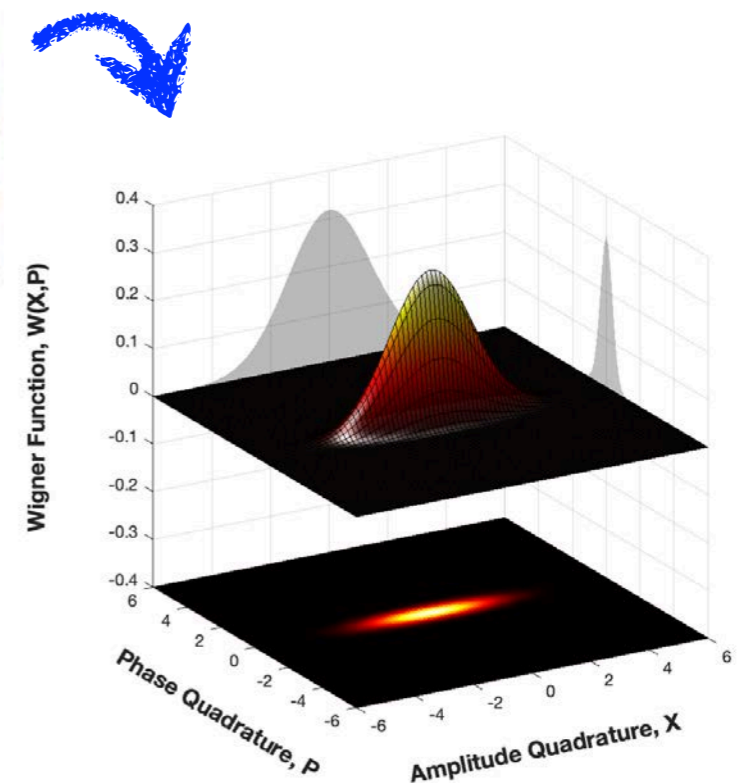
Can we Monitor the purity of the quantum state?



Low frequency region



Middle frequency region



High frequency region

Frequency dependent squeezing experiment
フリクエンスー ディペンデント クィーピング エクスぺリメント

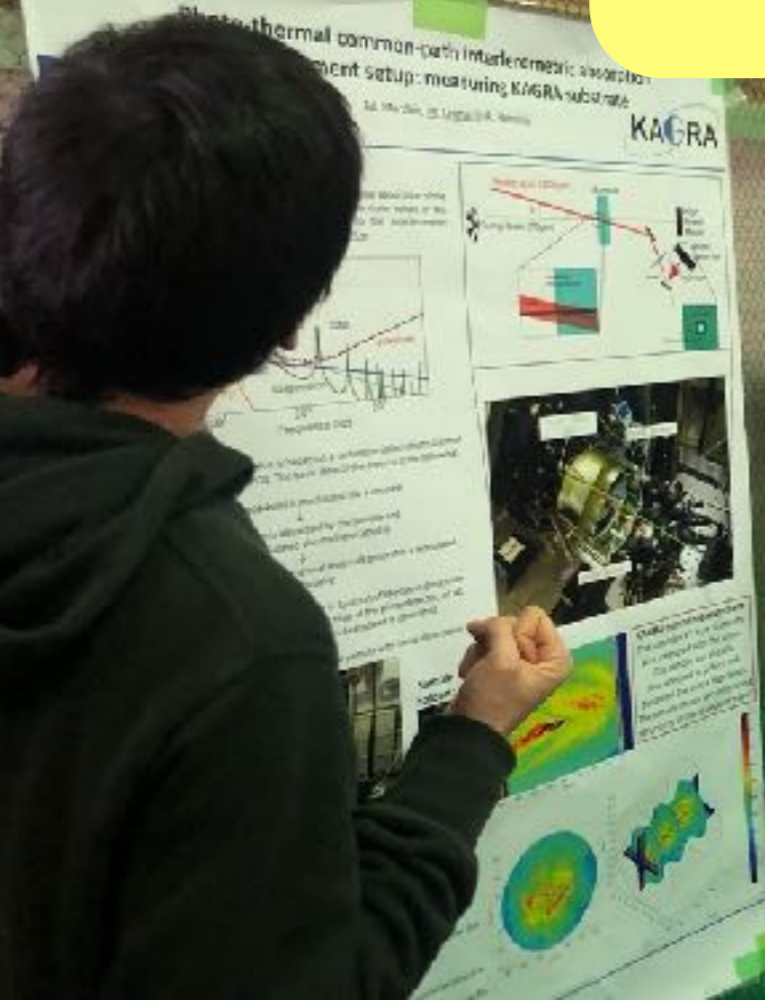
Dr. Marc Eisenmann (NAOJ)

Prof. Yoichi Aso (NAOJ)

Miss Hua Li Chen (NTHU)

Miss Yi-Ru Chen (NTHU)

Dr. Michael Page (NAOJ)



NAOJ, Feb. 2023

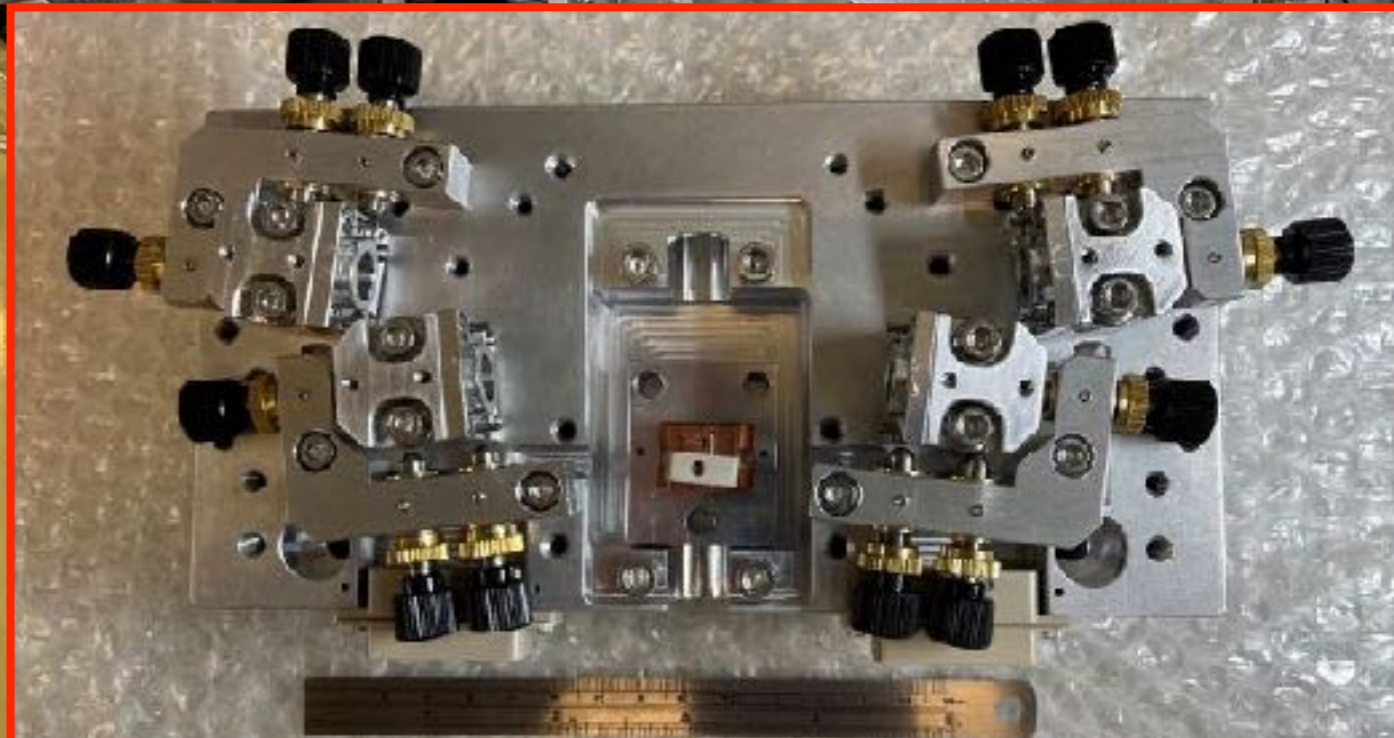


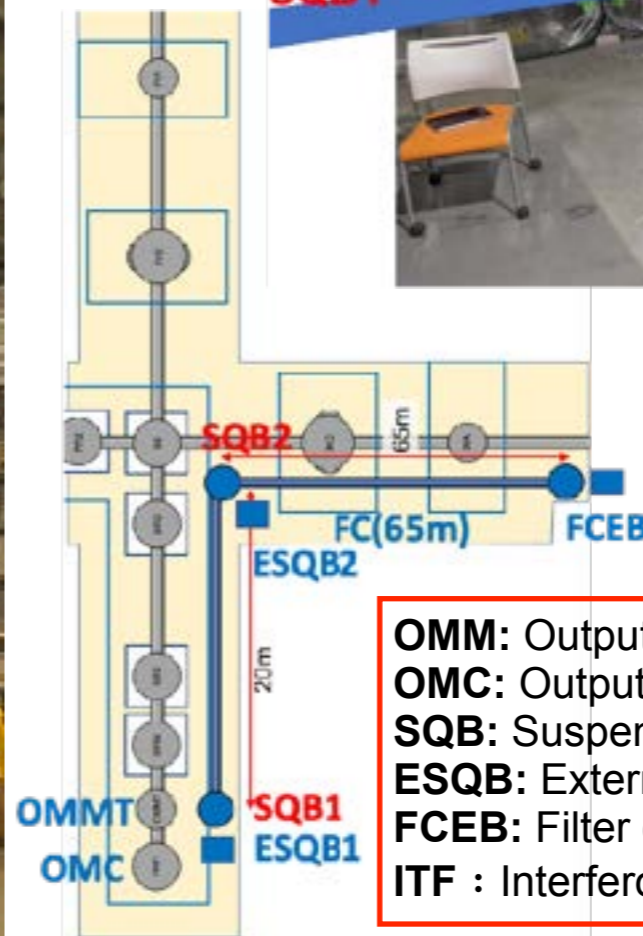
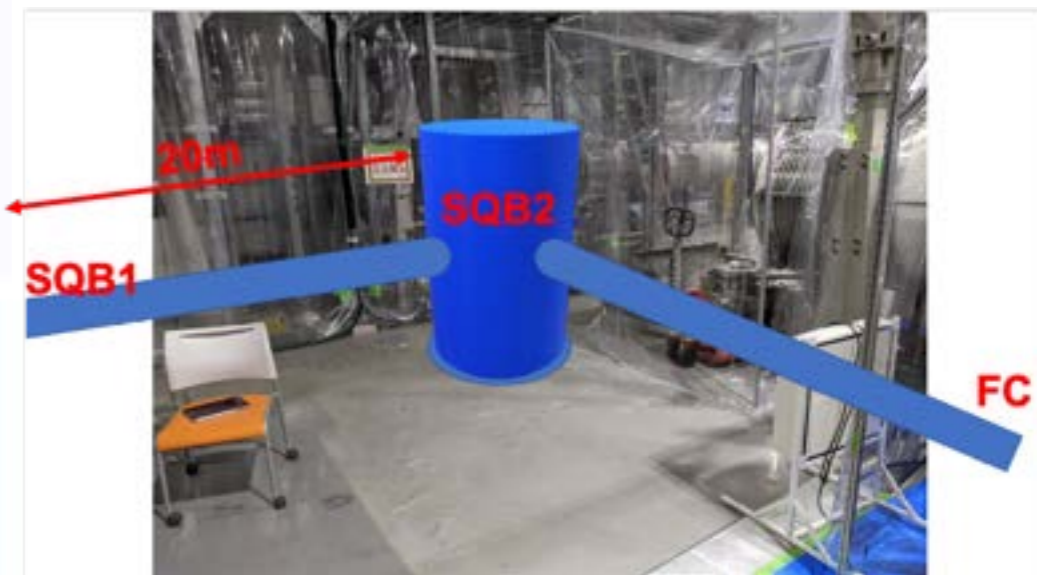
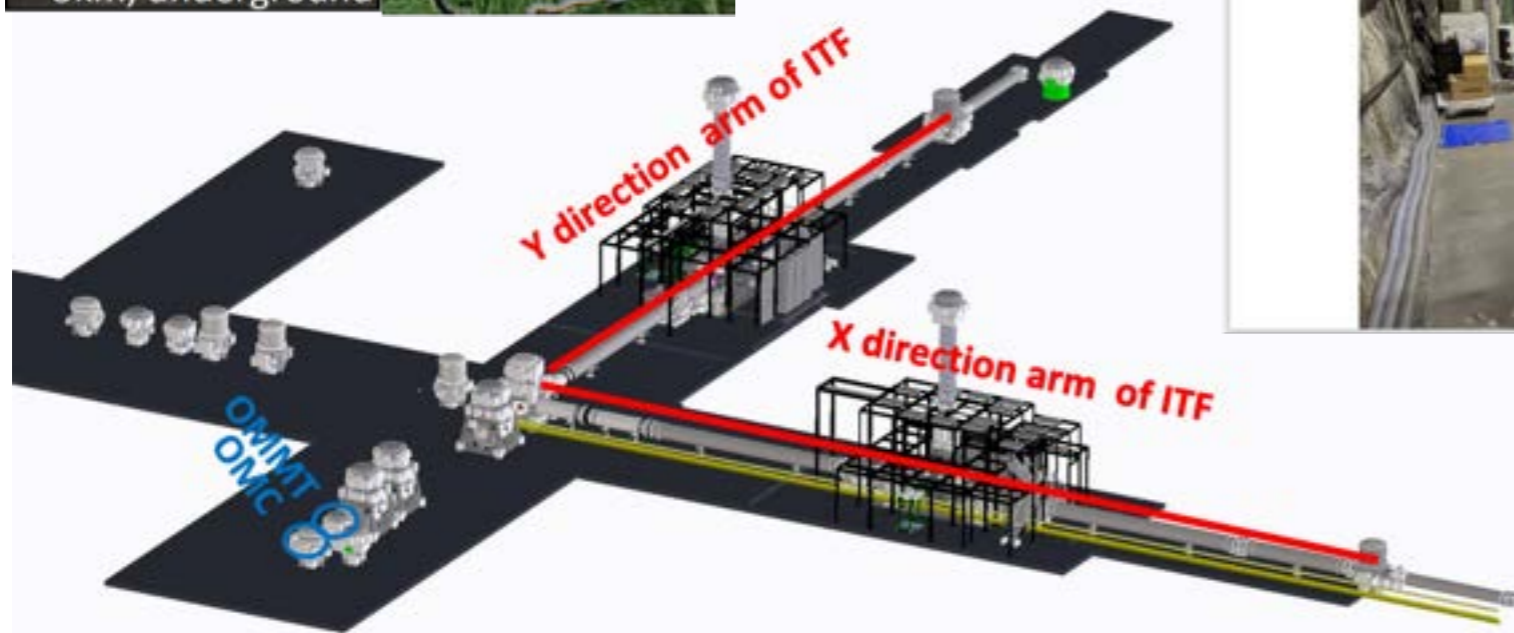
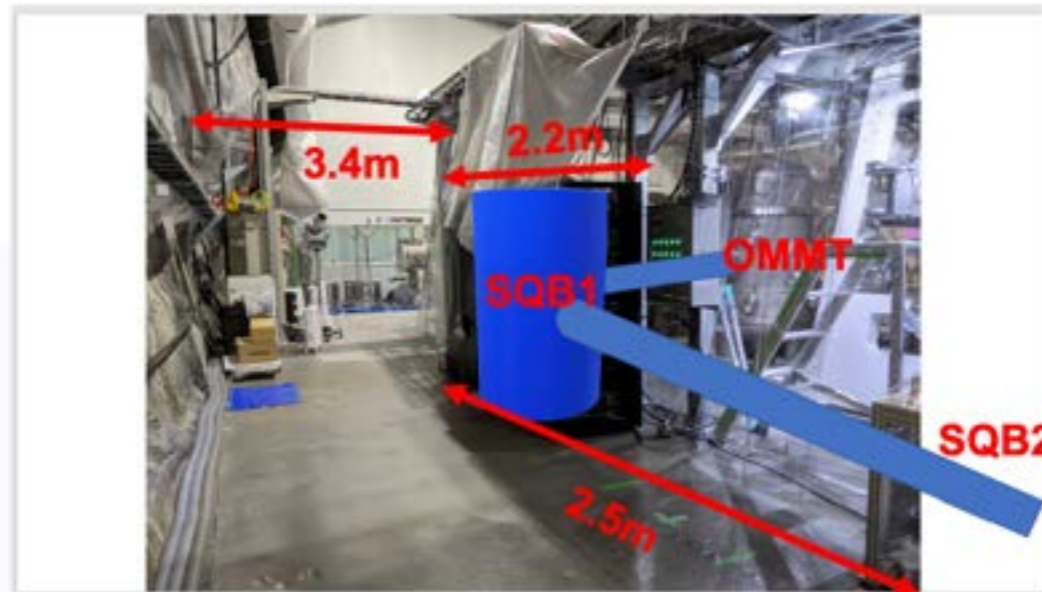
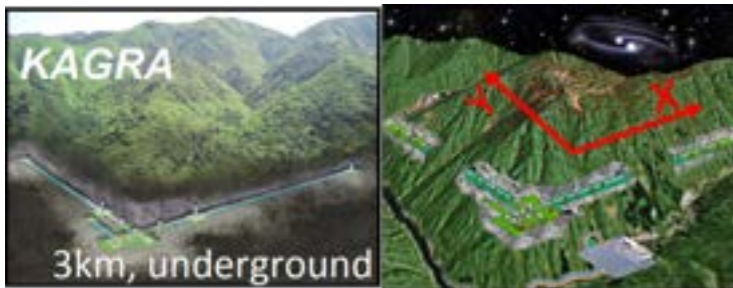
**Zi-Hao Shi
(NTHU)**

**Dr. Marc
Eisenmann (NAOJ)**

**Dr. Yi-Ru Chen
(NTHU)**

**Dr. Yuhang Zhao
(APC, U. Paris-7)**





by Hua Li Chen

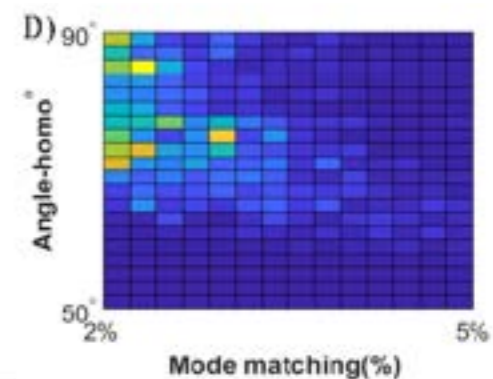
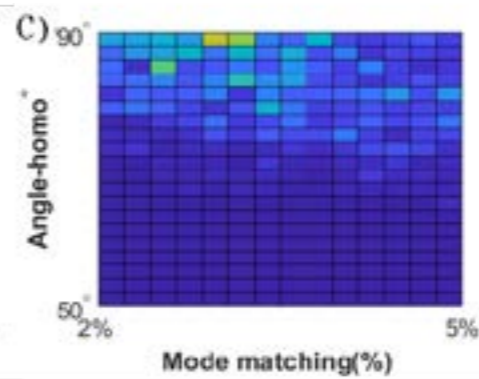
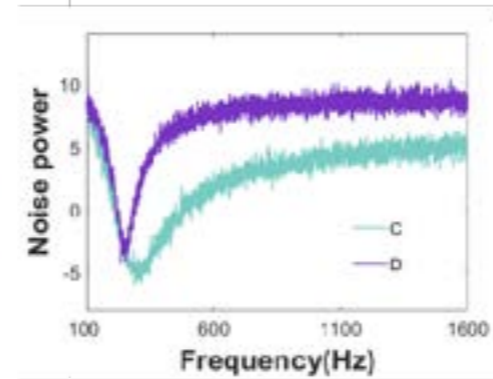
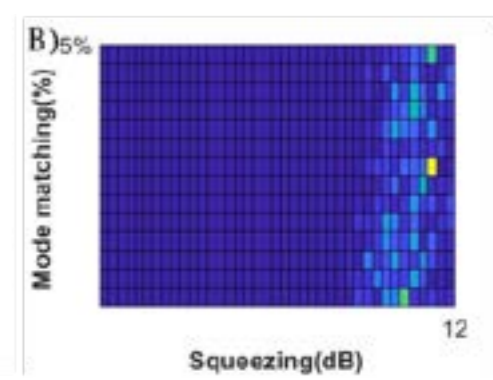
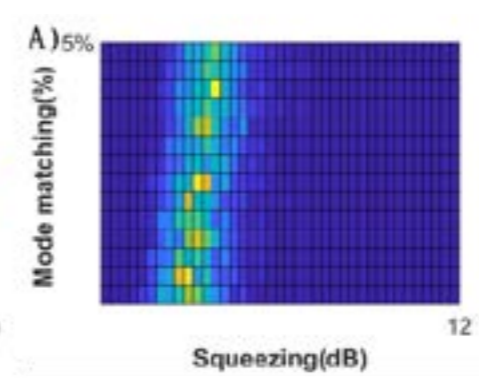
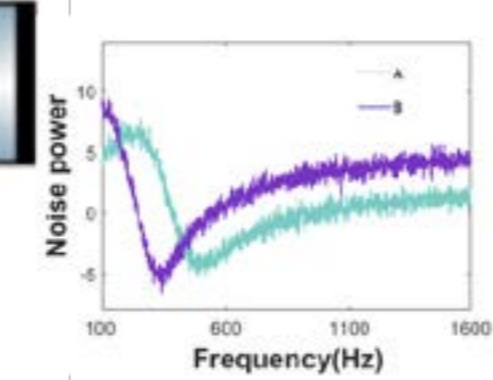
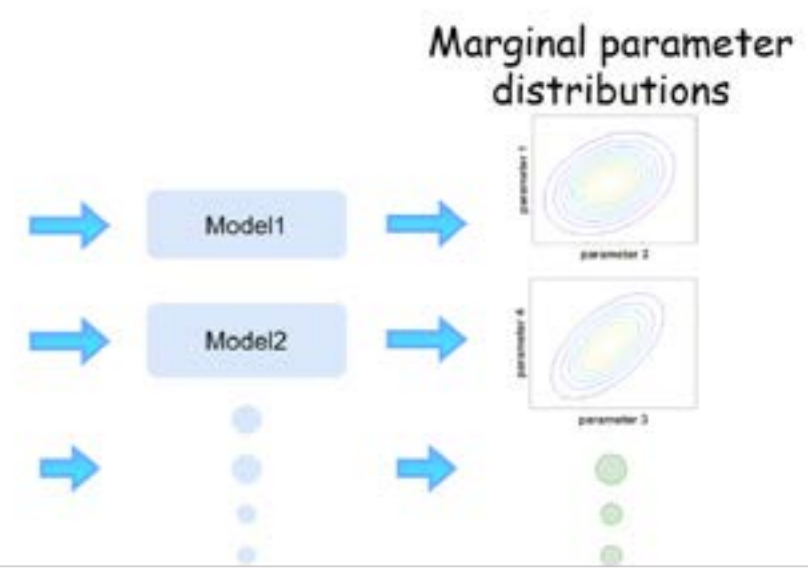
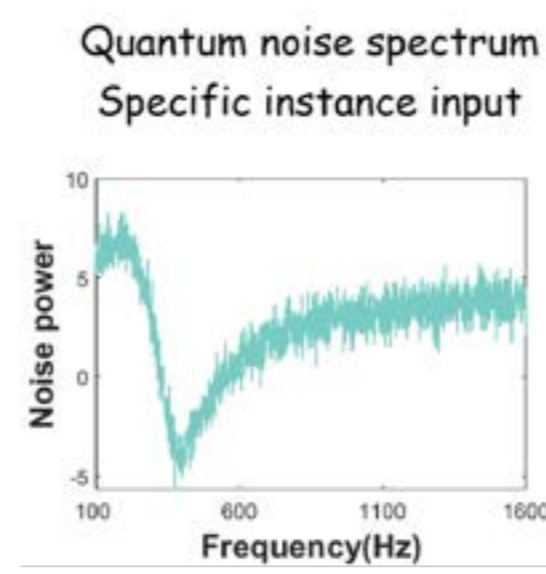
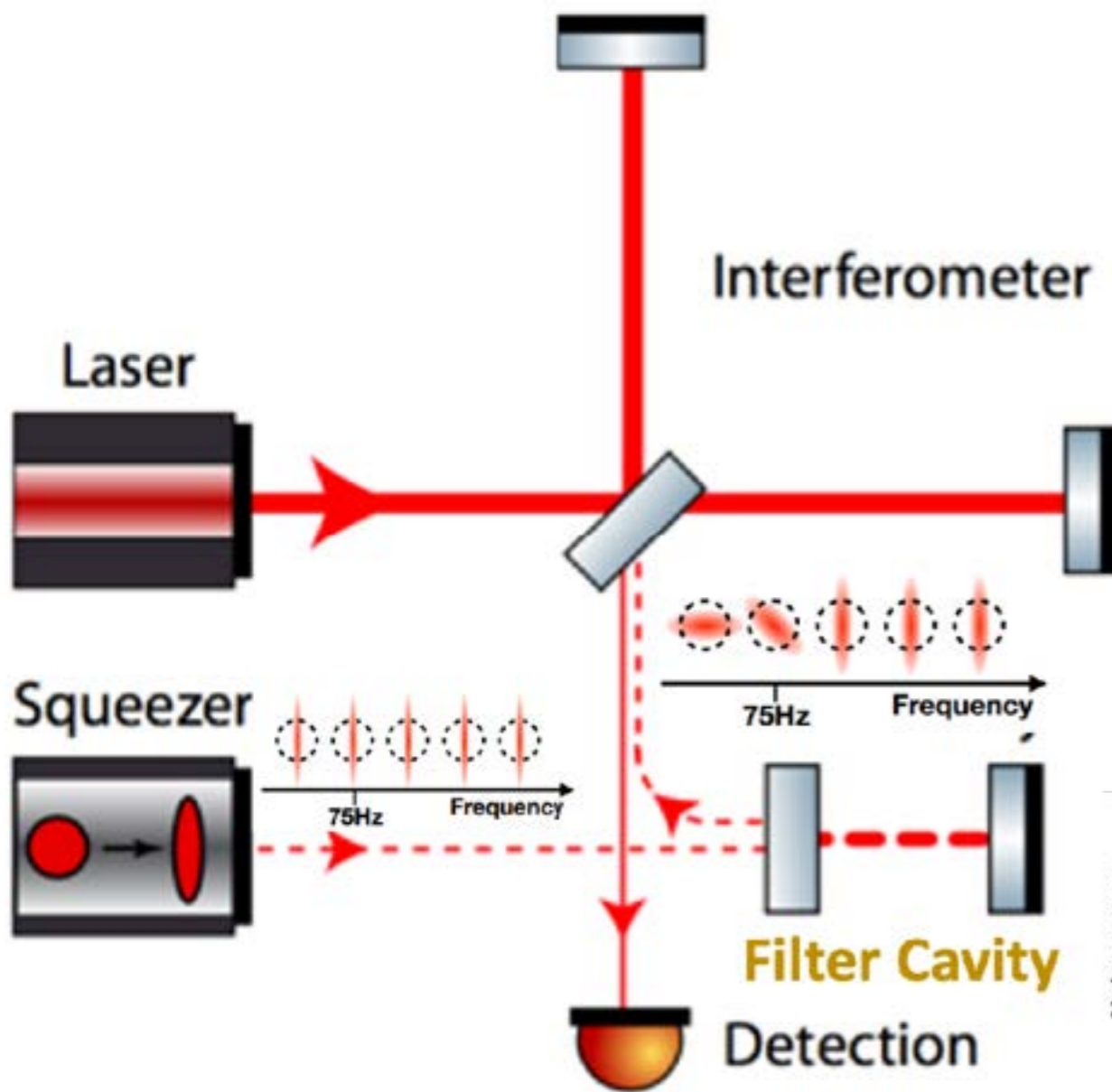
- OMM**: Output mode matching
- OMC**: Output mode cleaner
- SQB**: Suspended squeezing Bench
- ESQB**: External Suspended squeezing Bench
- FCEB**: Filter cavity external bench
- ITF** : Interferometer



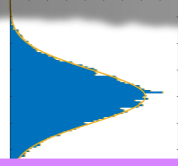
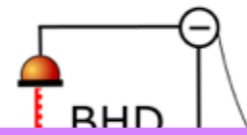
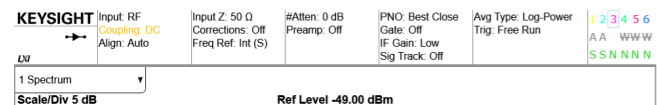
KAGRA, Sep. 2023

Machine-Learning for FDS

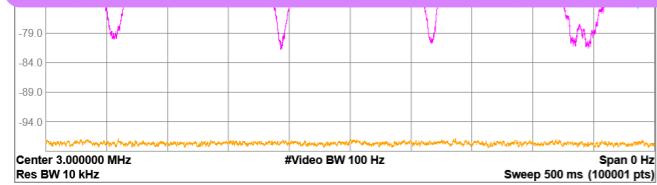
Multi-Parameters Bayesian Estimation



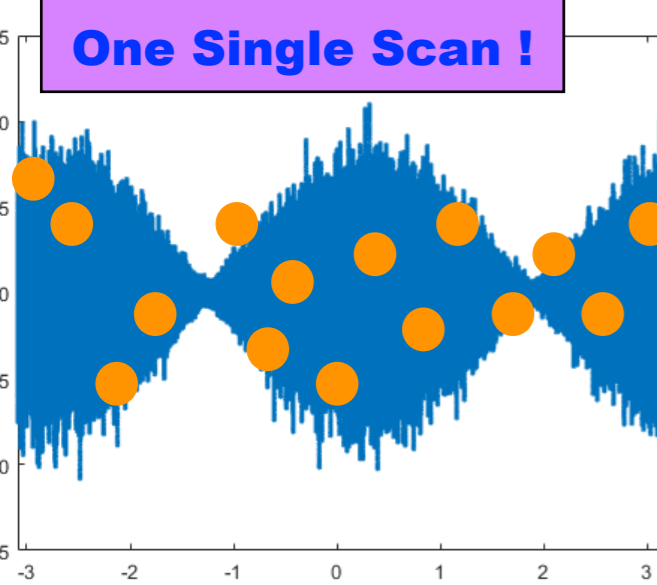
Summary



Accelerate with ML, but also **Re-use training data**



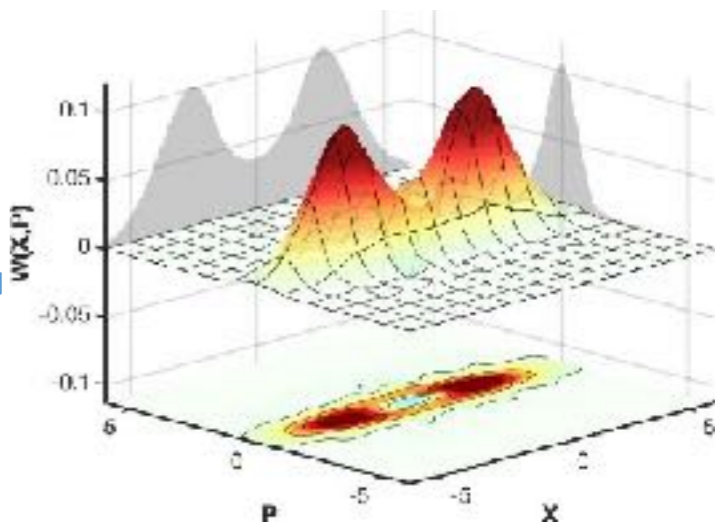
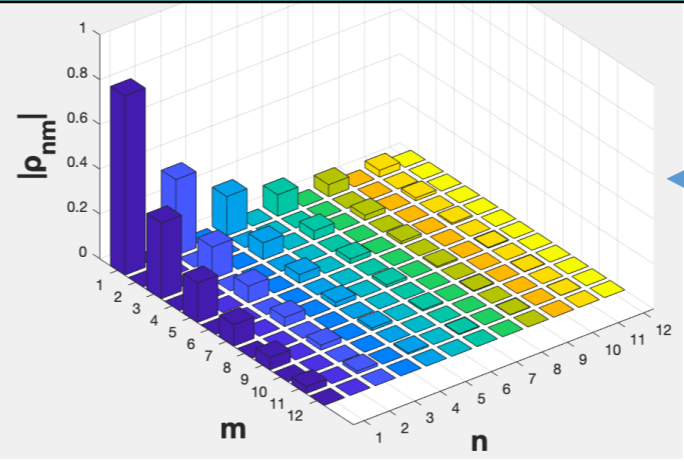
few minutes to reconstruct



< 1s to reconstruct

Local Oscillator
Max. Likelihood Estimation, MLE

Density matrix in number basis



arXiv:2306.13011 (2023);

Machine Learning (SQ Learner), CNN

Phys. Rev. Lett. 128, 073604 (2022);



ADVANCES IN PHYSICS: X
2023, VOL. 8, NO. 1, 2165452
<https://doi.org/10.1080/23746149.2023.2165452>

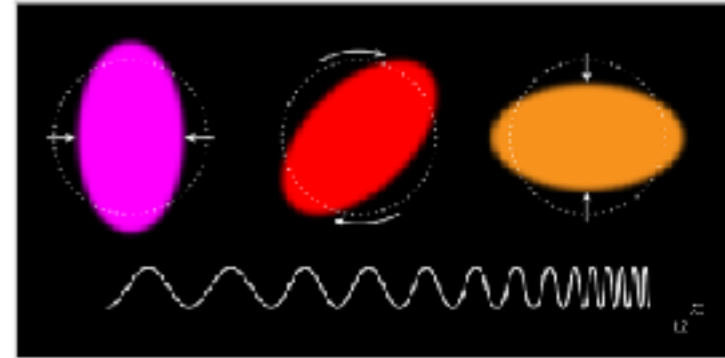


REVIEW

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Quantum machine learning: from physics to software engineering

Alexey Melnikov ^a, Mohammad Kordzanganeh ^a, Alexander Alodjants ^b and Ray-Kuang Lee ^{cd,ef}



Machine-Learning for FDS

ありがとうございました

Thanks for your attentions ^.^